

NTSE STAGE-II (2014)

CLASS-X [SAT]

HINTS & SOLUTIONS

ANSWER KEY

Ques.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Ans	4	2	3	1	4	2	3	2	4	3	4	4	1	2	3
Ques.	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
Ans	2	2	3	4	2	4	4	4	3	4	2	2	2	4	4
Ques.	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45
Ans	4	1	3	1	1	1	2	3	4	1	1	4	4	3	3
Ques.	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60
Ans	2	2	4	3	3	2	3	1	3	3	4	3	1	3	1
Ques.	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75
Ans	3	1	4	3	4	2	4	2	3	2	1	2	3	2	4
Ques.	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90
Ans	3	2	4	1	3	1	2	3	3	4	3	2	1	3	4
Ques.	91	92	93	94	95	96	97	98	99	100					
Ans	1	2	2	4	3	3	3	1	3	4					

CHEMISTRY

15. 15. Noise, vaccume and light flash not example of matter.

16. X Y
100 ML → water 100 ml → water
20°C
0°C → 100 g ← water 100 g ice ← 0°C

↓ more cooling
y is colder than x

17. At 313 k it from saturated solution. therefore all 50 gm. will be dissolve. when temperature down to 283 K (62 – 21 = 41 gm.) will be crystall cut.

18. A = Al B
z = 13 z = 8
valency = 3 valency = 2
= Al₂O₃

formula mass = 27 × 2 + 16 × 3
= 102

19. C_(g) + O₂ → CO_{2(g)}

mole of = $\frac{3}{12}$ mole of O₂ = $\frac{32}{32}$

$$= \frac{1}{4} = 1$$

→ LR

∴ 12 gm C give CO₂ = 44 gm

∴ 3 gm C give CO₂ = $\frac{44}{12} \times \frac{3}{1}$
= 11 gm

20. X → K, L, M ∴ M shell is the valency shell
2,8,7 therefore valency = 7
X = Cl

21. O₂ + H₂ → H₂O_(g)
O.S. of O₂ become → zero to - 2
∴ it will be reduced

and Oxidation state of H₂ becomes zero to + 1
it will be oxidised
∴ therefore reaction will be redox

22. NH₄OH + CH₃COOH → CH₃COONH₄ + H₂O
base acid salt
(neutralisation reaction)

2AgCl $\xrightarrow{h\nu}$ 2Ag + Br₂ (Photo chemical decomposition)

ZnCO₃ $\xrightarrow{\Delta}$ ZnO + CO₂ (thermla decompostion)
2Al + Fe₂O₃ → Al₂O₃ + 2Fe (Thermite reaction)

23. Order of acidic strength
 $\text{H}_2\text{SO}_4 > \text{HCl} > \text{NH}_4\text{OH} > \text{NaOH}$
Strongest acid **strong acid** **Weak base** **strong base**

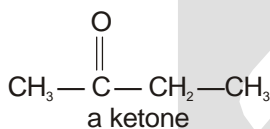
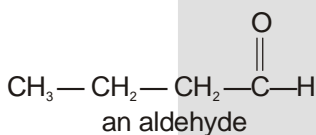
24. Na, K, Ca, Mg
 (i) \therefore these metals can lose e^- easily as compared to C therefore these are better reducing agent as compare to C.
 (ii) due to strong electropositive behaviour of these metals having strong tendency to react with oxygen.

25. Molecular formula $\rightarrow \text{C}_6\text{H}_{12}$



cyclohexane

26. M.F. $\text{C}_4\text{H}_8\text{O}$



27. (a) Atomic no 18
 it will be Ar \rightarrow inert gas
 valency = zero

(c) 9, 17, 35, all are belong same group that is 17 and have same valency.

