



# JEE MAIN 2016

## ONLINE EXAMINATION

### DATE : 10-04-2016

### SUBJECT : MATHEMATICS

## TEST PAPER WITH SOLUTIONS & ANSWER KEY

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1. Let C be a curve given by  $y(x) = 1 + \sqrt{4x-3}$ ,  $x > \frac{3}{4}$ . If P is a point on C, such that the tangent at P has slope  $\frac{2}{3}$ , then a point through which the normal at P passes, is

- (1) (3, -4)                      (2) (1, 7)                      (3) (4, -3)                      (4) (2, 3)

Ans. (2)

Sol.  $y(x) = 1 + \sqrt{4x-3}$ ,  $x > \frac{3}{4}$

Let  $P(\alpha, 1 + (\sqrt{4\alpha-3}))$  be the point.

at which

$$\frac{dy}{dx} \text{ at } P = \frac{2}{3}$$

$$\Rightarrow \frac{2}{\sqrt{4\alpha-3}} = \frac{2}{3}$$

$$\Rightarrow 4\alpha - 3 = 9$$

$$\Rightarrow \alpha = 3$$

Hence P(3,4)

slope of normal at P(3,4) is  $= -\frac{3}{2}$

equation of normal

$$Y - 4 = -\frac{3}{2}(X - 3)$$

$$2y - 8 = -3x + 9$$

$$3x + 2y = 17$$

clearly it passes through (1,7)

2. Let  $a, b \in \mathbb{R}$ , ( $a \neq 0$ ). If the function f defined as

$$f(x) = \begin{cases} \frac{2x^2}{a} & , 0 \leq x < 1 \\ a & , 1 \leq x < \sqrt{2} \\ \frac{2b^2 - 4b}{x^3} & , \sqrt{2} \leq x < \infty \end{cases}$$

- (1)  $(\sqrt{2}, 1 - \sqrt{3})$                       (2)  $(-\sqrt{2}, 1 - \sqrt{3})$                       (3)  $(\sqrt{2}, -1 + \sqrt{3})$                       (4)  $(-\sqrt{2}, 1 + \sqrt{3})$

Ans. (1)

Sol.  $f(x) = \begin{cases} \frac{2x^2}{a} & 0 \leq x < 1 \\ a & 1 \leq x < \sqrt{2} \\ \frac{2b^2 - 4b}{x^3} & \sqrt{2} \leq x < \infty \end{cases}$

is continuous in  $[0, \infty)$






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⇒ continuous at  $x = 1$  and  $x = \sqrt{2}$

$$\lim_{x \rightarrow 1^-} f(x) = \lim_{x \rightarrow 1^+} f(x) = f(1)$$

$$\Rightarrow \frac{2}{a} = a \Rightarrow a^2 = 2 \quad \text{----- (1)}$$

$$\text{and } \lim_{x \rightarrow \sqrt{2}^-} f(x) = \lim_{x \rightarrow \sqrt{2}^+} f(x) = f(\sqrt{2})$$

$$\Rightarrow a = \frac{2b^2 - 4b}{2\sqrt{2}}$$

$$\Rightarrow b^2 - 2b = \sqrt{2} a$$

$$\text{If } a = \sqrt{2} \text{ then } b^2 - 2b - 2 = 0 \Rightarrow b = 1 \pm \sqrt{3}$$

If  $a = -\sqrt{2}$  then  $b^2 - 2b + 2 = 0 \Rightarrow b$  is imaginary which is not possible

$$\Rightarrow (a, b) = (\sqrt{2}, 1 + \sqrt{3}) \text{ or } (\sqrt{2}, 1 - \sqrt{3})$$

3. Let  $a_1, a_2, a_3, \dots, a_n, \dots$  be in A.P. If  $a_3 + a_7 + a_{11} + a_{15} = 72$  then the sum of its first 17 terms is equal to

- (1) 153                      (2) 306                      (3) 612                      (4) 204

Ans. (2)

Sol.  $a_1, a_2, a_3, \dots, a_n, \dots$  are in A.P.

$$a_3 + a_{15} = a_7 + a_{11} = a_1 + a_{17} = 36$$

$$\begin{aligned} \text{sum of first 17 term} &= \frac{17}{2} (a_1 + a_{17}) \\ &= \frac{17}{2} \times 36 \\ &= 17 \times 18 \\ &= 306 \end{aligned}$$

4. If  $A > 0, B > 0$  and  $A + B = \frac{\pi}{6}$ , then the minimum value of  $\tan A + \tan B$  is

- (1)  $2 - \sqrt{3}$                       (2)  $\frac{2}{\sqrt{3}}$                       (3)  $\sqrt{3} - \sqrt{2}$                       (4)  $4 - 2\sqrt{3}$

Ans. (4)

Sol.  $A, B > 0$  and  $A + B = \frac{\pi}{6}$

$$\text{Let } y = \tan A + \tan B$$

$$\frac{dy}{dA} = \sec^2 A - \sec^2 \left( \frac{\pi}{6} - A \right)$$

$$\text{Hence } \tan A + \tan B \uparrow \forall A \in \left[ \frac{\pi}{12}, \frac{\pi}{6} \right]$$






