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# J = <br> [ADVANGED] 2023 <br> <br> QUESTIONS \& TEXT SOLUTION 

 <br> <br> QUESTIONS \& TEXT SOLUTION}
PAPER-1

## DATE \& DAY: $4^{\text {th }}$ JUNE 2023, SUNDAY

PAPER-1
Duration: 3 Hrs .
Time: 09:00-12:00 IST

PAPER-2
Duration: 3 Hrs .
Time: 14:30-17:30 IST

## SUBJECT: PHYSICS

## ADMISSIONS OPEN FOR CLASS 12 PASSED STUDENTS



## 100\% SCHOLARSHIP ON THE BASIS OF JEE CADV.] / JEE (MAIN) 2023 SCORE

〇 REGISTERED \& CORPORATE OFFICE (CIN: U80302RJ2007PLC024029): CG Tower, A-46 \& 52, IPIA, Near City Mall, Jhalawar Road, Kota (Rajasthan) - 324005

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## TARGET: JEE (AdV.) 2024

## VIJAY COURSE

For $12^{\text {th }}$ Passed Students
Course Features*
Course Duration: $\mathbf{3 2}$ Weeks
Total No. of Lectures: $\mathbf{5 3 3}$ (P: $\mathbf{1 7 8}|\mathrm{C}: 177|$ M: 178)
Duration of One Lecture: $\mathbf{1 . 5}$ Hrs. (90 Minutes)
Classroom Teaching Hours.: $\mathbf{8 0 0}$ Hrs.
Testing Duration: $\mathbf{6 0}$ Hrs.
Total Academic Hours.: $\mathbf{8 6 0}$ Hrs.


## TARGET: JEE (Main) 2024



# AJAY COURSE 

For $12^{\text {th }}$ Passed Students

## Course Features*

- Course Duration: 33 Weeks
- Total No. of Lectures: 571 (P:184 |C: 203 | M: 184)
- Duration of One Lecture: 1.5 Hrs. (90 Minutes)
- Classroom Teaching Hours.: $\mathbf{8 5 7}$ Hrs.
- Testing Duration: $\mathbf{3 3}$ Hrs.
- Total Academic Hours.: $\mathbf{8 9 0}$ Hrs.


## scholarship upto 100\%

Based on JEE (Main) 2023 Score, Scholarship Test (ResoNET) \& $12^{\text {th }}$ Board

## PART : PHYSICS

## SECTION 1 (Maximum Marks: 12)

- This section contains THREE (03) questions.
- Each question has FOUR options (A), (B), (C) and (D). ONE OR MORE THAN ONE of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

Full Marks $\quad: \quad+4$ ONLY if (all) the correct option(s) is(are) chosen;
Partial Marks : +3 If all the four options are correct but ONLY three options are chosen;
Partial Marks : +2 If three or more options are correct but ONLY two options are chosen, both of which are correct;

Partial Marks : +1 If two or more options are correct but ONLY one option is chosen and it is acorrect option;
Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);
Negative Marks: -2 In all other cases.

- For example, in a question, if (A), (B) and (D) are the ONLY three options corresponding to correctanswers, then
choosing ONLY (A), (B) and (D) will get +4 marks;
choosing ONLY (A) and (B) will get +2 marks;
choosing ONLY (A) and (D) will get +2 marks;
choosing ONLY (B) and (D) will get +2 marks;
choosing ONLY (A) will get +1 mark;
choosing ONLY (B) will get +1 mark;
choosing ONLY (D) will get +1 mark;
choosing no option (i.e. the question is unanswered) will get 0 marks; and choosing any other combination of options will get -2 marks.


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1. A slide with a frictionless curved surface, which becomes horizontal at its lower end, is fixed on the terrace of a building of height 3 h from the ground, as shown in the figure. A spherical ball of mass $m$ is released on the slide from rest at a height $h$ from the top of the terrace. The ball leaves the slide with a velocity $\overrightarrow{\mathrm{u}}_{0}-\mathrm{u}_{0} \hat{\mathrm{x}}$ and falls on the ground at a distance d from the building making an angle $\theta$ with the horizontal. It bounces off with a velocity $\overrightarrow{\mathrm{V}}$ and reaches a maximum height $h_{1}$. The acceleration due to gravity is $g$ and the coefficient of restitution of the ground is $1 / \sqrt{3}$. Which of the following statement(s) is(are) correct?

