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JEE MAIN 2015

ONLINE EXAMINATION

DATE : 11-04-2015

TEST PAPER

WITH SOLUTIONS & ANSWER KEY



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Announces

CRASH COURSE (CC) of 5 WEEKS

VIVEK

Short-term Classroom Contact Program (SCCP)

Target: JEE (Advanced) 2015

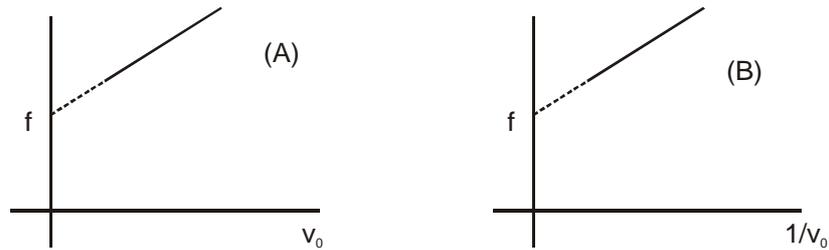


Target	Duration	Commencement Date/(Day)	End Date/(Day)
JEE (Advanced) 2015	05 Weeks*	13.04.2015 (Monday)	17.05.2015 (Sunday)

*Approximate Duration

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3. A source of sound emits sound waves at frequency f_0 . It is moving towards an observer with fixed speed v_s ($v_s < v$, where v is the speed of sound in air). If the observer were to move towards the source with speed v_o , one of the following two graphs (A and B) will give the correct variation of the frequency f heard by the observer as v_o is changed.



The variation of f with v_o is given correctly by :

- (1) graph A with slope = $\frac{f_0}{(v + v_s)}$ (2) graph B with slope = $\frac{f_0}{(v - v_s)}$
 (3) graph A with slope = $\frac{f_0}{(v - v_s)}$ (4) graph B with slope = $\frac{f_0}{(v + v_s)}$

Ans. (3)



Sol.

$$f = \frac{v + v_o}{v - v_s} f_0$$

$$f = \left(\frac{f_0}{v - v_s} \right) v_o + \frac{v f_0}{v - v_s}$$

$$\text{slope} = \frac{f_0}{v - v_s}$$

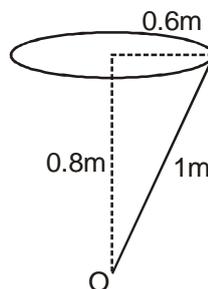
option (3)

4. A particle of mass 2 kg is on a smooth horizontal table and moves in a circular path of radius 0.6 m. The height of the table from the ground is 0.8 m. If the angular speed of the particle is 12 rad s^{-1} , the magnitude of its angular momentum about a point on the ground right under the centre of the circle is :

- (1) $14.4 \text{ kg m}^2\text{s}^{-1}$ (2) $8.64 \text{ kg m}^2\text{s}^{-1}$ (3) $20.16 \text{ kg m}^2\text{s}^{-1}$ (4) $11.52 \text{ kg m}^2\text{s}^{-1}$

Ans. (1)

Sol. $L_0 = mvr \sin 90^\circ$



$$\begin{aligned} &= m(0.6\omega)r \\ &= 2 \times 0.6 \times 12 \times 1 \\ &= 14.4 \text{ kgm}^2/\text{s} \end{aligned}$$



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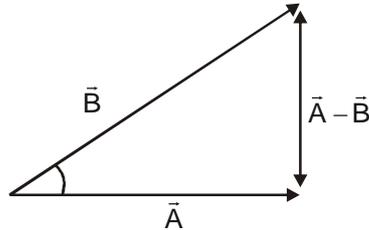
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5. A vector \vec{A} is rotated by a small angle $\Delta\theta$ radians ($\Delta\theta \ll 1$) to get a new vector \vec{B} . In that case $|\vec{B} - \vec{A}|$ is :

- (1) $|\vec{A}| \Delta\theta$ (2) $|\vec{B}| \Delta\theta - |\vec{A}|$ (3) $|\vec{A}| \left(1 - \frac{\Delta\theta^2}{2}\right)$ (4) 0

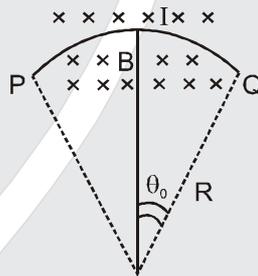
Ans. (1)

Sol. Arc length = Radius \times Angle



$$|\vec{B} - \vec{A}| = |\vec{A}| \Delta\theta$$

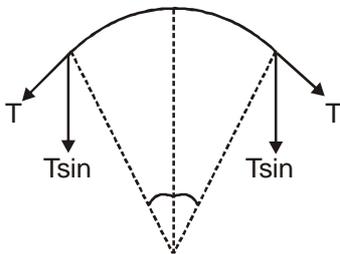
6. A wire carrying current I is tied between points P and Q and is in the shape of a circular arch of radius R due to a uniform magnetic field B (perpendicular to the plane of the paper, shown by xxx) in the vicinity of the wire. If the wire subtends an angle $2\theta_0$ at the centre of the circle (of which it forms an arch) then the tension in the wire is :



- (1) $\frac{IBR}{2\sin\theta_0}$ (2) $\frac{IBR\theta_0}{\sin\theta_0}$ (3) IBR (4) $\frac{IBR}{\sin\theta_0}$

Ans. (3)

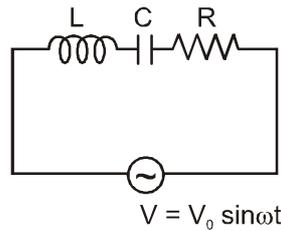
Sol. For small arc length $2T \sin \theta = BIR 2\theta$
 $T = BIR$



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7. For the LCR circuit, shown here, the current is observed to be in phase with the applied voltage. An additional capacitor C' , when joined with the capacitor C present in the circuit, makes the power factor of the circuit unity. The capacitor C' , must have been connected in :



- (1) series with C and has a magnitude $\frac{C}{(\omega^2 LC - 1)}$ (2) series with C and has a magnitude $\frac{1 - \omega^2 LC}{\omega^2 L}$
 (3) parallel with C and has a magnitude $\frac{1 - \omega^2 LC}{\omega^2 L}$ (4) parallel with C and has a magnitude $\frac{C}{(\omega^2 LC - 1)}$

Ans. (3)

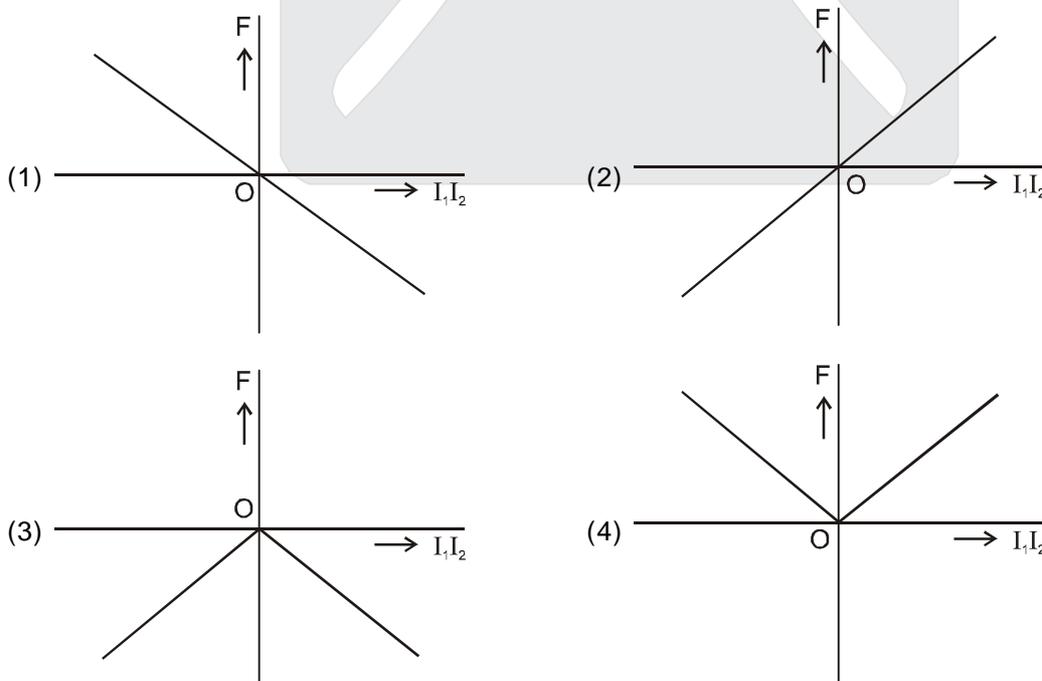
Sol. $\cos\phi = \frac{R}{\sqrt{R^2 + \left[\omega L - \frac{1}{\omega(C+C')}\right]^2}} = 1$

$$\omega L = \frac{1}{\omega(C+C')}$$

$$C' = \frac{1 - \omega^2 LC}{\omega^2 L}$$

option (3)