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and  $\tan A + \tan B \downarrow \forall A \in \left[0, \frac{\pi}{12}\right]$

clearly  $\tan A + \tan B$  is minimum when

$$A = B = \frac{\pi}{12}$$

$$\begin{aligned} \Rightarrow y_{\min} &= 2 \tan \frac{\pi}{12} \\ &= (2 - \sqrt{3}) \times 2 = 4 - 2\sqrt{3} \end{aligned}$$

5. The contrapositive of the following statement,  
" If the side of a square doubles, then its area increases four times", is
- (1) If the area of a square does not increase four times, then its side is not doubled.
  - (2) If the area of a square increases four times, then its side is not doubled.
  - (3) If the area of a square increases four times, then its side is doubled.
  - (4) If the side of a square is not doubled, then its area does not increase four times.

Ans. (1)

Sol.  $p \equiv$  The side of a square doubles  
 $q \equiv$  Area of square increases four time  
 so the contrapositive of  $p \rightarrow q$  is  $\sim q \rightarrow \sim P$

6. Let A be a  $3 \times 3$  matrix such that  $A^2 - 5A + 7I = 0$ .
- Statement - I :  $A^{-1} = \frac{1}{7}(5I - A)$ .
- Statement - II : The polynomial  $A^3 - 2A^2 - 3A + I$  can be reduced to  $5(A - 4I)$ .
- Then
- (1) Statement-I is false, but Statement-II is true.
  - (2) Both the statements are false.
  - (3) Both the statements are true.
  - (4) Statement-I is true, but Statement-II is false.

Ans. (3)

Sol.  $A^2 - 5A + 7I = 0 \quad |A| \neq 0$   
 $\Rightarrow A - 5I = -7A^{-1}$   
 $\Rightarrow A^{-1} = \frac{1}{7}(5I - A)$

Hence statement 1 is true

$$\begin{aligned} \text{Now } A^3 - 2A^2 - 3A + I &= A(A^2) - 2A^2 - 3A + I \\ &= A(5A - 7I) - 2A^2 - 3A + I \\ &= 3A^2 - 10A + I \\ &= 5A - 20I = 3((5A - 7I) - 10A + I) \\ &= 5(A - 4I) \end{aligned}$$

Statement 2 also correct






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7. Equation of the tangent to the circle, at the point  $(1, -1)$ , whose centre is the point of intersection of the straight lines  $x - y = 1$  and  $2x + y = 3$  is

(1)  $3x - y - 4 = 0$       (2)  $x + 4y + 3 = 0$       (3)  $x - 3y - 4 = 0$       (4)  $4x + y - 3 = 0$

Ans. (2)

Sol. Centre of circle is  $\left(\frac{4}{3}, \frac{1}{3}\right)$

$$\Rightarrow \text{equation of circle is } \left(x - \frac{4}{3}\right)^2 + \left(y - \frac{1}{3}\right)^2 = \left(1 - \frac{4}{3}\right)^2 + \left(-1 - \frac{1}{3}\right)^2$$

$$\Rightarrow x^2 - \frac{8}{3}x + \frac{16}{9} + y^2 - \frac{2}{3}y + \frac{1}{9} = \frac{4}{9} + \frac{16}{9}$$

$$\Rightarrow x^2 + y^2 - \frac{8}{3}x - \frac{2}{3}y = 0$$

$$\Rightarrow 3x^2 + 3y^2 - 8x - 2y = 0$$

$$\text{Equation of tangent at } (1, -1) \text{ is } 3x - 3y - 4(x + 1) - (y - 1) = 0$$

$$\Rightarrow -x - 4y - 3 = 0$$

$$\Rightarrow x + 4y + 3 = 0$$

8. The sum  $\sum_{r=1}^{10} (r^2 + 1) \times (r!)$  is equal to

(1)  $10 \times (11!)$       (2)  $101 \times (10!)$       (3)  $(11!)$       (4)  $11 \times (11!)$

Ans. (1)

Sol.  $\sum_{r=1}^{10} (r^2 + 1) \cdot r!$

$$= \sum_{r=1}^{10} \{(r+1)^2 - 2r\} r!$$

$$= \sum_{r=1}^{10} (r+1)(r+1)! - 2 \sum_{r=1}^{10} r \cdot r!$$

$$= \sum_{r=1}^{10} \{(r+1)(r+1)! - r(r!)\} - \sum_{r=1}^{10} r \cdot r!$$

$$= (11 \cdot 11! - 1) - \sum_{r=1}^{10} \{(r+1)! - r!\}$$

$$= (11 \cdot 11! - 1) - (11! - 1!)$$

$$= 10 \cdot 11!$$






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9. Let ABC be a triangle whose circumcentre is at P. If the position vectors of A, B, C and P are  $\vec{a}, \vec{b}, \vec{c}$  and  $\frac{\vec{a} + \vec{b} + \vec{c}}{4}$  respectively, then the position vector of the orthocentre of this triangle, is