(A) $\vec{u}_{0}=\sqrt{2 g h} \hat{x}$
(B) $\vec{v}=\sqrt{2 g h}(\hat{x}-\hat{z})$
(C) $\theta=60^{\circ}$
(D) $d / h_{1}=2 \sqrt{3}$

Ans. (ACD)
Sol. From energy conservation :
$\frac{1}{2} \mathrm{mu}_{0}^{2}=\mathrm{mgh} \Rightarrow \mathrm{u}_{0}=\sqrt{2 \mathrm{gh}}$
Option (A) is correct
$\vec{v}_{0}=\sqrt{2 g h} \hat{i}-\sqrt{2 g h(3 h)} \hat{k}$
$=\sqrt{2 g h}(\hat{i}-\sqrt{3} \hat{k})$
$\tan \theta=\frac{v_{z}}{v_{x}}=\frac{\sqrt{2 g(3 h)}}{\sqrt{2 g h}}=\sqrt{3}$
$\theta=60^{\circ}$
Option (C) is correct
$\sqrt{\frac{h_{1}}{3 h}}=e=\frac{1}{\sqrt{3}} \Rightarrow h_{1}=h$
$d=u_{0} \sqrt{\frac{2(3 h)}{g}}=\sqrt{2 g h} \sqrt{\frac{2 \times 3 h}{g}}$
$d=2 h \sqrt{3}$
$\frac{\mathrm{d}}{\mathrm{h}_{1}}=2 \sqrt{3}$
Option (D) is correct

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2. A plane polarized blue light ray is incident on a prism such that there is no reflection from the surface of the prism. The angle of deviation of the emergent ray is $\delta=60^{\circ}$ (see Figure-1). The angle of minimum deviation for red light from the same prism is $\delta_{\min }=30^{\circ}$ (see Figure-2). The refractive index of the prism material for blue light is $\sqrt{3}$. Which of the following statement(s) is(are) correct?


Figure-1


Figure-2
(A) The blue light is polarized in the plane of incidence.
(B) The angle of the prism is $45^{\circ}$.
(C) The refractive index of the material of the prism for red light is $\sqrt{2}$.
(D) The angle of refraction for blue light in air at the exit plane of the prism is $60^{\circ}$.

Ans. (ACD)
Sol. For blue light
$\mu=\tan \mathrm{i}_{\mathrm{p}}$
$\sqrt{3}=\tan \mathrm{i}_{\mathrm{p}}$
$\mathrm{i}_{\mathrm{p}}=60^{\circ}$
$\delta=\mathrm{i}+\mathrm{e}-\mathrm{A}$
$60=60+e-A$
$e=A$
$\sin 60^{\circ}=\sqrt{3} \sin r_{1}$
$\frac{\sqrt{3}}{2}=\sqrt{3} \sin r_{1}$
$r_{1}=30^{\circ}$
$r_{2}=A-30^{\circ}$
$\sqrt{3} \sin \left(A-30^{\circ}\right)=\sin A$

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$\sqrt{3}\left[\sin A \frac{\sqrt{3}}{2}-\cos A \frac{1}{2}\right]=\sin A$

$$
\frac{3}{2} \sin A-\frac{\sqrt{3}}{2} \cos A=\sin A
$$

$\frac{-\sqrt{3}}{2} \cos A=-\frac{\sin A}{2}$
$\tan \mathrm{A}=\sqrt{3}$
$\mathrm{A}=60^{\circ}$
$\mathrm{e}=60^{\circ}$
For red light

$$
\begin{aligned}
& \frac{\sin \left(\frac{A+\delta_{\text {min }}}{2}\right)}{\sin \frac{A}{2}}=n_{R} \\
& \frac{\sin \left(\frac{90}{2}\right)}{\sin 30}=n_{R} \\
& n=\sqrt{2}
\end{aligned}
$$

3. In a circuit shown in the figure, the capacitor C is initially uncharged and the key K is open. In this condition, a current of 1 A flows through the $1 \Omega$ resistor. The key is closed at time $t=t$. Which of the following statement(s) is(are) correct? [Given: $\mathrm{e}^{-1}=0.36$ ]

(A) The value of the resistance R is $3 \Omega$.
(B) For $t<t_{0}$, the value of current $\mathrm{I}_{1}$ is 2 A .
(C) $\mathrm{At}=\mathrm{t}_{0}+7.2 \mu \mathrm{~s}$, the current in the capacitor is 0.6 A .
(D) For $\mathrm{t} \rightarrow \infty$, the charge on the capacitor is $12 \mu \mathrm{C}$.