8. Two long straight parallel wires, carrying (adjustable) current I_1 and I_2 , are kept at a distance d apart. If the force ' F ' between the two wires is taken as 'positive' when the wires repel each other and 'negative' when the wires attract each other, the graph showing the dependence of ' F ', on the product $I_1 I_2$, would be :



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Ans. (1)

Sol.  $I_1 I_2 = \text{Positive}$
(attract) $F = \text{Negative}$

 $I_1 I_2 = \text{Negative}$
(repel) $F = \text{Positive}$

Option (1)

9. A pendulum with time period of 1s is losing energy due to damping. At certain time its energy is 45 J. If after completing 15 oscillations, its energy has become 15 J, its damping constant (in s^{-1}) is :

- (1) $\frac{1}{2}$ (2) $\frac{1}{30} \ln 3$ (3) 2 (4) $\frac{1}{15} \ln 3$

Ans. (4)

Sol. $A = A_0 e^{-\frac{bt}{2m}}$

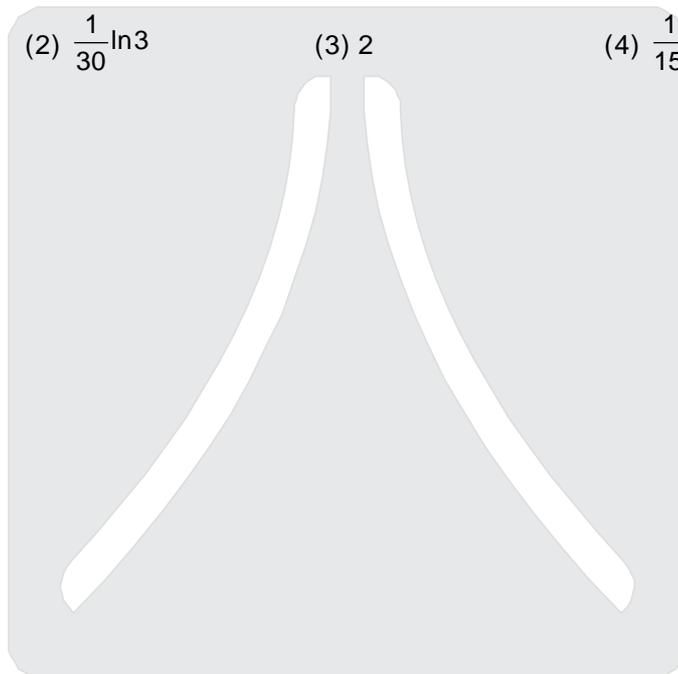
$$E = \frac{1}{2} K A_0^2 e^{-\frac{bt}{m}}$$

$$15 = 45 e^{-\frac{b15}{m}}$$

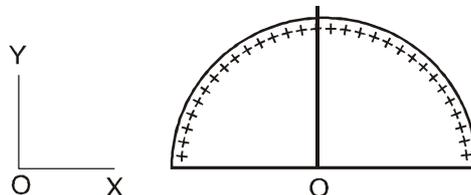
$$\frac{1}{3} = e^{-\frac{b15}{m}}$$

$$\frac{b}{m} = \frac{1}{15} \ln 3$$

Option (4)



10. A wire, of length L ($=20$ cm), is bent into a semicircular arc. If the two equal halves, of the arc, were each to be uniformly charged with charges $\pm Q$, [$|Q| = 10^3 \epsilon_0$. Coulomb where ϵ_0 is the permittivity (in SI units) of free space] the net electric field at the centre O of the semicircular arc would be :



- (1) $(50 \times 10^3 \text{N/C}) \hat{j}$ (2) $(50 \times 10^3 \text{N/C}) \hat{i}$ (3) $(25 \times 10^3 \text{N/C}) \hat{j}$ (4) $(25 \times 10^3 \text{N/C}) \hat{i}$



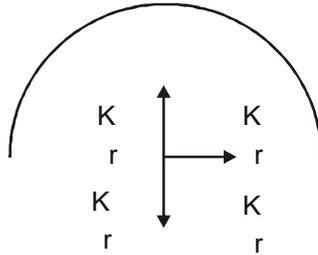
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Ans. (4)

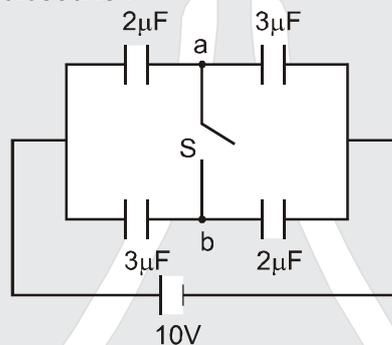
Sol. $E = \frac{2K\lambda}{r}$



$$E = \frac{2K\left(\frac{2Q}{\pi r}\right)}{r} = \frac{4KQ}{\pi r^2} = \frac{4KQ\pi^2}{\pi L^2} = \frac{4\pi KQ}{L^2} = 25 \times 10^3 \text{ N/C } \hat{i}$$

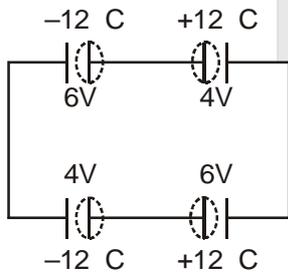
Option (4)

11. In figure is shown a system of four capacitors connected across a 10 V battery. Charge that will flow from switch S when it is closed is :

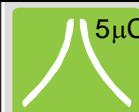
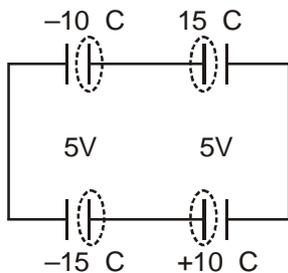


- (1) 5 μC from b to a (2) 20 μC from a to b (3) zero (4) 5 μC from a to b

Ans Sol. (1)



After switch is closed.

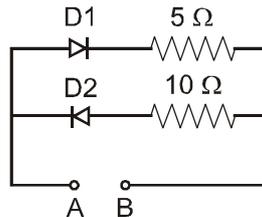


5 μC flows from b to a option (1)

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12. A 2V battery is connected across AB as shown in the figure. The value of the current supplied by the battery when in one case battery's positive terminal is connected to A and in other case when positive terminal of battery is connected to B will respectively be :



- (1) 0.4 A and 0.2 A (2) 0.2 A and 0.4 A (3) 0.1 A and 0.2 A (4) 0.2 A and 0.1 A

Ans. (1)

Sol. When positive terminal connected to A then D1 is forward biased

$$I = \frac{2}{5} = 0.4A$$

When positive terminal connected to B then D2 is forward biased

$$I = \frac{2}{10} = 0.2A$$

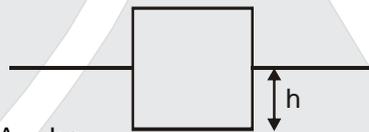
Option (1)

13. A cylindrical block of wood (density = 650 kg m⁻³), of base area 30cm² and height 54 cm, floats in a liquid of density 900 kg m⁻³. The block is depressed slightly and then released. The time period of the resulting oscillations of the block would be equal to that of a simple pendulum of length (nearly) :

- (1) 52 cm (2) 65 cm (3) 39 cm (4) 26 cm

Ans. (3)

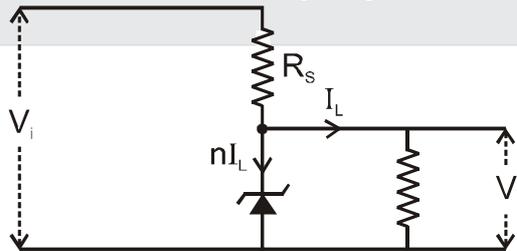
Sol. $mg = F_B$
 $h =$ Length of block immersed in water



$$650 \times A \times 54 \times 10^{-2}g = 900 \times A \times hg$$

$$h = 0.39m = 39 \text{ cm. Option (3)}$$

14. The value of the resistor, R_s , needed in the dc voltage regulator circuit shown here, equals :



- (1) $\frac{(V_i - V_L)}{(n+1)I_L}$ (2) $\frac{(V_i + V_L)}{(n+1)I_L}$ (3) $\frac{(V_i - V_L)}{nI_L}$ (4) $\frac{(V_i + V_L)}{nI_L}$

Ans. (1)

Sol. Voltage on resistor $R_s = V_i - V_L$
 $(I_L + nI_L) R_s = V_i - V_L$

$$R_s = \frac{V_i - V_L}{(n+1)I_L}$$



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15. If electronic charge e , electron mass m , speed of light in vacuum c and Planck's constant h are taken as fundamental quantities, the permeability, of vacuum μ_0 can be expressed in units of :

(1) $\left(\frac{h}{me^2}\right)$ (2) $\left(\frac{hc}{me^2}\right)$ (3) $\left(\frac{h}{ce^2}\right)$ (4) $\left(\frac{mc^2}{he^2}\right)$