- (1)  $\vec{0}$                       (2)  $-\left(\frac{\vec{a} + \vec{b} + \vec{c}}{2}\right)$                       (3)  $\vec{a} + \vec{b} + \vec{c}$                       (4)  $\left(\frac{\vec{a} + \vec{b} + \vec{c}}{2}\right)$

Ans. (4)

Sol. Position vector of the centroid of  $\Delta ABC$  is  $= \left(\frac{\vec{a} + \vec{b} + \vec{c}}{3}\right)$

Now we know that centroid divides the line joining orthocentre to circum centre divided by centroid divided by centroid in the ratio in 2 : 1

$$\Rightarrow \text{orthocentre} = 3\left(\frac{\vec{a} + \vec{b} + \vec{c}}{3}\right) - 2\left(\frac{\vec{a} + \vec{b} + \vec{c}}{4}\right) = \left(\frac{\vec{a} + \vec{b} + \vec{c}}{2}\right)$$

10. Let  $f(x) = \sin^4 x + \cos^4 x$ . Then f is an increasing function in the interval

- (1)  $\left[\frac{\pi}{4}, \frac{\pi}{2}\right]$                       (2)  $\left[\frac{5\pi}{8}, \frac{3\pi}{4}\right]$                       (3)  $\left]0, \frac{\pi}{4}\right[$                       (4)  $\left]\frac{\pi}{2}, \frac{5\pi}{8}\right[$

Ans. (1)

Sol.  $f(x) = \sin^4 x + \cos^4 x$   
 $f'(x) = 4\sin^3 x \cos x - 4\cos^3 x \sin x$   
 $= 4\sin x \cos x (\sin^2 x - \cos^2 x)$   
 $= -2\sin 2x \cdot \cos 2x$   
 $= -\sin 4x > 0$   
 $\Rightarrow \sin 4x < 0$   
 $\Rightarrow \pi < 4x < 2\pi$   
 $\frac{\pi}{4} < x < \frac{\pi}{2}$

11. Let  $z = 1 + ai$  be a complex number,  $a > 0$  such that  $z^3$  is a real number. Then the sum  $1 + z + z^2 + \dots + z^{11}$  is equal to

- (1)  $-1250\sqrt{3}i$                       (2)  $1250\sqrt{3}i$                       (3)  $-1365\sqrt{3}i$                       (4)  $1365\sqrt{3}i$

Ans. (3)

Sol.  $z = 1 + ai, \quad a > 0$   
 $z^3 = 1 - 3a^2 + (3a - a^3)i$  is a real number  
 $\Rightarrow 3a - a^3 = 0$   
 $\Rightarrow a^2 = 3$   
 $\Rightarrow a = \sqrt{3}, \quad a > 0$   
 $\Rightarrow z = 1 + \sqrt{3}i$   
 $= 2\left(\cos\frac{\pi}{3} + i\sin\frac{\pi}{3}\right)$

$$\text{Now } 1 + z + z^2 + \dots + z^{11} = \frac{1(1 - z^{12})}{1 - z} = \frac{1 - 2^{12}(\cos 4\pi + i\sin 4\pi)}{1 - (1 + i\sqrt{3})} = \frac{1 - 2^{12}}{-i\sqrt{3}} = \frac{4095}{i\sqrt{3}} = -1365\sqrt{3}i$$






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12. Let  $P = \{ \theta : \sin\theta - \cos\theta = \sqrt{2} \cos\theta \}$  and  $Q = \{ \theta : \sin\theta + \cos\theta = \sqrt{2} \sin\theta \}$  be two sets. Then  
 (1)  $Q \not\subset P$  (2)  $P \not\subset Q$  (3)  $P \subset Q$  and  $Q - P \neq \phi$  (4)  $P = Q$

Ans. (4)

Sol. For Let P

$$\sin\theta = \cos\theta(\sqrt{2} + 1)$$

$$(\sqrt{2} - 1) \sin\theta = \cos\theta \quad \dots (i)$$

For Let Q

$$\cos\theta = (\sqrt{2} - 1) \sin\theta \quad \dots (ii)$$

(i) & (ii) are same  $P = Q$

13. The mean of 5 observations is 5 and their variance is 124. If three of the observations are 1, 2 and 6, then the mean deviation from the mean of the data is

- (1) 2.5 (2) 2.8 (3) 2.6 (4) 2.4

Ans. (Bonus)