Ans. (ABCD)

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Sol.

$\frac{x-5}{1}=1 \Rightarrow x=+6$ volt, $\quad i_{1}=\frac{6-0}{3}=2 A$
$R=\frac{15-6}{3}=3 \Omega$
After switching on :


$$
\begin{aligned}
& \varepsilon_{\text {eq }}=\frac{\frac{15}{3}+\frac{5}{1}+\frac{0}{3}}{\frac{1}{3}+\frac{1}{1}+\frac{1}{3}}=6 \text { volt } \\
& \frac{1}{r_{\text {eq }}}=\frac{1}{3}+\frac{1}{1}+\frac{1}{3} \Rightarrow r_{\text {eq }}=\frac{3}{5} \Omega
\end{aligned}
$$


(D) Steady state charge on the capacitor
$\mathrm{q}=\mathrm{CV}=(2 \mu)(6)=12 \mu \mathrm{C}$
(C) $R_{\text {eq }}=\frac{3}{5}+3=\frac{18}{5} \Omega, i_{\max }=\frac{\varepsilon_{\text {eq }}}{R_{\text {eq }}}=\frac{6}{18 / 5}=\frac{5}{3} \mathrm{~A}$
$\mathrm{Req}_{\mathrm{eq}} \mathrm{C}=\frac{18}{5} \times 2 \Omega=\frac{36}{5} \mu \mathrm{sec}$.
$\frac{\mathrm{t}}{\mathrm{R}_{\mathrm{C}}}=\frac{7.2}{36 / 5}=1$
$i(t)=\frac{\varepsilon_{e q}}{R_{\text {eq }}} e^{-\frac{t}{R_{e q} C}}=\frac{5}{3} e^{-1}=\frac{5}{3} \times 0.36$
$\mathrm{i}=0.6 \mathrm{~A}$

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## SECTION 2 (Maximum Marks: 12)

- This section contains FOUR (04) questions.
- Each question has FOUR options (A), (B), (C) and (D). ONLY ONE of these four options is the correctanswer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:

Full Marks : $\quad+3$ If ONLY the correct option is chosen
Zero Marks : 0 If none of the options is chosen (i.e., the questions is unanswered) ;
Negative Marks: -1 In all other cases.
4. A bar of mass $M=1.00 \mathrm{~kg}$ and length $L=0.20 \mathrm{~m}$ is lying on a horizontal frictionless surface. One end of the bar is pivoted at a point about which it is free to rotate. A small mass $m=0.10 \mathrm{~kg}$ is moving on the same horizontal surface with $5.00 \mathrm{~ms}^{-1}$ speed on a path perpendicular to the bar. It hits the bar at a distance $\mathrm{L} / 2$ from the pivoted end and returns back on the same path with speed v. After this elastic collision, the bar rotates with an angular velocity $\omega$. Which of the following statement is correct?
(A) $\omega=6.98 \mathrm{rad} \mathrm{s}^{-1}$ and $\mathrm{v}=4.30 \mathrm{~ms}^{-1}$
(B) $\omega=3.75 \mathrm{rad} \mathrm{s}^{-1}$ and $v=4.30 \mathrm{~ms}^{-1}$
(C) $\omega=3.75 \mathrm{rad} \mathrm{s}^{-1}$ and $\mathrm{v}=10.0 \mathrm{~ms}^{-1}$
(D) $\omega=6.80 \mathrm{rad} \mathrm{s}^{-1}$ and $\mathrm{v}=4.10 \mathrm{~ms}^{-1}$

Ans. (A)
Sol.


For the (rod + ball) system :
(i) The angular momentum will remain conserved only about the hinge axis.

About the hinge axis: $\mathrm{L}_{\mathrm{i}}=\mathrm{L}_{\mathrm{f}}$
$0+(0.1)(5)(0.1)=\left(\frac{(1)(0.2)^{2}}{3}\right) \omega-(0.1)(v)(0.1)$

$$
\begin{equation*}
\frac{4 \omega}{3}-v=5 \tag{1}
\end{equation*}
$$

(ii) $e=\frac{\omega(0.1)+v}{5}$ where $e=1$
$\frac{\omega}{10}+v=5$
Solving $\omega=\frac{300}{43}=6.98 \mathrm{rad} / \mathrm{sec}$.
$\mathrm{v}=4.30 \mathrm{~m} / \mathrm{sec}$.