(d) atomic no. 17 is Cl
 atomic no. 16 is S
 atomic no. 35 is Br
 \therefore Cl is more electronegative

PHYSICS

28. Body moving with constant speed can have acceleration only if it moves along a curved path.

29. $m = 20 \text{ Kg}$, $u = 2 \text{ m/s}$, $v = 0$, $S = 5 \text{ m}$
 $v^2 = u^2 - 2aS$
 $0 = 4 - 2a \times 5$
 $a = 0.4 \text{ m/s}^2$
 $F = ma = 20 \times 0.4 = 8 \text{ N}$

30. $F = \frac{G(m)(4m)}{(100 \times 10^3)^2}$

for smaller mass

$$m(1) = \frac{G(m)(4m)}{(10^{10})}$$

$$Gm = \frac{10^{10}}{4}$$

for bigger mass

$$(4m)(a) = \frac{G(m)(4m)}{(25 \times 10^3)^2}$$

$$a = \frac{Gm}{625 \times 10^{10}}$$

$$a = \frac{10^{10}}{4 \times 625 \times 10^6}$$

$$a = \frac{10^4}{2500}$$

$$a = 4 \text{ m/s}^2$$

31. Buoyant force
 $B = 0.02$

$$\rho_l g V' = 0.02$$

$$100 \times 10 \times V' = 0.02$$

$$V' = 0.02 \times 10^{-4} \text{ m}^3$$

$$= 2 \text{ cm}^3$$

32. Given : $F = 10 \text{ N}$, $m = 1 \text{ kg}$, $t = 2\text{s}$, $u = 0$
 $W = ?$

$$s = 0 + \frac{1}{2} (10/1) (2)^2 = 20 \text{ m}$$

$$W = 10 \times 20 = 200 \text{ J}$$

33. Stethoscope is based on multiple reflection of sound.

34. $\frac{\sin i}{\sin r} = \frac{v_1}{v_2} = n_{21}$

35. $f_1 = 0.5 \text{ m}$, $P_1 = \frac{1}{0.5} = 2 \text{ D}$

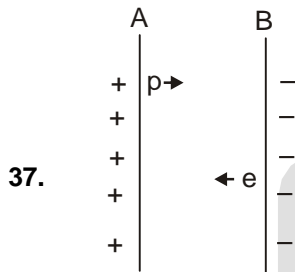
$$P_1 + P_2 = 1.5$$

$$2 + P_2 = 1.5$$

$$P_2 = -0.5 \text{ D}$$

$$\therefore f_2 = \frac{1}{-0.5} = -2 \text{ m}$$

36. Myopia, means person can see nearby objects.



$$W = \Delta KE$$

$$5(q) = \frac{1}{2} mv^2$$

$$v^2 = \frac{10q}{m}$$

$$m_p > m_e$$

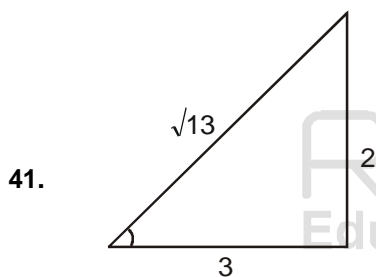
$$\therefore v_e > v_p$$

38. Magnetic field lines are continuous lines passing inside and outside the magnet, only one field line passes through a point

39. DC generator has split ring (commutator), whereas AC generator does not.

40. Energy of star is due to Nuclear Fusion.

MATHEMATICS



$$\left(\frac{1 + \frac{2}{3}}{\frac{2}{\sqrt{13}} + \frac{3}{\sqrt{13}}} \right) \left(\frac{1 - \frac{3}{2}}{\frac{\sqrt{13}}{3} + \frac{\sqrt{13}}{2}} \right)$$

$$= \left(\frac{\frac{5}{3}}{\frac{5}{\sqrt{13}}} \right) \left(\frac{\frac{-1}{2}}{\frac{5\sqrt{13}}{6}} \right)$$

$$= \frac{\sqrt{13}}{3} \times \left(\frac{-1}{2} \right) \times \frac{6}{5\sqrt{13}}$$

$$= -\frac{1}{5}$$

42.