Sol. This question is wrong

$$\bar{x} = \frac{x_1 + x_2 + x_3 + x_4 + x_5}{5} = 5$$

$$\sum_{i=1}^5 x_i = 25 \dots\dots\dots(i)$$

Also  $\sigma^2 = 124$

$$\Rightarrow \frac{\sum x_i^2}{5} - (\bar{x})^2 = 124$$

$$\Rightarrow \frac{\sum x_i^2}{5} = 124 + 25 = 149$$

$$\Rightarrow (x_1^2 + x_2^2 + \dots + x_5^2) = 745$$

$$\Rightarrow x_1^2 + x_2^2 = 704 \dots\dots\dots(ii)$$

by (i)  $x_1 + x_2 = 16 \dots\dots\dots(iii)$

$$2x_1 x_2 + 704 = 256$$

$$x_1 x_2 = \frac{256 - 704}{2}$$

$$x_1 x_2 = 128 - 352 = -224 \dots\dots\dots(iv)$$

Now 
$$\frac{\sum |x_i - 5|}{5} = \frac{|x_1 - 5| + |x_2 - 5| + 4 + 3 + 1}{5}$$

$$= \frac{8 + |x_1 - 5| + |11 - x_1|}{5}$$

$$= \frac{8 + 6}{5} = 2.8 \text{ Ans}$$






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14. The number of distinct real values of  $\lambda$  for which the lines  $\frac{x-1}{1} = \frac{y-2}{2} = \frac{z+3}{\lambda^2}$  and  $\frac{x-3}{1} = \frac{y-2}{\lambda^2} = \frac{z-1}{2}$  are coplanar is  
 (1) 3 (2) 2 (3) 1 (4) 4

Ans. (1)

Sol. 
$$\begin{vmatrix} 1 & 2 & \lambda^2 \\ 1 & \lambda^2 & 2 \\ 2 & 0 & 4 \end{vmatrix} = 0$$

$$4\lambda^2 - 2(0) + \lambda^2(-2\lambda^2) = 0$$

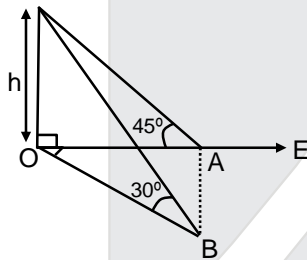
$$2\lambda^2[2 - \lambda^2] = 0$$

$$\lambda = 0 \quad \lambda = \pm\sqrt{2}$$

15. The angle of elevation of the top of a vertical tower from a point A, due east of it is  $45^\circ$ . The angle of elevation of the top of the same tower from a point B, due south of A is  $30^\circ$ . If the distance between A and B is  $54\sqrt{2}$  m, then the height of the tower (in metres), is  
 (1) 54 (2) 108 (3)  $54\sqrt{3}$  (4)  $36\sqrt{3}$

Ans. (1)

Sol. Let height of tower is h.



$$\Rightarrow OA = h$$

$$OB = \sqrt{3}h$$

$$\text{Also } OB^2 = OA^2 + AB^2$$

$$\Rightarrow 3h^2 = h^2 + (54\sqrt{2})^2 \Rightarrow h = 54$$

16.  $\lim_{x \rightarrow 0} \frac{(1 - \cos 2x)^2}{2x \tan x - x \tan 2x}$  is  
 (1) 2 (2)  $-\frac{1}{2}$  (3)  $\frac{1}{2}$  (4) -2

Ans. (1)

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Sol.

$$\frac{(2\sin^2 x)^2}{x \left[ 2 \left( x - \frac{x^3}{3} + \frac{2x^5}{15} \dots \right) - \left( 2x - \frac{8x^3}{3} \dots \right) \right]}$$

$$= \frac{4\sin^4 x}{x^4 \left[ -\frac{2}{3} + \frac{8}{3} \right]} = \frac{4}{2} = 2$$

17. The solution of the differential equation  $\frac{dy}{dx} + \frac{y}{2} \sec x = \frac{\tan x}{2y}$ , where  $0 \leq x < \frac{\pi}{2}$  and  $y(0) = 1$ , is given by

(1)  $y^2 = 1 - \frac{x}{\sec x + \tan x}$

(2)  $y^2 = 1 + \frac{x}{\sec x + \tan x}$

(3)  $y = 1 + \frac{x}{\sec x + \tan x}$

(4)  $y = 1 - \frac{x}{\sec x + \tan x}$

Ans. (1)

Sol.  $2y \frac{dy}{dx} + y^2 \sec x = \tan x$

put  $y^2 = t \Rightarrow 2y \frac{dy}{dx} = \frac{dt}{dx}$

$\frac{dt}{dx} + t \sec x = \tan x$

I.F. =  $e^{\int \sec x dx} = e^{\ln(\sec x + \tan x)} = \sec x + \tan x$

$t(\sec x + \tan x) = \int (\sec x + \tan x) \tan x dx$   
 $= \int \sec x \tan x dx + \int \tan^2 x dx$

$y^2(\sec x + \tan x) = \sec x + \tan x - x + c$

$y(0) = 1 \Rightarrow c = 0$

$\Rightarrow y^2 = 1 - \frac{x}{\sec x + \tan x}$

18. P and Q are two distinct points on the parabola,  $y^2 = 4x$ , with parameters  $t$  and  $t_1$  respectively. If the normal at p passes through Q, then the minimum value of  $t_1^2$  is