Ans. (3)

Sol. $\mu_0 = ke^a m^b c^c h^d$

$$[MLT^{-2}A^{-2}] = [AT]^a [M]^b [LT^{-1}]^c [ML^2T^{-1}]^d$$

$$= [M^{b+d} L^{c+2d} T^{a-c-d} A^a]$$

Comparing

$$a = -2$$

$$b + d = 1$$

$$c + 2d = 1$$

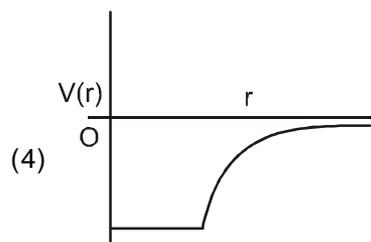
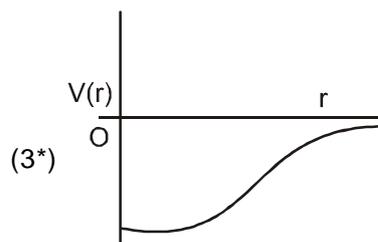
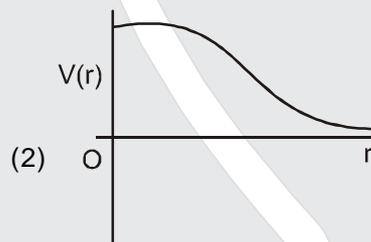
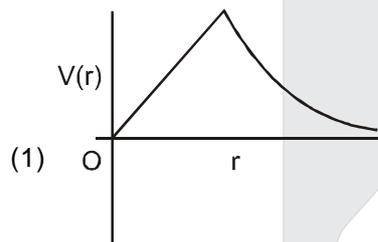
$$a - c - d = -2$$

Solving $a = -2, b = 0, c = -1, d = 1$

$$[\mu_0] = \left[\frac{h}{ce^2}\right]$$

Option (3)

16. Which of the following most closely depicts the correct variation of the gravitation potential $V(r)$ due to a large planet of radius R and uniform mass density ? (figures are not drawn to scale)



Ans. (3)

Sol. $V = -\frac{GM}{2R^3} (3R^2 - r^2)$

Option (3)



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17. In a Young's double slit experiment with light of wavelength λ the separation of slits is d and distance of screen is D such that $D \gg d \gg \lambda$. If the fringe width is β , the distance from point of maximum intensity to the point where intensity falls to half of maximum intensity on either side is:

- (1) $\frac{\beta}{6}$ (2) $\frac{\beta}{3}$ (3) $\frac{\beta}{4}$ (4) $\frac{\beta}{2}$

Ans. (3)

Sol. $2I_0 = 4I_0 \cos^2\left(\frac{\Delta\phi}{2}\right)$

$$\Delta\phi = \frac{\pi}{2}$$

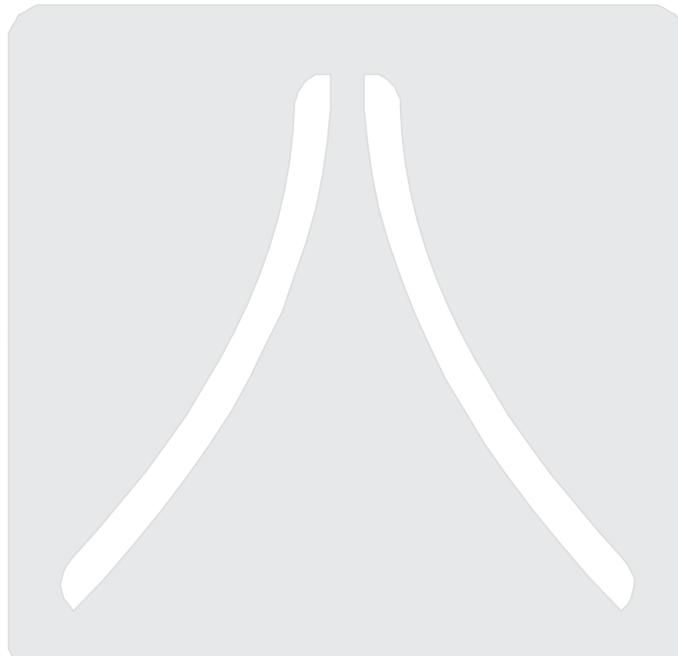
$$\Delta\phi = \frac{2\pi}{\lambda} \Delta x$$

$$\Delta x = \frac{\lambda}{4}$$

$$\frac{dy}{D} = \frac{\lambda}{4} \dots\dots(i)$$

$$\frac{\lambda D}{d} = \beta \dots(ii)$$

Multiply both $y = \frac{\beta}{4}$



18. Let N_β be the number of β particles emitted by 1 gram of N_a^{24} radioactive nuclei (half life = 15 hrs) in 7.5 hours, N_β is close to (Avogadro number = 6.023×10^{23} /g. mole) :

- (1) 6.2×10^{21} (2) 7.5×10^{21} (3) 1.25×10^{22} (4) 1.75×10^{22}

Ans. (2)

Sol. $N_\beta = N_0(1 - e^{-\lambda t})$

$$N_\beta = \frac{6.023 \times 10^{23}}{24} \left[1 - e^{-\frac{\ln 2}{15} \times 7.5} \right]$$

$$N_\beta = 7.4 \times 10^{21}$$

Option (2)

19. A short bar magnet is placed in the magnetic meridian of the earth with north pole pointing north. Neutral points are found at a distance of 30 cm from the magnet on the East - West line, drawn through the middle point of the magnet. The magnetic moment of the magnet in Am^2 is close to :

(Given $\frac{\mu_0}{4\pi} = 10^{-7}$ in SI units and $B_H =$ Horizontal component of earth's magnetic field = 3.6×10^{-5} Tesla)

- (1) 14.6 (2) 19.4 (3) 9.7 (4) 4.9

Ans. (3)

Sol. $\frac{\mu_0}{4\pi} \frac{M}{r^3} = 3.6 \times 10^{-5}$

$$M = \frac{3.6 \times 10^{-5}}{10^{-7}} (0.3)^3$$

$$M = 9.7 \text{ Am}^2$$

20. An experiment takes 10 minutes to raise the temperature of water in a container from 0°C to 100°C and another 55 minutes to convert it totally into steam by a heater supplying heat at a uniform rate. Neglecting the specific heat of the container and taking specific heat of water to be $1 \text{ cal / g } ^\circ\text{C}$, the heat of vapourization according to this experiment will come out to be :

- (1) 560 cal/ g (2) 550 cal / g (3) 540 cal/ g (4) 530 cal/ g

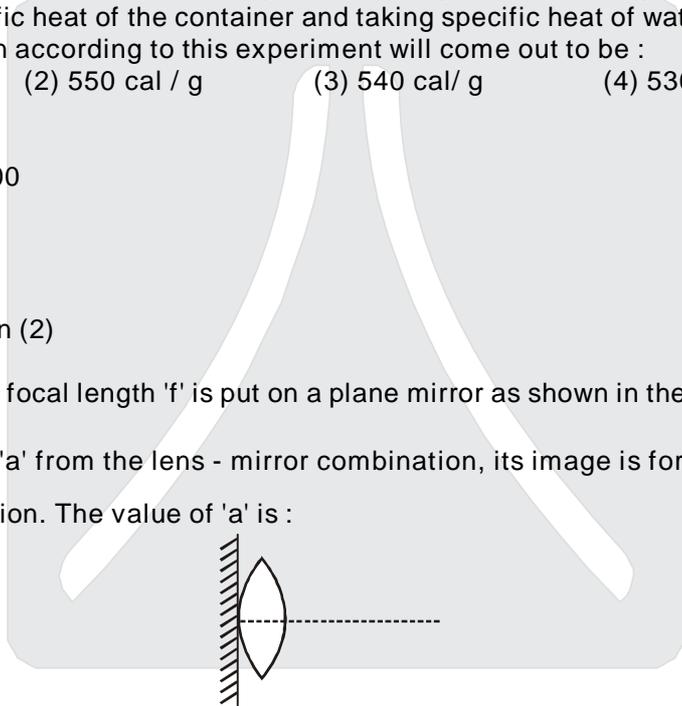
Ans. (2)

Sol. $Pt = mC\Delta T$
 $P \times 10 \times 60 = mC \cdot 100$
 $P \times 55 \times 60 = mL$

$$\frac{10}{55} = \frac{C \times 60}{L}$$

$$L = 550 \text{ cal./g. Option (2)}$$

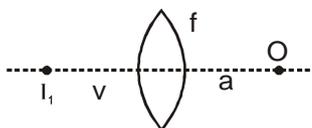
21. A thin convex lens of focal length 'f' is put on a plane mirror as shown in the figure. When an object is kept at a distance 'a' from the lens - mirror combination, its image is formed at a distance $\frac{a}{3}$ in front of the combination. The value of 'a' is :



- (1) $3f$ (2) $\frac{3}{2}f$ (3) f (4) $2f$

Ans. (4)