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## 

5. A container has a base of $50 \mathrm{~cm} \times 5 \mathrm{~cm}$ and height 50 cm , as shown in the figure. It has two parallel electrically conducting walls each of area $50 \mathrm{~cm} \times 50 \mathrm{~cm}$. The remaining walls of the container are thin and non-conducting. The container is being filled with a liquid of dielectric constant 3 at a uniform rate of $250 \mathrm{~cm}^{3} \mathrm{~s}^{-1}$. What is the value of the capacitance of the container after 10 seconds?
[Given: Permittivity of free space $\epsilon_{0}=9 \times 10^{-12} \mathrm{C}^{2} \mathrm{~N}^{-1} \mathrm{~m}^{-2}$, the effects of the non-conducting walls on the capacitance are negligible]

(A) 27 pF
(B) 63 pF
(C) 81 pF
(D) 135 pF

Ans. (B)
Sol. Height of water filled at $t=10 \mathrm{sec}$.
$h=\frac{250 \times 10}{50 \times 5}=10 \mathrm{~cm}$
$\mathrm{C}=\frac{\varepsilon_{0}}{\mathrm{~d}}\left[\mathrm{~A}_{1} \mathrm{~K}_{1}+\mathrm{A}_{2} \mathrm{~K}_{2}\right]=\frac{9 \times 10^{-12}}{0.05}[0.5 \times 0.1 \times 3+0.5 \times 0.4 \times 1]=63 \times 10^{-12} \mathrm{~F}$
6. One mole of an ideal gas expands adiabatically from an initial state $\left(T_{A}, V_{0}\right)$ to final state $\left(T_{f}, 5 V_{0}\right)$. Another mole of the same gas expands isothermally from a different initial state ( $T_{B}, V_{0}$ ) to the same final state $\left(T_{f}, 5 V_{0}\right)$. The ratio of the specific heats at constant pressure and constant volumeof this ideal gas is $\gamma$. What is the ratio $T_{A} / T_{B}$ ?
(A) $5^{\gamma-1}$
(B) $5^{1-\gamma}$
(C) $5^{\gamma}$
(D) $5^{1+\gamma}$

Ans. (A)
Sol.

$\mathrm{T}_{\mathrm{A}} \mathrm{V}_{0}{ }^{\gamma-1}=\mathrm{T}_{\mathrm{B}}\left(5 \mathrm{~V}_{0}\right)^{\gamma-1}$
$\mathrm{T}_{\mathrm{A}}=5^{\gamma-1} \mathrm{~T}_{\mathrm{B}}$
$T_{A} / T_{B}=5^{\gamma-1}$

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## 

7. Two satellites $P$ and $Q$ are moving in different circular orbits around the Earth (radius $R$ ). The heights of $P$ and $Q$ from the Earth surface are $h_{P}$ and $h_{Q}$, respectively, where $h_{P}=R / 3$. The accelerations of $P$ and $Q$ due to Earth's gravity are $g_{p}$ and $g_{Q}$, respectively. If $g_{p} / g_{Q}=36 / 25$, what is the value of $h_{Q}$ ?
(A) $3 \mathrm{R} / 5$
(B) $R / 6$
(C) $6 \mathrm{R} / 5$
(D) $5 \mathrm{R} / 6$

Ans. (A)
Sol. $\frac{g_{p}}{g_{Q}}=\frac{G M / r_{P}^{2}}{G M / r_{Q}^{2}}=\frac{36}{25}$
$\frac{r_{Q}}{r_{P}}=\frac{6}{5} \quad \Rightarrow \quad r \mathrm{Q}=\left(\frac{6}{5}\right)\left(\frac{4 \mathrm{R}}{3}\right)=\frac{8 \mathrm{R}}{5}$
$h_{Q}=\frac{8 R}{5}-R=\frac{3 R}{5}$

## SECTION 3 (Maximum Marks: 24)

- This section contains SIX (06) questions.
- The answer to each question is a NON-NEGATIVE INTEGER.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
Answer to each question will be evaluated according to the following marking scheme :
Full Marks : + 4 If ONLY the correct integer is entered ;
Zero Marks : 0 In all other cases.