(1) 4

(2) 6

(3) 8

(4) 2

Ans. (3)






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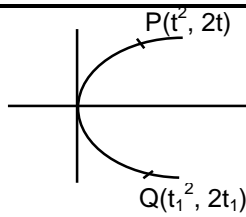
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Sol.



$$t_1 = -t - \frac{2}{t}$$

$$t_1^2 = t^2 + \frac{4}{t^2} + 4$$

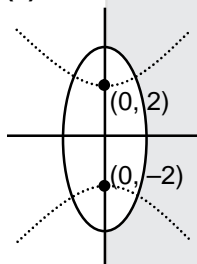
$$\text{min of } t_1^2 = 8$$

19. A hyperbola whose transverse axis is along the major axis of the conic,  $\frac{x^2}{3} + \frac{y^2}{4} = 4$  and has vertices at the foci of this conic. If the eccentricity of the hyperbola is  $\frac{3}{2}$ , then which of the following points does NOT lie on it ?

- (1)  $(\sqrt{5}, 2\sqrt{2})$       (2)  $(5, 2\sqrt{3})$       (3)  $(0, 2)$       (4)  $(\sqrt{10}, 2\sqrt{3})$

Ans. (2)

Sol.

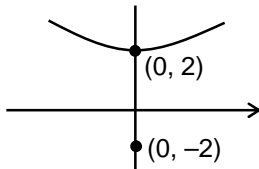


ellipse  $\frac{x^2}{12} + \frac{y^2}{16} = 1$

foci  $(0, \pm be)$

$$e_e = \sqrt{1 - \frac{12}{16}} = \frac{1}{2}$$

for hyperbola



$$h_H = 2$$






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$$e_H = \frac{3}{2}$$

$$\text{equation} \Rightarrow \frac{x^2}{a^2} - \frac{y^2}{b^2} = -1$$

$$e_H = \frac{3}{2} = \sqrt{1 + \frac{a^2}{b^2}} \Rightarrow \frac{9}{4} - 1 = \frac{a^2}{b^2}$$

$$\frac{a^2}{b^2} = \frac{5}{4} \Rightarrow a^2 = 5$$

$$\frac{x^2}{5} - \frac{y^2}{4} = -1$$

Clearly point  $(5, 2\sqrt{3})$  does not lie on it.

20. For  $x \in \mathbb{R}$ ,  $x \neq 0$ , if  $y(x)$  is a differentiable function such that  $x \int_1^x y(t) dt = (x+1) \int_1^x ty(t) dt$ , then  $y(x)$  equals

(where  $C$  is a constant)

(1)  $Cx^3 e^{\frac{1}{x}}$

(2)  $\frac{C}{x} e^{-\frac{1}{x}}$

(3)  $\frac{C}{x^2} e^{-\frac{1}{x}}$

(4)  $\frac{C}{x^3} e^{-\frac{1}{x}}$

Ans. (4)

Sol.  $x \int_1^x y(t) dt = (x+1) \int_1^x ty(t) dt \dots(i)$

differentiate equation (1)

$$xy(x) + \int_1^x y(t) dt = (x+1)xy(x) + \int_1^x ty(t) dt$$

$$\int_1^x y(t) dt = x^2y(x) + \int_1^x ty(t) dt$$

again differentiate

$$y(x) = 2xy(x) + x^2y'(x) + xy(x)$$

$$y = 3xy + x^2 \frac{dy}{dx}$$

$$y(1-3x) = x^2 \frac{dy}{dx}$$

$$\frac{(1-3x)}{x^2} dx = \frac{dy}{y}$$






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solve differential equation

$$-\frac{1}{x} - 3\ln x = \ln y + \ln c$$

$$-\frac{1}{x} = \ln x^3 y + \ln c$$

$$x^3 y c = e^{-1/x}$$

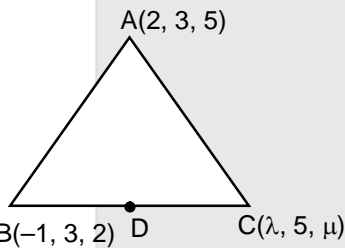
$$y = \frac{c}{x^3} e^{-1/x}$$

21. ABC is a triangle in a plane with vertices A(2,3,5), B(-1,3,2) and C(λ, 5, μ). If the median through A is equally inclined to the coordinate axes, then the value of (λ<sup>3</sup> + μ<sup>3</sup> + 5) is

(1) 676 (2) 1130 (3) 1348 (4) 1077

Ans. (3)

Sol.