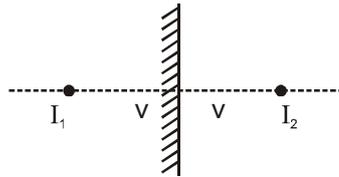
Sol. Lens :



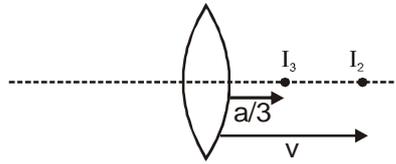
$$\frac{1}{v} - \frac{1}{(-a)} = \frac{1}{f}$$

$$\frac{1}{v} = \frac{1}{f} - \frac{1}{a}$$

Mirror : Forms image at equal distance from mirror



lens :



$$\frac{3}{a} - \frac{1}{v} = \frac{1}{f}$$

$$\frac{3}{a} - \frac{1}{f} + \frac{1}{a} = \frac{1}{f}$$

$$a = 2f$$

Option(4)

22. A beaker contains a fluid of density ρ kg / m³, specific heat S J / kg°C and viscosity η . The beaker is filled upto height h . To estimate the rate of heat transfer per unit area (Q / A) by convection when

beaker is put on a hot plate, a student proposes that it should depend on η , $\left(\frac{S\Delta\theta}{h}\right)$ and $\left(\frac{1}{\rho g}\right)$

when $\Delta\theta$ (in °C) is the difference in the temperature between the bottom and top of the fluid. In that situation the correct option for (Q / A) is :

- (1) $\eta \left(\frac{S\Delta\theta}{h}\right) \left(\frac{1}{\rho g}\right)$ (2) $\left(\frac{S\Delta\theta}{\eta h}\right) \left(\frac{1}{\rho g}\right)$ (3) $\frac{S\Delta\theta}{\eta h}$ (4) $\eta \frac{S\Delta\theta}{h}$

Ans. (4)

Sol. $\frac{\dot{Q}}{A} = \eta^a \left(\frac{S\Delta\theta}{h}\right)^b \left(\frac{1}{\rho g}\right)^c$

$$MT^{-3} = [ML^{-1}T^{-1}]^a [LT^{-2}]^b [M^{-1}L^2T^2]^c$$

$$MT^{-3} = [M^{a-c}L^{-a+b+2c}T^{-a-2b+2c}]$$

Solving

$$\frac{\dot{Q}}{A} = \eta \frac{S\Delta\theta}{h}$$

Option (4)



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23. The AC voltage across a resistance can be measured using a :

- (1) hot wire voltmeter
- (2) moving coil galvanometer
- (3) potential coil galvanometer
- (4) moving magnet galvanometer

Ans. (2)

Sol. A moving coil galvanometer is used to measure AC voltage.

24. Unpolarized light of intensity I_0 is incident on surface of a block of glass at Brewster's angle. In that case, which one of the following statements is true ?

- (1) reflected light is completely polarized with intensity less than $\frac{I_0}{2}$
- (2) transmitted light is completely polarized with intensity less than $\frac{I_0}{2}$
- (3) transmitted light is partially polarized with intensity $\frac{I_0}{2}$
- (4) reflected light is partially polarized with intensity $\frac{I_0}{2}$

Ans. (1)

Sol. When unpolarised light is incident at Brewster's angle then the intensity of the reflected light is less than half of the incident light.

25. An electric field $\vec{E} = (25\hat{i} + 30\hat{j})\text{NC}^{-1}$ exists in a region of space. If the potential at the origin is taken to be zero then the potential at $x = 2\text{ m}$, $y = 2\text{ m}$ is :

- (1) -110 J
- (2) -140 J
- (3) -120 J
- (4) -130 J

Ans. (1)

Sol.
$$\int_0^V dV = - \int_0^{2,2} (25dx + 30dy)$$

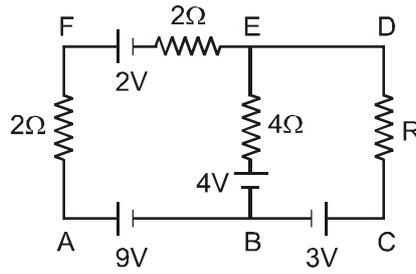
$V = -110\text{ volt.}$



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26. In the electric network shown, when no current flows through the 4Ω resistor in the arm EB, the potential difference between the points A and D will be :



- (1) 6 V (2) 3 V (3) 5 V (4) 4 V

Ans. (3)
Sol. Let

$$\begin{aligned} V_D &= 0V \\ V_E &= 0V \\ V_B &= -4V \\ V_A &= 5V \\ V_A - V_D &= 5V \\ \text{Option (3)} \end{aligned}$$

27. Using equipartition of energy, the specific heat (in $\text{J kg}^{-1} \text{K}^{-1}$) of aluminium at room temperature can be estimated to be (atomic weight of aluminium = 27)

- (1) 410 (2) 25 (3) 1850 (4) 925

Ans. (4)
Sol. Using equipartition of energy

$$\begin{aligned} \frac{6}{2}KT &= mCT \\ C &= \frac{3 \times 1.38 \times 10^{-23} \times 6.02 \times 10^{23}}{27 \times 10^{-3}} \\ &= 925 \text{ J/kgK} \end{aligned}$$

28. A uniform thin rod AB of length L has linear mass density $\mu(x) = a + \frac{bx}{L}$, where x is measured from

A. If the CM of the rod lies at a distance of $\left(\frac{7}{12}\right)L$ from A, then a and b are related as :

- (1) $a = 2b$ (2) $2a = b$ (3) $a = b$ (4) $3a = 2b$

Ans. (2)

Sol.
$$x_{cm} = \frac{\int_0^L (ax + \frac{bx^2}{L}) dx}{\int_0^L (a + \frac{bx}{L}) dx}$$

$$\frac{7L}{12} = \frac{\frac{a}{2} + \frac{b}{3}}{a + \frac{b}{2}}$$

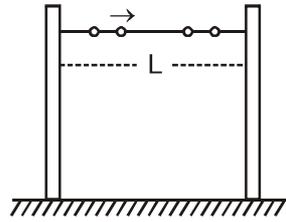
$b = 2a$
Option (2)

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29. A large number (n) of identical beads, each of mass m and radius r are strung on a thin smooth rigid horizontal rod of length L ($L \gg r$) and are at rest at random positions. The rod is mounted between two rigid supports (see figure). If one of the beads is now given a speed v , the average force experienced by each support after a long time is (assume all collisions are elastic) :

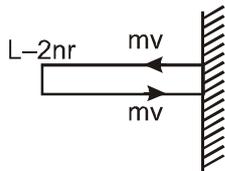


- (1) $\frac{mv^2}{2(L-nr)}$ (2) $\frac{mv^2}{L-2nr}$ (3) $\frac{mv^2}{L-nr}$ (4) zero

Ans. (2)

Sol. Space between the supports for motion of beads is $L - 2nr$

$$F = \frac{2mV}{V} = \frac{mV^2}{L - 2nr}$$



Options (2)

30. The de-Broglie wavelength associated with the electron in the $n = 4$ level is :

(1) $\frac{1}{4}$ th of the de-Broglie wavelength of the electron in the ground state.

(2) four times the de-Broglie wavelength of the electron in the ground state

(3) two times the de-Broglie wavelength of the electron in the ground state

(4) half of the de-Broglie wavelength of the electron in the ground state

Ans. (2)

Sol. De-Broglie wavelength of electron

$$\lambda = \frac{h}{mV} \quad V \propto \frac{1}{n}$$

$$\lambda \propto n$$

$$\lambda_4 = 4\lambda_1$$

\therefore option (2)



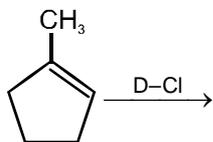
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PART - B : CHEMISTRY

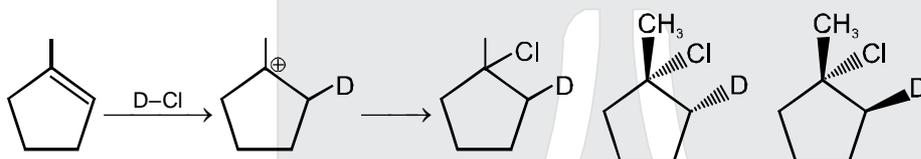
1. What is the major product expected from the following reaction ?



Where D is an isotope of Hydrogen.



Sol.



2. Which physical property of dihydrogen is wrong ?

- (1) Odourless gas (2) Tasteless gas (3) Colourless gas (4*) Non-inflammable gas

Sol. H_2 is highly inflammable.

3. $A + 2B \rightarrow C$, the rate equation for this reaction is given as

$$\text{Rate} = k[A][B]$$

If the concentration of A is kept the same but that of B is doubled what will happen to the rate itself ?