8. A Hydrogen-like atom has atomic number Z. Photons emitted in the electronic transitions from level $\mathrm{n}=4$ to level $\mathrm{n}=3$ in these atoms are used to perform photoelectric effect experiment on a target metal. The maximum kinetic energy of the photoelectrons generated is 1.95 eV . If the photoelectric threshold wavelength for the target metal is 310 nm , the value of $Z$ is $\qquad$ _.
[Given: hc $=1240 \mathrm{eV}$-nm and $\mathrm{Rhc}=13.6 \mathrm{eV}$, where R is the Rydberg constant, h is the Planck's constant and c is the speed of light in vacuum]

Ans. 3
Sol. $\Psi=\frac{\mathrm{hc}}{\lambda_{\mathrm{th}}}=\frac{1240}{310}=4 \mathrm{eV}$
$K E_{\text {max }}=h \nu-\Psi$
$1.95=h \nu-4 \Rightarrow h \nu=5.95 \mathrm{eV}$
Energy of photon emitted due to electron transition: $\Delta \mathrm{E}=13.6 \mathrm{eV} \mathrm{Z}^{2}\left(\frac{1}{\mathrm{n}_{1}^{2}}-\frac{1}{\mathrm{n}_{2}^{2}}\right)$
$5.95 \mathrm{eV}=13.6 \mathrm{eV}(Z)^{2}\left(\frac{1}{(3)^{2}}-\frac{1}{(4)^{2}}\right)$
$Z=3$

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9. An optical arrangement consists of two concave mirrors $M_{1}$ and $M_{2}$, and a convex lens $L$ with a common principal axis, as shown in the figure. The focal length of $L$ is 10 cm . The radii of curvature of $M_{1}$ and $M_{2}$ are 20 cm and 24 cm , respectively. The distance between $L$ and $M_{2}$ is 20 cm . A point object $S$ is placed at the mid-point between $L$ and $M_{2}$ on the axis. When the distance between $L$ and $M_{1}$ is $\mathrm{n} / 7 \mathrm{~cm}$, one of the images coincides with S . The value of n is $\qquad$ -


Ans. 150
Sol. Case-I


Ist Image
Consider refraction on $\mathrm{M}_{1}$
$\frac{1}{\mathrm{~V}}+\frac{1}{-10}=\frac{1}{-12}$
$\Rightarrow \mathrm{V}=60$
IInd image
Consider refraction from L
$\frac{1}{V}-\frac{1}{-80}=\frac{1}{10} \Rightarrow V=\frac{80}{7}$
It is at the focus of $\mathrm{M}_{2}$,
so $\frac{80}{7}+10=\frac{n}{7}$
$\mathrm{n}=150$

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10. In an experiment for determination of the focal length of a thin convex lens, the distance of the object from the lens is $10 \pm 0.1 \mathrm{~cm}$ and the distance of its real image from the lens is $20 \pm 0.2 \mathrm{~cm}$. The error in the determination of focal length of the lens is $n \%$. The value of $n$ is $\qquad$ .

Ans. 1
Sol. $\frac{1}{V}-\frac{1}{U}=\frac{1}{f}$
$\frac{1}{20}-\frac{1}{-10}=\frac{1}{f}$
$\mathrm{f}=\frac{20}{3}$
$\frac{d f}{f^{2}}= \pm\left[\frac{d v}{v^{2}}+\frac{d u}{\mathrm{U}^{2}}\right] \Rightarrow \frac{\mathrm{df}}{\mathrm{f}}= \pm \mathrm{f}\left[\frac{0.2}{20^{2}}+\frac{0.1}{10^{2}}\right]$
$\frac{d f}{f}= \pm \frac{20}{3}\left[\frac{0.2+0.4}{400}\right] \Rightarrow \frac{d f}{f}= \pm \frac{20}{3}\left[\frac{0.6}{400}\right]$
$\frac{d f}{f} \times 100= \pm \frac{20}{3}\left[\frac{0.6}{400}\right] \times 100 \%=1 \%$
11. A closed container contains a homogeneous mixture of two moles of an ideal monatomic gas $(\gamma=5 / 3)$ and one mole of an ideal diatomic gas $(\gamma=7 / 5)$. Here, $\gamma$ is the ratio of the specific heats at constant pressure and constant volume of an ideal gas. The gas mixture does a work of 66 Joule when heated at constant pressure. The change in its internal energy is $\qquad$ Joule.