$$D \equiv \left( \frac{-1+\lambda}{2}, 4, \frac{2+\mu}{2} \right)$$

$$\text{direction cosine of AD} = \left\{ \frac{-1+\lambda}{2} - 2, 4 - 3, \frac{2+\mu}{2} - 5 \right\}$$

$$\left\{ \frac{-1+\lambda}{2} - 2, 4 - 3, \frac{2+\mu}{2} - 5 \right\}$$

$$\vec{AD} = \frac{\lambda-5}{2} \hat{i} + \hat{j} + \frac{\mu-8}{2} \hat{k}$$

$$\Rightarrow \frac{\left( \frac{\lambda-5}{2} \right)}{\sqrt{\left( \frac{\lambda-5}{2} \right)^2 + 1^2 + \left( \frac{\mu-8}{2} \right)^2}} = \frac{1}{\sqrt{\left( \frac{\lambda-5}{2} \right)^2 + 1 + \left( \frac{\mu-8}{2} \right)^2}} = \frac{\left( \frac{\mu-8}{2} \right)}{\sqrt{\left( \frac{\lambda-5}{2} \right)^2 + 1 + \left( \frac{\mu-8}{2} \right)^2}}$$

$$\vec{AD} \cdot \hat{i} = \vec{AD} \cdot \hat{j} = \vec{AD} \cdot \hat{k}$$

$$\lambda = 7, \quad \mu = 10$$

$$\lambda^3 + \mu^3 + 5 = 343 + 1000 + 5 = 1348$$






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22. A ray of light is incident along a line which meets another line,  $7x - y + 1 = 0$ , at the point  $(0, 1)$ . The ray is then reflected from this point along the line,  $y + 2x = 1$ . Then the equation of the line of incidence of the ray of light is

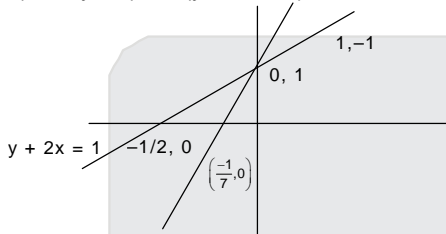
(1)  $41x + 38y - 38 = 0$  (2)  $41x - 38y + 38 = 0$  (3)  $41x + 25y - 25 = 0$  (4)  $41x - 25y + 25 = 0$

Ans. (2)

Sol. Incidence line

$$L_1 + \lambda L_2 = 0$$

$$(7x - y + 1) + \lambda(y + 2x - 1) = 0$$



Let a point  $(1, -1)$  on  $y + 2x = 1$

And image of  $(1, -1)$  lie on incidence line in

$$7x - y + 1 = 0$$

$$\frac{x-1}{1} = \frac{y+1}{-1} = \frac{-2(7+1+1)}{50} = x = \frac{-38}{25}, \quad y = \frac{-16}{25}$$

$$\left(7\left(\frac{-38}{25}\right) + \frac{16}{25} + 1\right) + \lambda\left(\frac{-16}{25} - \frac{76}{25} - 1\right)$$

$$\lambda = \frac{-225}{117}$$

$$(7x - y + 1) - \frac{225}{117}(y + 2x - 1) = 0$$

$$369x - 342y + 342 = 0$$

$$41x - 38y + 38 = 0$$

23. A straight line through origin  $O$  meets the line  $3y = 10 - 4x$  and  $8x + 6y + 5 = 0$  at points  $A$  and  $B$  respectively. Then  $O$  divides the segment  $AB$  in the ratio

(1)  $3 : 4$  (2)  $1 : 2$  (3)  $2 : 3$  (4)  $4 : 1$

Ans. (4)

Sol. Let equation of line through  $O(0, 0)$  is  $\frac{x}{\cos\theta} = \frac{y}{\sin\theta} = r$ . If this line meets  $3y = 10 - 4x$  at  $A$  then

$$3r, \sin\theta = 10 - 4r_1 \cos\theta$$

$$r_1(3\sin\theta + 4\cos\theta) = 10 \dots\dots(i)$$

Again the line meets  $8x + 6y + 5 = 0$  at  $B$

$$\Rightarrow 8r_2 \cos\theta + 6r_2 \sin\theta + 5 = 0$$

$$\Rightarrow 2r_2(3\sin\theta + 4\cos\theta) = -5 \dots\dots(ii)$$

$$\text{by } \frac{1}{2} \Rightarrow \frac{r_1}{2r_2} = \frac{10}{-5} \Rightarrow \frac{r_1}{r_2} = -\frac{4}{1} = 4$$

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24. The value of the integral  $\int_4^{10} \frac{[x^2]dx}{[x^2 - 28x + 196] + [x^2]}$ , where  $[x]$  denotes the greatest integer less than or equal to  $x$ , is

- (1) 3                                      (2) 7                                      (3) 6                                      (4)  $\frac{1}{3}$

Ans. (1)

Sol.  $I = \int_4^{10} \frac{[x^2]dx}{[x^2 - 28x + 196] + [x^2]} \dots\dots(i)$

Use property  $\int_a^b f(a+b-x)dx = \int_a^b f(x)dx$

$\Rightarrow I = \int_4^{10} \frac{[x^2 - 28x + 196]dx}{[x^2] + [x^2 - 28x + 196]} \dots\dots(ii)$

by (i) and (ii)