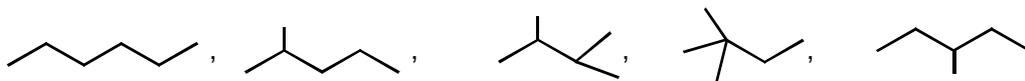
- (1) halved (2) the same (3*) doubled (4) quadrupled

Sol. Rate is first order with respect to B. So it doubles on doubling concentration of B, while keeping concentration of A as same.

4. The number of structural isomers for C_6H_{14} is :

- (1) 4 (2) 3 (3) 6 (4*) 5

Sol.



5. When concentrated HCl is added to an aqueous solution of $CoCl_2$, its colour changes from reddish pink to deep blue. Which complex ion gives blue colour in this reaction ?

- (1*) $[CoCl_4]^{2-}$ (2) $[CoCl_6]^{3-}$ (3) $[CoCl_6]^{4-}$ (4) $[Co(H_2O)_6]^{2+}$

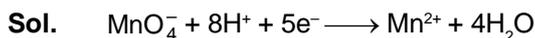
Sol. $[CoCl_4]^{2-}$ is formed which is blue in colour.



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$$E = 1.51 - \frac{0.059}{5} \log \frac{[\text{Mn}^{2+}]}{[\text{MnO}_4^-][\text{H}^+]^8}$$

Taking Mn^{2+} and MnO_4^- in standard state i.e. 1 M,

$$E = 1.51 - \frac{0.059}{5} \times 8 \log \frac{1}{[\text{H}^+]^8}$$

$$= 1.51 - \frac{0.059}{5} \times 8 \times 3 = 1.2268 \text{ V}$$

Hence at this pH, MnO_4^- will oxidise only Br^- and I^- as SRP of Cl_2/Cl^- is 1.36 V which is greater than that for $\text{MnO}_4^-/\text{Mn}^{2+}$.

Ans. is (2).

13. Calamine is an ore of :

(1*) Zinc

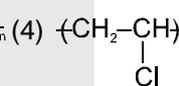
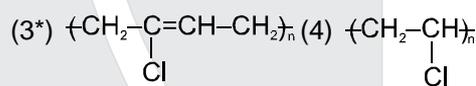
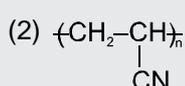
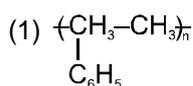
(2) Aluminium

(3) Iron

(4) Copper

Sol. $\text{ZnCO}_3 = \text{calamine}$.

14. Which one of the following structures represents the neoprene polymer ?



Sol. $\left\langle \text{CH}_2-\underset{\text{Cl}}{\text{C}=\text{CH}-\text{CH}_2 \right\rangle_n$ is neoprene polymer.

15. When does a gas deviate the most from its ideal behaviour ?

(1) At low pressure and low temperature

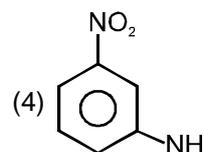
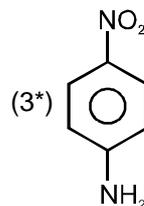
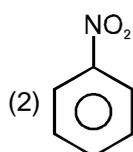
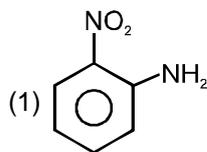
(2) At low pressure and high temperature

(3*) At high pressure and low temperature

(4) At high pressure and high temperature

Sol. At high pressure and low temperature, size of molecules and inter molecular forces cannot be neglected.

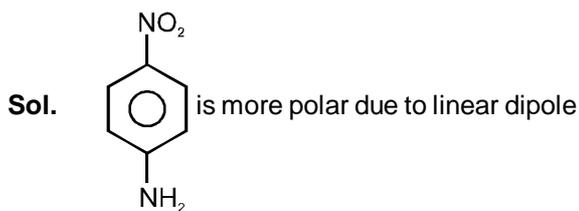
16. Which compound exhibits maximum dipole moment among the following ?



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17. Addition of phosphate fertilisers to water bodies causes :
- (1) increase in amount of dissolved oxygen in water
 - (2) deposition of calcium phosphate
 - (3) increase in fish population
 - (4*) enhanced growth of algae

Sol.

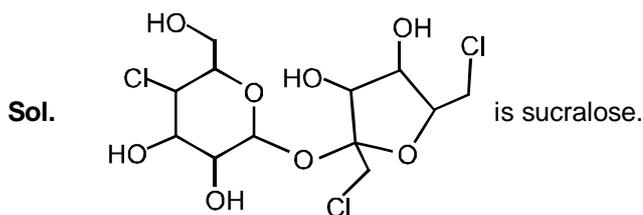
18. At temperature T, the average kinetic energy of any particle is $\frac{3}{2}KT$. The de Broglie wavelength follows the order :
- (1) Visible photon > Thermal neutron > Thermal electron
 - (2) Thermal proton > Thermal electron > Visible photon
 - (3) Thermal proton > Visible photon > Thermal electron
 - (4*) Visible photon > Thermal electron > Thermal neutron

Sol. De-broglie wavelength (for particles) = $\frac{h}{\sqrt{2m KE}}$

As temperature is same, KE is same. So, $\lambda \propto \frac{1}{\sqrt{m}}$.

Hence $\lambda_{db}(\text{electron}) > \lambda_{db}(\text{neutron})$

19. Which artificial sweetener contains chlorine ?
- (1*) Sucralose
 - (2) Alitame
 - (3) Aspartame
 - (4) Saccharin



20. For the equilibrium, $A(g) \rightleftharpoons B(g)$, ΔH is -40 kJ/mol. If the ratio of the activation energies of the forward (E_f) and reverse (E_b) reactions is $\frac{2}{3}$ then :
- (1*) $E_f = 80$ kJ/mol; $E_b = 120$ kJ/mol
 - (2) $E_f = 60$ kJ/mol; $E_b = 100$ kJ/mol
 - (3) $E_f = 30$ kJ/mol; $E_b = 70$ kJ/mol
 - (4) $E_f = 70$ kJ/mol; $E_b = 30$ kJ/mol



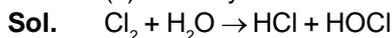
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Sol. $\Delta H = E_{af} - E_{ab}$
 $\Rightarrow -40 = 2x - 3x$
 $\Rightarrow E_{af} = 80 \text{ kJ/mol}$
 $E_{ab} = 120 \text{ kJ/mol}$

21. Chlorine water on standing loses its colour and forms :
 (1) HCl only (2) HCl and HClO₂ (3*) HCl and HOCl (4) HOCl and HOCl₂



22. Determination of the molar mass of acetic acid in benzene using freezing point depression is affected by :
 (1) partial ionization (2) dissociation (3) complex formation (4*) association

Sol. Benzene is non-polar solvent.

23. $\text{A} + 3\text{B} + 3\text{C} \rightleftharpoons \text{AB}_2\text{C}_3$
 Reaction of 6.0 g of A, 6.0×10^{23} atoms of B, and 0.036 mol of C yields 4.8 g of compound AB₂C₃. If the atomic mass of A and C are 60 and 80 amu, respectively, the atomic mass of B is (Avogadro no. = 6×10^{23}):
 (1*) 50 amu (2) 60 amu (3) 70 amu (4) 40 amu

Sol. $n_A = 0.1$, $n_B = 1$, $n_C = 0.036$
 Limiting reagent = C

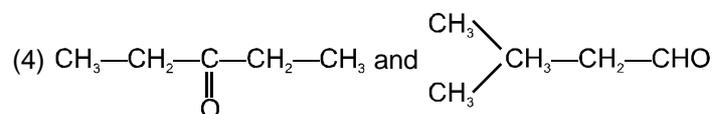
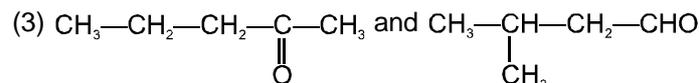
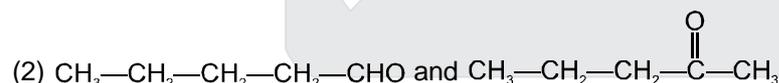
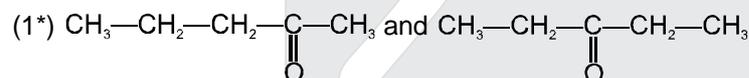
$$\Rightarrow n_{\text{AB}_2\text{C}_3} \text{ formed} = \frac{0.036}{3} = 0.012$$

$$\Rightarrow \text{MM}_{(\text{AB}_2\text{C}_3)} \frac{4.8}{0.012} = 400$$

$$\Rightarrow 60 + 2x + 80 \times 3 = 400$$

$$x = 50$$

24. Which of the following pairs of compounds are positional isomers ?



Sol. Pentane-2-one and pentan-3-one are positional isomers.



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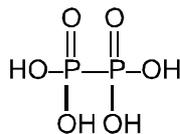
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25. Which of the following compound has a P–P bond ?