$$\frac{1}{\sqrt{6} - \sqrt{5}} - \frac{3}{\sqrt{5} - \sqrt{2}} - \frac{4}{\sqrt{6} + \sqrt{2}}$$

$$\Rightarrow \sqrt{6} + \sqrt{5} - \sqrt{5} - \sqrt{2} - \sqrt{6} + \sqrt{2}$$

$$\Rightarrow 0$$

43.

$$p(x) = 3x^2 - 5x + 2$$

$$= 3\left(x^2 - \frac{5}{3}x + \frac{2}{3}\right)$$

$$= 3\left[x^2 - \frac{5}{3}x + \left(\frac{5}{6}\right)^2 - \left(\frac{5}{6}\right)^2 + \frac{2}{3}\right]$$

$$= 3\left[\left(x - \frac{5}{6}\right)^2 - \frac{25}{36} + \frac{2}{3}\right]$$

$$= 3\left[\left(x - \frac{5}{6}\right)^2 + \frac{-25 + 24}{36}\right]$$

$$= 3\left[\left(x - \frac{5}{6}\right)^2 - \frac{1}{36}\right]$$

$$= 3\left(x - \frac{5}{6}\right)^2 - \frac{1}{12}$$

so minimum value is $-\frac{1}{12}$

44. Let $|x| = y$

$$y^2 + y - 6 = 0$$

$$(y + 3)(y - 2) = 0$$

$$y = -3 \text{ or } y = 2$$

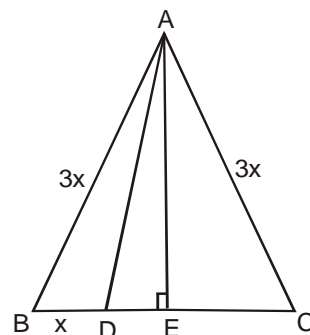
$$|x| = -3 \text{ which is not possible}$$

$$|x| = 2$$

$$\therefore x = \pm 2$$

The product of the roots is -4

45. $3x = 12, x = 4$



$$AE = \frac{\sqrt{3}}{2} (3x)$$

$$DE = AE - AD$$

$$= \frac{3x}{2} - x$$

$$= \frac{x}{2}$$

$$AD = \sqrt{AE^2 + DE^2}$$

$$= \sqrt{\frac{27}{4}x^2 + \frac{x^2}{4}}$$

$$= \sqrt{\frac{28x^2}{4}} = \sqrt{7x^2} = \sqrt{7}x = 4\sqrt{7}$$

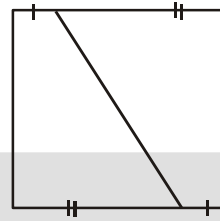
46. $\left(\frac{BX}{AB}\right)^2 = \frac{1}{2}$

$$\frac{BX}{AB} = \frac{1}{\sqrt{2}}$$

$$1 - \frac{BX}{AB} = 1 - \frac{1}{\sqrt{2}}$$

$$\frac{AB - BX}{AB} = \frac{\sqrt{2} - 1}{\sqrt{2}}$$

$$\frac{AX}{AB} = \frac{2 - \sqrt{2}}{2}$$



48.

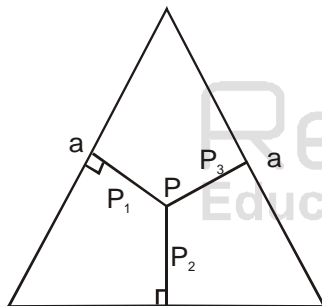
infinite tripezium can be made

- 49.
- | | |
|-----------------------|-------|
| 1 + 1 + 1 + 1 + 1 + 1 | 1 way |
| 2 + 1 + 1 + 1 + 1 | 5 way |
| 3 + 1 + 1 + 1 | 4 way |
| 4 + 1 + 1 | 3 way |
| 5 + 1 | 2 way |
| 2 + 3 + 1 | 6 way |
| 2 + 4 | 2 way |
| 3 + 3 | 1 way |
| 2 + 2 + 2 | 1 way |
| 2 + 2 + 1 + 1 | 6 way |

50.