$2I = \int_4^{10} dx = 10 - 4 = 6$

$I = 3$

25. If  $\frac{{}^{n+2}C_6}{{}^{n-2}P_2} = 11$ , then  $n$  satisfies the equation

- (1)  $n^2 + n - 110 = 0$       (2)  $n^2 + 5n - 84 = 0$       (3)  $n^2 + 3n - 108 = 0$       (4)  $n^2 + 2n - 80 = 0$

Ans. (3)

Sol.  $\frac{{}^{n+2}C_6}{{}^{n-2}P_2} = 11 \Rightarrow \frac{(n+2)!}{6!(n-4)!} = 11 \cdot \frac{(n-2)!}{(n-4)!}$

$\Rightarrow (n+2)! = 11 \cdot 6! (n-2)! \cdot 1$

1  $\emptyset$ 1  $(n+2)(n+1)n(n-1) = 11 \cdot 6!$

1  $\emptyset$ 1  $(n+2)(n+1)n(n-1) = 11 \cdot 10 \cdot 9 \cdot 8$

1  $\emptyset$ 1  $n + 2 = 11$

1  $\emptyset$ 1  $n = 9$

Which satisfies the  $n^2 + 3n - 108 = 0$






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26. If the coefficients of  $x^{-2}$  and  $x^{-4}$  in the expansion of  $\left(x^{\frac{1}{3}} + \frac{1}{2x^{\frac{1}{3}}}\right)^{18}$ , ( $x > 0$ ), are  $m$  and  $n$  respectively, then

$\frac{m}{n}$  is equal to

- (1)  $\frac{5}{4}$                       (2)  $\frac{4}{5}$                       (3) 27                      (4) 182

Ans. (4)

Sol.  $T_{r+1} = {}^{18}C_r (x^{1/3})^{18-r} \left(\frac{1}{2x^{1/3}}\right)^r$   
 $= {}^{18}C_r \left(\frac{1}{2}\right)^r x^{\frac{18-2r}{3}}$

For coefficient of  $x^{-2}$ ,  $\frac{18-2r}{3} = -2 \Rightarrow r = 12$

For coefficient of  $x^{-4}$ ,  $\frac{18-2r}{3} = -4 \Rightarrow r = 15 \Rightarrow \frac{m}{n} = \frac{{}^{18}C_{12} \left(\frac{1}{2}\right)^{12}}{{}^{18}C_{15} \left(\frac{1}{2}\right)^{15}}$

$\frac{{}^{18}C_6 (2)^3}{{}^{18}C_3} = 182$

27. If  $A = \begin{bmatrix} -4 & -1 \\ 3 & 1 \end{bmatrix}$ , then the determinant of the matrix  $(A^{2016} - 2A^{2015} - A^{2014})$  is

- (1) 2014                      (2) 2016                      (3) -175                      (4) -25

Ans. (4)

Sol.  $A = \begin{bmatrix} -4 & -1 \\ 3 & 1 \end{bmatrix}$

$A^2 = \begin{bmatrix} -4 & -1 \\ 3 & 1 \end{bmatrix} \begin{bmatrix} -4 & -1 \\ 3 & 1 \end{bmatrix} = \begin{bmatrix} 13 & 3 \\ -9 & -2 \end{bmatrix}$

$A^2 - 2A - I = \begin{bmatrix} 13 & 3 \\ -9 & -2 \end{bmatrix} - \begin{bmatrix} -8 & -2 \\ 6 & 2 \end{bmatrix} - \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 20 & 5 \\ -15 & -5 \end{bmatrix}$

And  $|A| = -1$

$\Rightarrow |A^{2016} - 2A^{2015} - A^{2014}| = |A|^{2014} |A^2 - 2A - I| = 1 \begin{vmatrix} 20 & 5 \\ -15 & -5 \end{vmatrix} = (-100 + 75) = -25$






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28. If  $x$  is a solution of the equation,  $\sqrt{2x+1} - \sqrt{2x-1} = 1$ ,  $\left(x \geq \frac{1}{2}\right)$ , then  $\sqrt{4x^2-1}$  is equal to

- (1) 2                      (2)  $\frac{3}{4}$                       (3)  $2\sqrt{2}$                       (4)  $\frac{1}{2}$

Ans. (2)

Sol.  $\sqrt{2x+1} = 1 + \sqrt{2x-1}$

Squaring on both sides

$$2x + 1 = 1 + 2x - 1 + 2\sqrt{2x-1} + 1$$

$$1 = 2\sqrt{2x-1}$$

$$1 = 4\sqrt{2x-1}$$

$$x = 5/8$$

Now  $\sqrt{4x^2-1}$  at  $x = 5/8$  =  $\sqrt{4 \times \frac{25}{64} - 1} = 3/4$

29. An experiment succeeds twice as often as it fails. The probability of at least 5 successes in the six trials of this experiment is

- (1)  $\frac{192}{729}$                       (2)  $\frac{256}{729}$                       (3)  $\frac{240}{729}$                       (4)  $\frac{496}{729}$

Ans. (2)