- (1) $H_4P_2O_5$ (2) $(HPO_3)_3$ (3*) $H_4P_2O_6$ (4) $H_4P_2O_7$

Sol. $H_4P_2O_6$ has P–P linkage



26. Choose the incorrect formula out of the four compounds for an element X below :

- (1) X_2O_3 (2*) X_2Cl_3 (3) $X_2(SO_4)_3$ (4) XPO_4

Sol. 1,3 and 4 suggests that valency of X is +3.

So, formula of chloride is XCl_3 .

27. Molecular AB has a bond length of 1.61 \AA and a dipole moment of 0.38 D. The fractional charge on each atom (absolute magnitude) is : ($e_0 = 4.802 \times 10^{-10} \text{ esu}$)

- (1) 0.5 (2*) 0.05 (3) 0 (4) 1.0

Sol. $1D = 10^{-18} \text{ esu cm}$

$$\delta = \frac{0.38 \times 10^{-18}}{1.617 \times 10^{-8} \times 4.8 \times 10^{-10}}$$

$$= 0.0485 \approx 0.05$$

28. Which of the following statements is false ?

- (1*) $Na_2Cr_2O_7$ is less soluble than $K_2Cr_2O_7$ (2) $Na_2Cr_2O_7$ is primary standard in volumetry
(3) CrO_4^{2-} is tetrahedral in shape (4) CrO_7^{2-} has a Cr–O–Cr bond

Sol. $Na_2C_2O_7$ is more soluble than $K_2Cr_2O_7$.

29. In the reaction sequence



- (1) $CH_3-CH_2-CH_2-CH_2-OH$ (2*) $CH_3-CH=CH-CHO$

- (3) $CH_3-CH_2-CH_2-CH_3$ (4) $CH_3-\overset{\text{O}}{\parallel}{C}-CH_2$

Sol. It is aldol condensation reaction.

30. A pink coloured salt turns blue on heating. The presence of which cation is most likely ?

- (1*) Co^{2+} (2) Cu^{2+} (3) Zn^{2+} (4) Fe^{2+}

Sol. Zn^{2+} salts are white usually Fe^{2+} salts are rarely pink. Cu^{2+} salts are usually blue in hydrated form. Co^{2+} is pink in aqueous solution.



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PART - C : MATHEMATICS

1. The term independent of x in the binomial expansion of $\left(1 - \frac{1}{x} + 3x^5\right)\left(2x^2 - \frac{1}{x}\right)^8$ is :

- (1) 496 (2) - 496 (3*) 400 (4) -400

Ans. (3)

Sol. $\left(1 - \frac{1}{x} + 3x^5\right) \cdot {}^8C_r (2x^2)^{8-r} \left(-\frac{1}{x}\right)^r$

$$= {}^8C_r (2x^2)^{8-r} \left(-\frac{1}{x}\right)^r - \frac{1}{x} {}^8C_r (2x^2)^{8-r} \left(-\frac{1}{x}\right)^r + 3x^5 {}^8C_r (2x^2)^{8-r} \left(-\frac{1}{x}\right)^r$$

$$= {}^8C_r 2^{8-r} (-1)^r x^{16-3r} - {}^8C_r 2^{8-r} (-1)^r x^{15-3r} + 3 {}^8C_r 2^{8-r} \left(-\frac{1}{x}\right)^r (-1)^r x^{21-3r}$$

for independent term

$$16-3r = 0, 15-3r = 0, 21-3r = 0$$

$$r = 5, \quad r = 7 \text{ in III term}$$

in II term

$$-{}^8C_5 (2^3) (-1) - 3 \cdot {}^8C_7 \cdot 2$$

$$= 448 - 6 \times 8 = 448 - 48 = 400$$

2. Let k be a non-zero real number. If $f(x) = \begin{cases} \frac{(e^x - 1)^2}{x}, & x \neq 0 \\ \sin\left(\frac{x}{k}\right) \log\left(1 + \frac{x}{4}\right), & x \neq 0 \\ 12, & x = 0 \end{cases}$ is a continuous function, then the

value of k is :

- (1) 4 (2) 1 (3*) 3 (4) 2

Ans. (3)

Sol. $\lim_{x \rightarrow 0} \frac{x^2 \left(\frac{e^x - 1}{x}\right)^2 4k}{\frac{\sin \frac{x}{k}}{\frac{x}{k}} \cdot \frac{\log\left(1 + \frac{x}{4}\right)}{\frac{x}{4}}}$

$$\Rightarrow 4k = 12 \Rightarrow k = 3$$

3. If the incentre of an equilateral triangle is $(1, 1)$ and the equation of its one side is $3x + 4y + 3 = 0$, then the equation of the circumcircle of this triangle is :

(1*) $x^2 + y^2 - 2x - 2y - 14 = 0$

(2) $x^2 + y^2 - 2x - 2y - 2 = 0$

(3) $x^2 + y^2 - 2x - 2y + 2 = 0$

(4) $x^2 + y^2 - 2x - 2y - 7 = 0$

Ans. (1)

Sol. Let radius is r

$$\Rightarrow \frac{r}{2} = \frac{10}{5} \Rightarrow r = 4$$

So circle is

$$(x - 1)^2 + (y - 1)^2 = 16$$

$$\Rightarrow x^2 + y^2 - 2x - 2y - 14 = 0$$

4. Let $f: \mathbb{R} \rightarrow \mathbb{R}$ be a function such that $f(2 - x) = f(2 + x)$ and $f(4 - x) = f(4 + x)$, for all $x \in \mathbb{R}$ and $\int_0^2 f(x) dx = 5$.

Then the value of $\int_{10}^{50} f(x) dx$ is :

(1) 125

(2) 80

(3*) 100

(4) 200

Ans. (3)

Sol. Put $x = 2 + x$

$$f(-x) = f(4 + x) = f(4 - x)$$

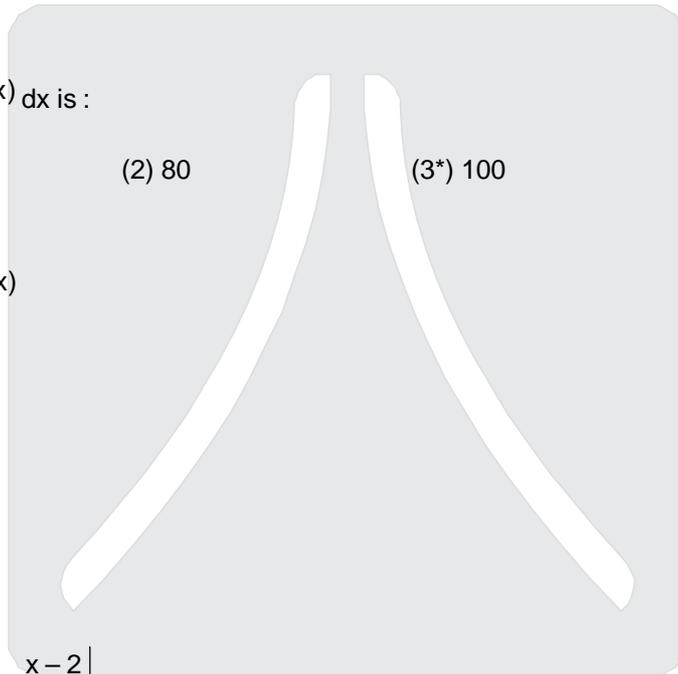
$$\Rightarrow f(x) = f(x + 4)$$

Hence period is 4

$$\int_{10}^{50} f(x) dx = 10 \int_{10}^{14} f(x) dx$$

$$= 10[5 + 5]$$

$$= 100$$



5. If $\begin{vmatrix} x^2 + x & x + 1 & x - 2 \\ 2x^2 + 3x - 1 & 3x & 3x - 3 \\ x^2 + 2x + 3 & 2x - 1 & 2x - 1 \end{vmatrix} = ax - 12$, then 'a' is equal to :

(1*) 24

(2) -12

(3) -24

(4) 12

Ans. (1)

Sol. Put $x = -1$

$$\begin{vmatrix} 0 & 0 & -3 \\ -2 & -3 & 0 \\ 2 & -3 & -3 \end{vmatrix} = -a - 12$$

$$\Rightarrow a = 24$$



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6. Let k and K be the minimum and the maximum values of the function $f(x) = \frac{(1+x)^{0.6}}{1+x^{0.6}}$ in $[0, 1]$ respectively, then the ordered pair (k, K) is equal to :
- (1*) $(2^{-0.4}, 1)$ (2) $(2^{-0.4}, 2^{0.6})$ (3) $(2^{-0.6}, 1)$ (4) $(1, 2^{0.6})$
- Ans. (1)**