$n^2 - 3n + 3 = m^2 \dots (1)$
 $n^2 - 3n + 3 - m^2 = 0$
 this eq. have integer roots. if $a = 1, b, c \in I$
 D is perfect sq.
 $\therefore 9 - 4 \cdot 1 \cdot (3 - m^2) = k^2$
 $4m^2 - k^2 = 3$
 $(2m + k)(2m - k) = 3 \times 1$
 $2m + k = 3$
 $2m - k = 1$
 on solving we get $m = 1$
 Put $m = 1$ in equ.(1)
 $n^2 - 3n + 3 = 1$
 $(n - 2) \times (n - 1) = 0$
 $n = 2, 1$
 so two values of n are possible

47.



area equilateral $D = \frac{\sqrt{3}}{4}a^2 = \frac{1}{2}a(P_1 + P_2 + P_3)$

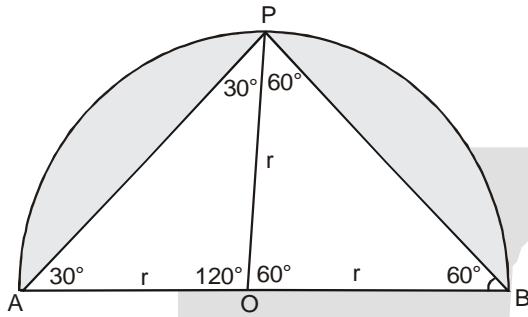
$$\frac{\sqrt{3}}{4}a^2 \times \frac{2}{a} = P_1 + P_2 + P_3$$

$$\frac{\sqrt{3}a}{2} = P_1 + P_2 + P_3$$

51.

$N_1 = 15x$
 $N_2 = 15y$ x and y are coprime
 $LCM \times HCF = N_1 \times N_2$
 $225 \times 15 = 15x \cdot 15y$
 $xy = 15$
 $3 \cdot 5 = 15$
 $1 \cdot 15 = 15$
 So, $N_1 = 3 \times 15 = 45$ or $N_1 = 1 \times 15 = 15$
 $N_2 = 5 \times 15 = 75$ or $N_2 = 15 \times 15 = 225$
 $(45, 75), (15, 225)$
 two such pair exist

52.



Let radius = r

area of sector APO

$$= \frac{120}{360} \times \pi r^2 = \frac{1}{3} \pi r^2$$

area of sector PBO = $\frac{60}{360} \times \pi r^2$

$$= \frac{1}{6} \pi r^2$$

Now area of $\triangle AOP = \frac{1}{2} \times \frac{\sqrt{3}r}{2} \times \frac{r}{2}$

$$= \frac{\sqrt{3}r^2}{4}$$

Now area of $\triangle BOP = \frac{\sqrt{3}}{4} r^2$

area of major shaded area : Area of minor shaded area

$$= \left(\frac{1}{3} \pi r^2 - \frac{\sqrt{3}}{4} r^2 \right) : \left(\frac{1}{6} \pi r^2 - \frac{\sqrt{3}}{4} r^2 \right)$$

$$= \frac{4\pi - 3\sqrt{3}}{2\pi - 3\sqrt{3}}$$

54.