Ans. 121
Sol. $n_{1}=2$

$$
n_{2}=1
$$

$C_{P_{1}}=\frac{5}{2} R$
$C_{P_{2}}=\frac{7}{2} R$
$C_{V_{1}}=\frac{3}{2} R$

$$
C_{V_{2}}=\frac{5}{2} R
$$

For mixture of gases
$\gamma=\frac{n_{1} C_{P_{1}}+n_{2} C_{P_{2}}}{n_{1} C_{V_{1}}+n_{2} C_{V_{2}}}=\frac{2 \times \frac{5}{2} R+1 \times \frac{7}{2} R}{2 \times \frac{3}{2} R+1 \times \frac{5}{2} R}=\frac{17}{11}$
as gas is heated at constant pressure.
$\mathrm{W}=\mathrm{nR} \Delta \mathrm{T}$
$\Delta U=n C v \Delta T$
$Q=n C_{p} \Delta T$
Now, $\frac{\Delta U}{W}=\frac{\Delta U}{Q-\Delta U}=\frac{1}{\frac{Q}{\Delta U}-1}$

$$
\text { as } Q=\Delta U+W
$$

$\frac{\Delta \mathrm{U}}{\mathrm{W}}=\frac{1}{\frac{\mathrm{C}_{\mathrm{P}}}{\mathrm{C}_{\mathrm{V}}}-1}=\frac{1}{\gamma-1} ; \frac{\Delta \mathrm{U}}{\mathrm{W}}=\frac{1}{\frac{17}{11}-1} ; \frac{\Delta \mathrm{U}}{66}=\frac{11}{6} ; \Delta \mathrm{U}=121 \mathrm{~J}$

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12. A person of height 1.6 m is walking away from a lamp post of height 4 m along a straight path on the flat ground. The lamp post and the person are always perpendicular to the ground. If the speed of the person is $60 \mathrm{~cm} \mathrm{~s}^{-1}$, the speed of the tip of the person's shadow on the ground with respect to the person is $\qquad$ $\mathrm{cm} \mathrm{s}{ }^{-1}$.

Ans. 40
Sol.

$\frac{x_{1}+x_{2}}{x_{2}}=\frac{4}{1.6}=\frac{5}{2} \Rightarrow x_{2}=\frac{2}{3} x_{1}$
$\frac{\mathrm{dx}_{2}}{\mathrm{dt}}=\frac{2}{3} \frac{\mathrm{dx}_{1}}{\mathrm{dt}}$ where $\frac{\mathrm{dx}_{1}}{\mathrm{dt}}=60 \mathrm{~cm} / \mathrm{sc}$.
$\frac{\mathrm{dx}_{2}}{\mathrm{dt}}=\left(\frac{2}{3}\right)(60)=40 \mathrm{~cm} / \mathrm{sec}$.
13. Two point-like objects of masses 20 gm and 30 gm are fixed at the two ends of a rigid massless rodof length 10 cm . This system is suspended vertically from a rigid ceiling using a thin wire attached to its center of mass, as shown in the figure. The resulting torsional pendulum undergoes small oscillations. The torsional constant of the wire is $1.2 \times 10^{-8} \mathrm{~N} \mathrm{~m} \mathrm{rad}^{-1}$. The angular frequency of the oscillations in $n \times 10^{-3} \mathrm{rad} \mathrm{s}^{-1}$. The value of $n$ is.


Ans. 10

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Sol. $m_{e q}=\frac{m_{1} m_{2}}{m_{1}+m_{2}}=\frac{(20)(30)}{20+30}=12 \mathrm{gm}=12 \times 10^{-3} \mathrm{~kg}$

$$
\mathrm{Icm}_{\mathrm{cm}}=\mathrm{meq} \mathrm{r}^{2}=\left(12 \times 10^{-3}\right)(0.1)^{2}=12 \times 10^{-5} \mathrm{~kg} \cdot \mathrm{~m}^{2}
$$

$\mathrm{T}=2 \pi \sqrt{\frac{\mathrm{I}_{\mathrm{cm}}}{\mathrm{C}}}=\frac{2 \pi}{\omega_{\mathrm{n}}} \Rightarrow \omega_{\mathrm{n}}=\sqrt{\frac{\mathrm{C}}{\mathrm{I}_{\mathrm{cm}}}}=\sqrt{\frac{1.2 \times 10^{-8}}{12 \times 10^{-5}}}$
$\omega_{n}=10 \times 10^{-3} \mathrm{rad} / \mathrm{sec}$.
$=\mathrm{n} \times 10^{-3} \mathrm{rad} / \mathrm{sec} . \quad \Rightarrow \mathrm{n}=10$

## SECTION 4 (Maximum Marks: 12)

This section contains FOUR (04) Matching List Sets.