Sol. $f(x) = \frac{(1+x)^{3/5}}{1+x^{3/5}}$
and $x \in [0, 1]$

$$\Rightarrow f'(x) = \frac{(1+x^{3/5}) \frac{3}{5}(1+x)^{-2/5} - \frac{3}{5}(1+x)^{3/5}(x^{-2/5})}{(1+x^{3/5})^2}$$

$$= \frac{3}{5} [(1+x^{3/5})(1+x)^{-2/5} - (1+x)^{3/5}x^{-2/5}]$$

$$= \frac{3}{5} \left[\frac{1+x^{3/5}}{(1+x)^{2/5}} - \frac{(1+x)^{3/5}}{x^{2/5}} \right]$$

$$= \frac{x^{2/5} + x - 1 - x}{x^{2/5}(1+x)^{2/5}} < 0$$

$$f(0) = 1 \Rightarrow f(x) \in [2^{-0.4}, 1]$$

$$f(1) = 2^{-0.4}$$

7. If $\cos \alpha + \cos \beta = \frac{3}{2}$ and $\sin \alpha + \sin \beta = \frac{1}{2}$ and θ is the arithmetic mean of α and β , then $\sin 2\theta + \cos 2\theta$ is equal to :
- (1) $\frac{3}{5}$ (2*) $\frac{7}{5}$ (3) $\frac{4}{5}$ (4) $\frac{8}{5}$

Ans. (2)

Sol. $2\cos \frac{\alpha+\beta}{2} \cos \frac{\alpha-\beta}{2} = \frac{3}{2}$

$$\text{and } 2 \sin \frac{\alpha+\beta}{2} \cos \frac{\alpha-\beta}{2} = \frac{1}{2}$$

$$\Rightarrow \tan \left(\frac{\alpha+\beta}{2} \right) = \frac{1}{3}$$

$$\Rightarrow \sin 2\theta + \cos 2\theta = \sin(\alpha + \beta) + \cos(\alpha + \beta)$$

$$= \frac{2}{3} - \frac{1}{9} + \frac{1}{1+\frac{1}{9}}$$

$$= \frac{6}{10} + \frac{8}{10} = \frac{7}{5}$$



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8. Let PQ be a double ordinate of the parabola, $y^2 = -4x$, where P lies in the second quadrant. If R divides PQ in the ratio 2 : 1 then the locus of R is :

- (1) $3y^2 = -2x$ (2) $3y^2 = 2x$ (3) $9y^2 = 4x$ (4*) $9y^2 = -4x$

Ans. (4)

Sol. Let $P(-at_1^2, 2at_1)$, $Q(-at_1^2, -2at_1)$, $R(h, k)$

$$\Rightarrow h = -at_1^2, k = \frac{-2at_1}{3}$$

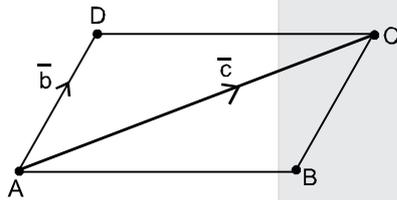
$$\Rightarrow 9k^2 = -4h \Rightarrow 9y^2 = -4x$$

9. In a parallelogram ABCD, $|\vec{AB}| = a$, $|\vec{AD}| = b$ and $|\vec{AC}| = c$, then $\vec{DA} \cdot \vec{AB}$ has the value :

- (1) $\frac{1}{2}(a^2 + b^2 + c^2)$ (2) $\frac{1}{2}(a^2 - b^2 + c^2)$ (3) $\frac{1}{4}(a^2 + b^2 - c^2)$ (4) $\frac{1}{3}(b^2 + c^2 - a^2)$

Ans. (1)

Sol.



$$|\vec{AB}| = a$$

$$|\vec{AD}| = b$$

$$|\vec{AC}| = c$$

$$\therefore \vec{AB} + \vec{BC} + \vec{AC}$$

$$\vec{AB} + \vec{AD} = \vec{AC}$$

$$|\vec{AB}|^2 + |\vec{AD}|^2 + 2\vec{AB} \cdot \vec{AD} = |\vec{AC}|^2$$

$$\Rightarrow a^2 + b^2 + 2\vec{AB} \cdot (\vec{AB} + \vec{BD}) = c^2$$

$$\Rightarrow a^2 + b^2 + 2a^2 + 2\vec{AB} \cdot \vec{BD} = c^2$$

$$\Rightarrow 3a^2 + b^2 - c^2 = +2\vec{AB} \cdot \vec{DB}$$

$$\Rightarrow \vec{AB} \cdot \vec{DB} = \frac{1}{2}(3a^2 + b^2 - c^2)$$



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10. If the two roots of the equation, $(a - 1)(x^4 + x^2 + 1) + (a + 1)(x^2 + x + 1)^2 = 0$ are real and distinct, then the set of all values of 'a' is :

(1) $\left(0, \frac{1}{2}\right)$ (2*) $\left(-\frac{1}{2}, 0\right) \cup \left(0, \frac{1}{2}\right)$ (3) $\left(-\frac{1}{2}, 0\right)$ (4) $(-\infty, -2) \cup (2, \infty)$

Ans. (2)

Sol. Equation becomes

$$(a - 1)(x^2 - x + 1) + (a + 1)(x^2 + x + 1) = 0$$

$$ax^2 + x + a = 0$$

for roots to be distinct and real

$$a \neq 0 \text{ and } 1 - 4a^2 > 0$$

$$\Rightarrow a \in \left(-\frac{1}{2}, 0\right) \cup \left(0, \frac{1}{2}\right)$$

11. The solution of the differential equation $ydx - (x + 2y^2)dy = 0$ is $x = f(y)$. If $f(-1) = 1$, then $f(1)$ is equal to :

(1) 4 (2*) 3 (3) 1 (4) 2

Ans. (2)

Sol. $\frac{ydx - xdy}{y^2} = 2dy$

$$d\left(\frac{x}{y}\right) = 2dy$$

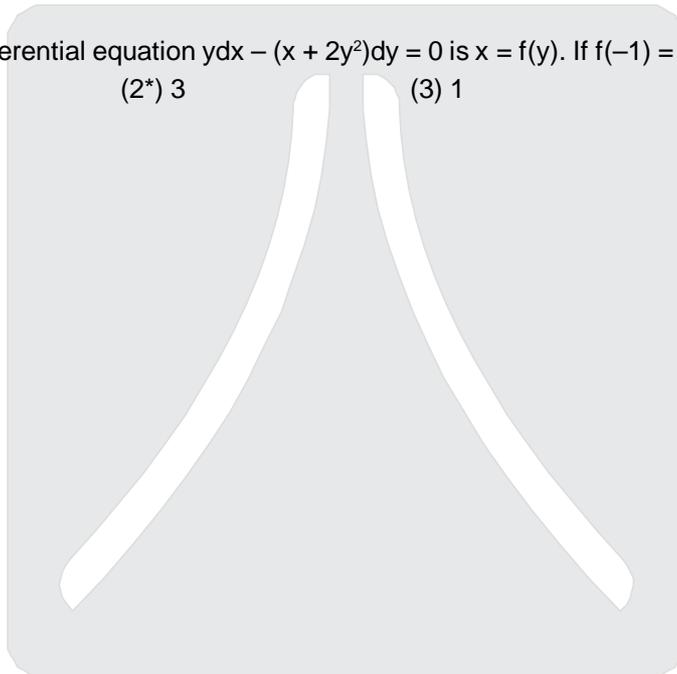
$$\frac{x}{y} = 2y + c$$

$$\Rightarrow c = 1$$

$$\Rightarrow \frac{x}{y} = 2y + 1$$

$$\text{put } y = 1$$

$$f(1) = 3$$

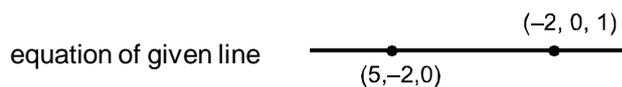


12. The shortest distance between the z-axis and the line $x + y + 2z - 3 = 0 = 2x + 3y + 4z - 4$, is :

(1) 1 (2*) 2 (3) 4 (4) 3

Ans. (2)

Sol. Equation of z-axis $\frac{x}{0} = \frac{y}{0} = \frac{z}{1}$



$$\text{S.D.} = \left| \frac{(5i - 2i) \cdot 2j}{2} \right| = 2$$

Ans. (3)

Sol. $\tan 60^\circ = \frac{m - (-\sqrt{3})}{1 + (-\sqrt{3}m)}$

$\Rightarrow m = 0, m = \sqrt{3}$

line $y + 2 = \sqrt{3}(x - 3)$

$y - \sqrt{3}x + 2 + 3\sqrt{3} = 0$

22. If z is a non-real complex number, then the minimum value of $\frac{\text{Im } z^5}{(\text{Im } z)^5}$ is :

(1) -1

(2*) -4

(3) -2

(4) -5

Ans. (2)