Sol. Given  $p = 2q$  & we know that  $p+q = 1$   $\therefore P = 2/3$ ,  $q = 1/3$

The probability of at least 5 successes

$$= {}^6C_5 P^5 q + {}^6C_6 P^6$$

$$= 6 \times \left(\frac{2}{3}\right)^5 \left(\frac{1}{3}\right) + 1 \times \left(\frac{2}{3}\right)^6 = \frac{256}{729}$$

30. The integral  $\int \frac{dx}{(1+\sqrt{x})\sqrt{x-x^2}}$  is equal to (where C is a constant of integration)

- (1)  $-2 \sqrt{\frac{1+\sqrt{x}}{1-\sqrt{x}}} + C$       (2)  $-2 \sqrt{\frac{1-\sqrt{x}}{1+\sqrt{x}}} + C$       (3)  $-\sqrt{\frac{1-\sqrt{x}}{1+\sqrt{x}}} + C$       (4)  $2 \sqrt{\frac{1+\sqrt{x}}{1-\sqrt{x}}} + C$

Ans. (2)






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Sol.  $I = \int \frac{dx}{(1+\sqrt{x})\sqrt{x-x^2}}$

put  $x = \cos^2\theta$

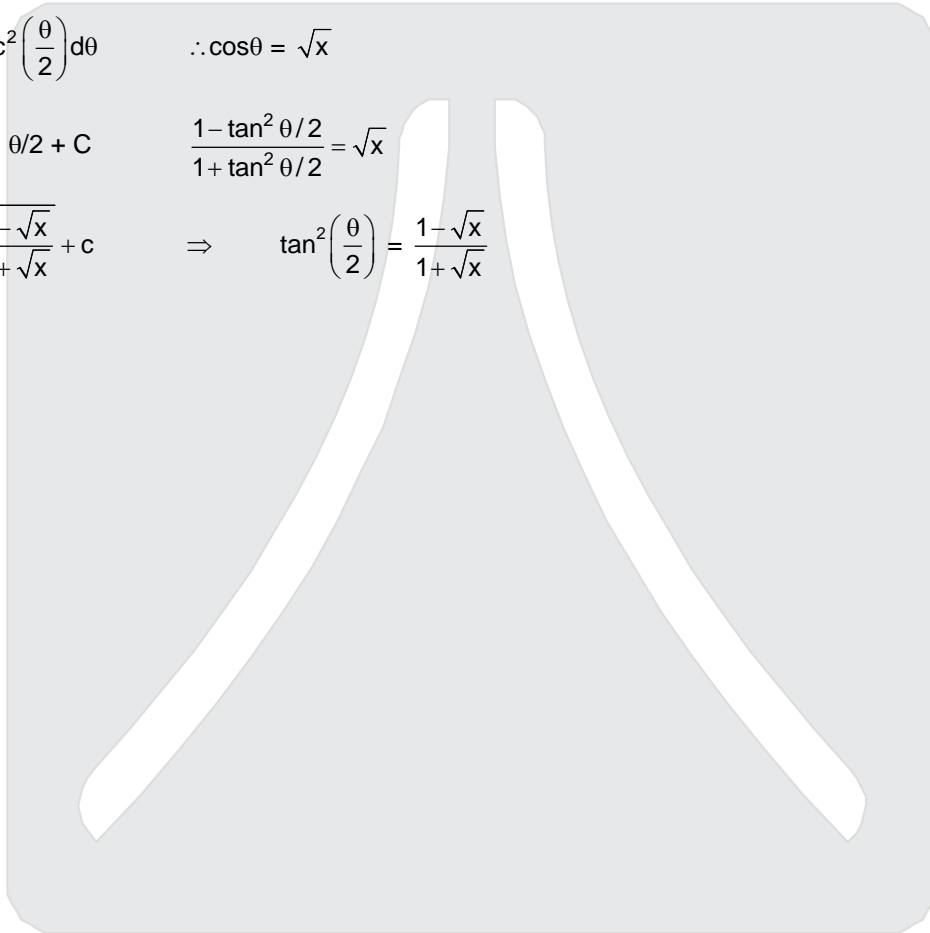
$dx = -2\cos\theta \sin\theta d\theta$

$$I = \int \frac{-2\sin\theta \cos\theta d\theta}{(1+\cos\theta)\cos\theta \sin\theta} = -2 \int \frac{d\theta}{2\cos^2\theta/2}$$

$$= - \int \sec^2\left(\frac{\theta}{2}\right) d\theta \quad \therefore \cos\theta = \sqrt{x}$$

$$= -2 \tan \theta/2 + C \quad \frac{1 - \tan^2 \theta/2}{1 + \tan^2 \theta/2} = \sqrt{x}$$

$$= -2\sqrt{\frac{1-\sqrt{x}}{1+\sqrt{x}}} + c \quad \Rightarrow \quad \tan^2\left(\frac{\theta}{2}\right) = \frac{1-\sqrt{x}}{1+\sqrt{x}}$$








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