- Each set has ONE Multiple Choice Question.
- Each set has TWO lists: List-I and List-II.
- List-I has Four entries (P), (Q), (R) and (S) and List-II has Five entries (1), (2), (3), (4) and (5).
- FOUR options are given in each Multiple Choice Question based on List-I and List-II and ONLY ONE of these four options satisfies the condition asked in the Multiple Choice Question.
- Answer to each question will be evaluated according to the following marking scheme:

Full Marks $\quad: \quad+3$ ONLY if the option corresponding to the correct combination is chosen;
Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);
Negative Marks : -1 In all other cases.
14. List-I shows different radioactive decay processes and List-II provides possible emitted particles. Match each entry in List-I with an appropriate entry from List-II, and choose the correct option.

## List-I

(P) ${ }_{92}^{238} \mathrm{U} \rightarrow{ }_{91}^{234} \mathrm{~Pa}$
(Q) ${ }_{82}^{214} \mathrm{~Pb} \rightarrow{ }_{82}^{210} \mathrm{~Pa}$
(R) ${ }_{81}^{210} \mathrm{Tl} \rightarrow{ }_{82}^{206} \mathrm{~Pb}$
(S) ${ }_{91}^{228} \mathrm{~Pa} \rightarrow{ }_{88}^{224} \mathrm{Ra}$

## List-II

(1) one $\alpha$ particle and one $\beta^{+}$particle
(2) three $\beta^{-}$particles and one $\alpha$ particle
(3) two $\beta^{-}$particles and one $\alpha$ particle
(4) one $\alpha$ particle and one $\beta^{+}$particles
(5) one $\alpha$ particle and one $\beta^{+}$particles
(B) $\mathrm{P} \rightarrow 4, \mathrm{Q} \rightarrow 1, \mathrm{R} \rightarrow 2, \mathrm{~S} \rightarrow 5$
(D) $P \rightarrow 5, Q \rightarrow 1, R \rightarrow 3, S \rightarrow 2$

Ans. (A)
Sol. (P) ${ }_{92}^{238} U \rightarrow{ }_{91}^{234} \mathrm{~Pa}+\mathrm{n}_{1}{ }_{2}^{4} \mathrm{He}+\mathrm{n}_{2}{ }_{-1}^{0} \mathrm{e}$
$238=234+4 n_{1} \Rightarrow n_{1}=1$
$92=91+2 n_{1}-n_{2} \Rightarrow n_{2}=1$
(Q) ${ }_{82}^{214} \mathrm{~Pb} \rightarrow{ }_{82}^{210} \mathrm{~Pb}+\mathrm{n}_{1}{ }_{2}^{4} \mathrm{He}+\mathrm{n}_{2}{ }_{-1}^{0} \mathrm{e}$
$214=210+4 n_{1} \Rightarrow n_{1}=1$ $82=82+2 n_{1}-n_{2} \Rightarrow n_{2}=2$
(R) ${ }_{81}^{210} \mathrm{~T} \ell \rightarrow{ }_{82}^{206} \mathrm{~Pb}++\mathrm{n}_{1}{ }_{2}^{4} \mathrm{He}+\mathrm{n}_{2}{ }_{-1}^{0} \mathrm{e}$ $210=206+4 n_{1} \Rightarrow n_{1}=1$
$81=82+2 n_{1}-n_{2} \Rightarrow n_{2}=3$
(S) ${ }_{91}^{228} \mathrm{~Pa} \rightarrow{ }_{88}^{224} \mathrm{Ra}++\mathrm{n}_{1}{ }_{2}^{4} \mathrm{He}+\mathrm{n}_{2}{ }_{-1}^{0} \mathrm{e}$ $228=224+4 n_{1} \Rightarrow n_{1}=1$
$91=88+2 n_{1}-n_{2}=n_{2}=-1$