Sol. Let $z = re^{i\theta}$

$$\frac{\text{Im } z^5}{(\text{Im } z)^5} = \frac{r^5(\sin 5\theta)}{r^5(\sin \theta)^5}$$

$$= \frac{\sin 5\theta}{\sin^5 \theta}$$

$$= \frac{16\sin^5 \theta - 20\sin^3 \theta + 5\sin \theta}{\sin^5 \theta}$$

$$= 5 \operatorname{cosec}^4 \theta - 20 \operatorname{cosec}^2 \theta + 16$$

minimum value of $\frac{\text{Im } z^5}{(\text{Im } z)^5}$ is -4

23. Let 10 vertical poles standing at equal distances on a straight line, subtend the same angle of elevation at a point O on this line and all the poles are on the same side of O. If the height of the longest pole is 'h' and the distance of the foot of the smallest pole from O is 'a'; then the distance between two consecutive poles, is :

(1*) $\frac{h \cos \alpha - a \sin \alpha}{9 \sin \alpha}$

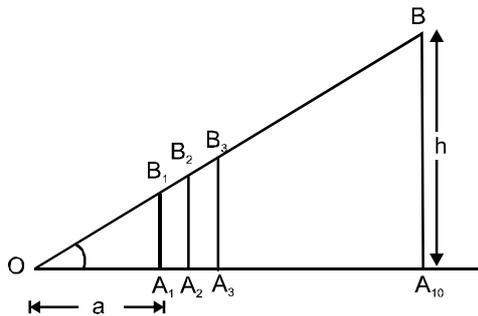
(2) $\frac{h \sin \alpha + a \cos \alpha}{9 \sin \alpha}$

(3) $\frac{h \cos \alpha - a \sin \alpha}{9 \cos \alpha}$

(4) $\frac{h \sin \alpha - a \cos \alpha}{9 \cos \alpha}$

Ans. (1)

Sol.



$\Delta OA_1 B_1, \Delta OA_2 B_2, \Delta OA_3 B_3, \dots, \Delta OA_{10} B_{10}$ are similar.



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$$\Rightarrow \frac{h_1}{a_1} = \frac{h_2}{a_2} = \frac{h_3}{a_3} = \dots = \frac{h_{10}}{a_{10}} = \tan \alpha.$$

$$\therefore h_{10} = h = a_{10} \tan \alpha \quad \dots (1)$$

$$\text{and } a_1 = a \Rightarrow h_1 = a \tan \alpha \quad \dots (2)$$

$$\Rightarrow h = (a + 9d) \tan \alpha \text{ where } d \text{ is distance between poles}$$

$$\Rightarrow h = a \tan \alpha + 9d \tan \alpha$$

$$\Rightarrow \frac{h - a \tan \alpha}{9 \tan \alpha} = d$$

$$\Rightarrow d = \frac{h \cos \alpha - a \sin \alpha}{9 \sin \alpha}$$

24. If the distance between the foci of an ellipse is half the length of its latus rectum, then the eccentricity of the ellipse is :

(1) $\frac{2\sqrt{2}-1}{2}$

(2*) $\sqrt{2} - 1$

(3) $\frac{1}{2}$

(4) $\frac{\sqrt{2}-1}{2}$

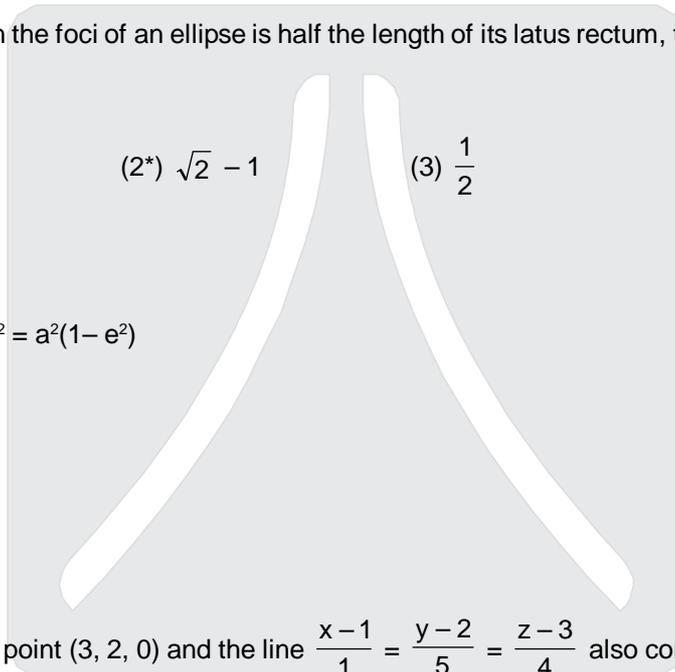
Ans. (2)

Sol. $2ae = \frac{b^2}{a} \Rightarrow 2a^2e = b^2 = a^2(1 - e^2)$

$$\Rightarrow 2e = 1 - e^2$$

$$\Rightarrow (e + 1)^2 = 2$$

$$\Rightarrow e = \sqrt{2} - 1$$



25. A plane containing the point (3, 2, 0) and the line $\frac{x-1}{1} = \frac{y-2}{5} = \frac{z-3}{4}$ also contains the point :

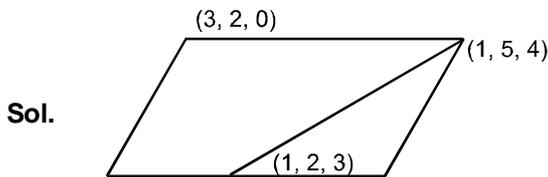
(1) (0, 3, 1)

(2) (0, 7, -10)

(3) (0, -3, 1)

(4*) (0, 7, 10)

Ans. (4)



equation of plane

$$15x - 11y + 10z = 23$$

26. If $\sum_{n=1}^5 \frac{1}{n(n+1)(n+2)(n+3)} = \frac{k}{3}$, then k is equal to :

(1) $\frac{1}{6}$

(2) $\frac{17}{105}$

(3*) $\frac{55}{336}$

(4) $\frac{19}{112}$

Ans. (3)

Sol. $T_r = \frac{1}{3} \left[\frac{1}{n(n+1)(n+2)} - \frac{1}{(n+1)(n+2)(n+3)} \right]$

$$\sum_{r=1}^5 T_r = \frac{1}{3} \left[\frac{1}{6} - \frac{1}{6.7.8} \right] = \frac{k}{3}$$

$$k = \frac{55}{336}$$

27. If the mean and the variance of a binomial variate X are 2 and 1 respectively, then the probability that X takes a value greater than or equal to one is :

(1) $\frac{9}{16}$

(2) $\frac{3}{4}$

(3) $\frac{1}{16}$

(4*) $\frac{15}{16}$

Ans. (4)

Sol. mean = np = 2
variance npq = 1
by (2) and (1)

$$q = \frac{1}{2}$$

$$p = \frac{1}{2}$$

$$\Rightarrow n = 4$$

$$P(x \geq 1) = {}^4C_1 p^1 q^3 + {}^4C_2 p^2 q^2 + {}^4C_3 p^3 q + {}^4C_4 p^4$$

$$= 1 - {}^4C_0 p^0 q^4$$

$$= 1 - \left(\frac{1}{2}\right)^4 = \frac{15}{16}$$

28. If A is a 3 × 3 matrix such that |5.adjA| = 5, then |A| is equal to :

(1*) $\pm \frac{1}{5}$

(2) $\pm \frac{1}{25}$

(3) ± 1

(4) ± 5

Ans. (1)

Sol. $125 |A|^2 = 5$

$$|A| = \pm \frac{1}{5}$$



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29. The equation of a normal to the curve, $\sin y = x \sin \left(\frac{\pi}{3} + y \right)$ at $x = 0$, is :

(1) $2x - \sqrt{3}y = 0$

(2*) $2x + \sqrt{3}y = 0$

(3) $2y - \sqrt{3}x = 0$

(4) $2y + \sqrt{3}x = 0$

Ans. (2)

Sol. $\therefore \sin y = x \sin \left(\frac{\pi}{3} + y \right)$

at $x = 0, y = 0$

diff with respect to x

$$\Rightarrow \cos y \frac{dy}{dx} = \sin \left(\frac{\pi}{3} + y \right) + x \cos \left(\frac{\pi}{3} + y \right) \frac{dy}{dx}$$

$$\text{at } (0, 0) \frac{dy}{dx} = \frac{\sqrt{3}}{2}$$

$$\Rightarrow \text{Equation of normal is } y - 0 = -\frac{2}{\sqrt{3}}(x - 0)$$

$$\Rightarrow 2x + \sqrt{3}y = 0$$

30. Consider the following statements :

P : Suman is brilliant

Q : Suman is rich.

R : Suman is honest

the negation of the statement

“Suman is brilliant and dishonest if and only if suman is rich” can be equivalently expressed as :

(1) $\sim Q \leftrightarrow \sim P \vee R$

(2) $\sim Q \leftrightarrow \sim P \wedge R$

(3) $\sim Q \leftrightarrow P \vee \sim R$

(4*) $\sim Q \leftrightarrow P \wedge \sim R$

Ans. (4)

Sol. Given statement is equal to $(p \wedge \sim R) \leftrightarrow Q$

Negation of the above statment is $\sim Q \leftrightarrow (p \wedge \sim R)$

$$\sim Q \leftrightarrow p \wedge \sim R$$



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