$$x^2 + y^2 = 250$$

$$a^2 + b^2 + c^2 = 250$$

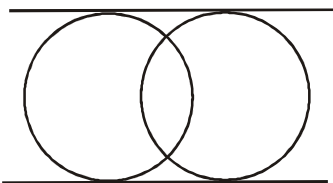
$$\therefore x = 13$$

$$y = 9$$

$$a = 5$$

$$b = 12$$

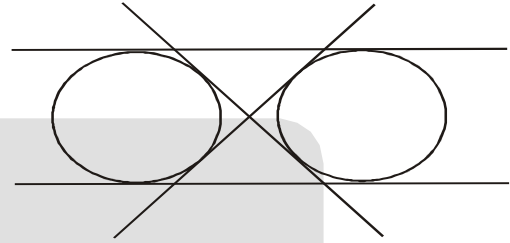
$$c = 9$$



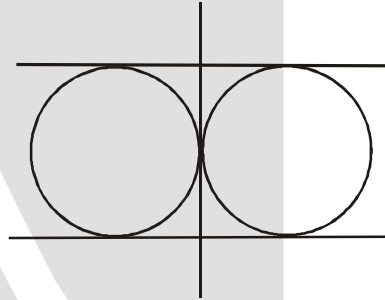
57.

(1)

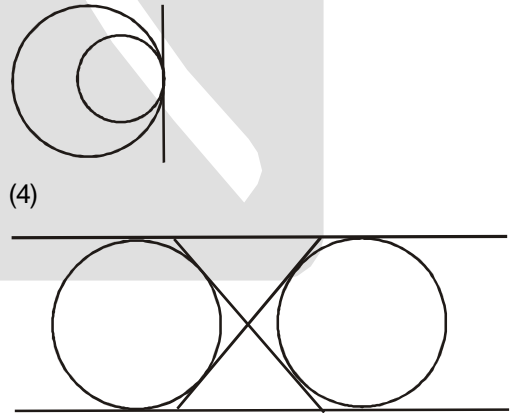
(2)



(3)



(4)



58.

$$s = \frac{20 + 21 + 29}{2} = 35$$

$$\Delta = \sqrt{35 \times 15 \times 14 \times 6}$$

$$= \sqrt{5 \times 7 \times 3 \times 5 \times 7 \times 2 \times 2 \times 3}$$

$$= 5 \times 7 \times 3 \times 2$$

$$= 210$$

$$210 = \frac{1}{2} A_1 \cdot 20$$

$$210 = \frac{1}{2} A_2 \cdot 29$$

$$A_1 = 21$$

$$A_2 = \frac{420}{29}$$

$$210 = \frac{1}{2} A_3 \times 21$$

$$A_3 = 20$$

$$A_1 + A_2 + A_3 = 21 + 20 + \frac{420}{29}$$

$$= 41 + \frac{420}{29}$$

$$= \frac{1189 + 420}{29} = \frac{1609}{29}$$

59. Let 4th term = $x + 3d = a$..(1)
 7th term = $x + 6d = b$..(2)
 10th term = $x + 9d = c$
 on solving (1) & (2) we get
 $x = 2a - b$

$$\& d = \frac{a - (2a - b)}{3}$$

$$10^{\text{th}} \text{ term} = x + 9d = C$$

$$2a - b + 9 \left(\frac{a - (2a - b)}{3} \right) = C$$

$$= 2a - b + 3a - 6a + 3b = C$$

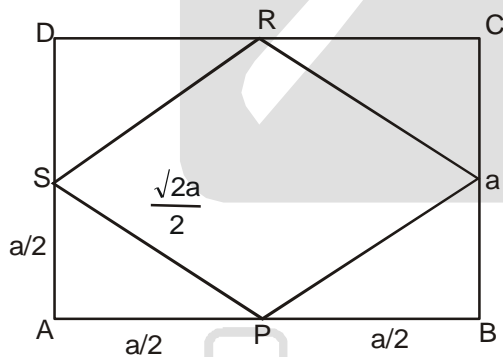
$$-a + 2b = C$$

$$2b = a + c$$

sum of roots of equation $ax^2 - 2bx + c = 0$

$$\text{sum of roots} = \frac{2b}{a} = \frac{a + c}{a}$$

60.



$$\frac{\text{area of square PQRS}}{\text{area of square PABCD}} = \frac{\frac{a^2}{2}}{a^2} = \frac{1}{2}$$