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## Resonance ${ }^{\circ}$

15. Match the temperature of a black body given in List-I with an appropriate statement in List-II, andchoose the correct option. [Given: Wien's constant as $2.9 \times 10^{-3} \mathrm{~m}-\mathrm{K}$ and $\frac{\mathrm{hc}}{\mathrm{e}}=1.24 \times 10^{-6} \mathrm{~V}-\mathrm{m}$ ]

## List-I

(P) 2000 K
(Q) 3000 K
(R) 5000 K
(S) 10000 K

## List-II

(1) The radiation at peak wavelength can lead to emission of photoelectrons from a metal of work function 4 eV .
(2) The radiation at peak wavelength is visible to human eye.
(3) The radiation at peak emission wavelength will result in the widest central maximum of a single slitdiffraction.
(4) The power emitted per unit area is $1 / 16$ of thatemitted by a blackbody at temperature 6000 K .
(5) The radiation at peak emission wavelength can be used to image human bones
(A) $\mathrm{P} \rightarrow 3, \mathrm{Q} \rightarrow 5, \mathrm{R} \rightarrow 2, \mathrm{~S} \rightarrow 3$
(B) $P \rightarrow 3, Q \rightarrow 2, R \rightarrow 4, S \rightarrow 1$
(C) $\mathrm{P} \rightarrow 3, \mathrm{Q} \rightarrow 4, \mathrm{R} \rightarrow 2, \mathrm{~S} \rightarrow 1$
(D) $\mathrm{P} \rightarrow 1, \mathrm{Q} \rightarrow 2, \mathrm{R} \rightarrow 5, \mathrm{~S} \rightarrow 3$

Ans. (C)
Sol. $\quad \lambda x T=b$
$\lambda=\frac{b}{T}$
$E=\frac{h c}{\lambda}=\frac{h c T}{b}$
$E=\left(\frac{h c}{e b}\right) \times T e V$
$E=\frac{1.24 \times 10^{-6}}{2.9 \times 10^{-3}} \times \mathrm{TeV}$
$E=\left(0.428 \times 10^{-3} \times T\right) \mathrm{eV}$
(P) $\mathrm{T}=2000 \mathrm{~K}$
$\Rightarrow$
$E=0.856 \mathrm{eV}$
(Q) $\mathrm{T}=3000 \mathrm{~K} \quad \Rightarrow \quad \mathrm{E}=1.284 \mathrm{eV}$
(R) $\mathrm{T}=5000 \mathrm{~K} \quad \Rightarrow \quad \mathrm{E}=2.14 \mathrm{eV}$
(S) $\mathrm{T}=10000 \mathrm{~K} \quad \Rightarrow \quad \mathrm{E}=4.28 \mathrm{eV}$

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## Resonance

16. A series LCR circuit is connected to a $45 \sin (\omega t)$ Volt source. The resonant angular frequency of the circuit is $10^{5} \mathrm{rad} \mathrm{s}^{-1}$ and current amplitude at resonance is I 0 . When the angular frequency of the source is $\omega=8 \times 10^{4} \mathrm{rad} \mathrm{s}^{-1}$, the current amplitude in the circuit is 0.05 I . If $\mathrm{L}=50 \mathrm{mH}$, match each entry in ListI with an appropriate value from List-II and choose the correct option.

## List-I

(P) Io in mA
(Q) The quality factor of the circuit
(R) The bandwidth of the circuit in rad s ${ }^{-1}$
(S) The peak power dissipated at resonance in Watt

## List-II

(1) 44.5
(2) 18
(3) 400
(4) 2250
(5) 500
(A) $\mathrm{P} \rightarrow 2, \mathrm{Q} \rightarrow 3, \mathrm{R} \rightarrow 5, \mathrm{~S} \rightarrow 1$
(B) $\mathrm{P} \rightarrow 3, \mathrm{Q} \rightarrow 1, \mathrm{R} \rightarrow 4, \mathrm{~S} \rightarrow 2$
(C) $\mathrm{P} \rightarrow 4, \mathrm{Q} \rightarrow 5, \mathrm{R} \rightarrow 3, \mathrm{~S} \rightarrow 1$
(D) $\mathrm{P} \rightarrow 4, \mathrm{Q} \rightarrow 2, \mathrm{R} \rightarrow 1, \mathrm{~S} \rightarrow 5$

Ans. (B)
Sol. $E=45 \sin (\omega t)$
$\omega_{r} L=\frac{1}{\omega_{r} C}$
$\omega_{r}^{2}=\frac{1}{L C}$
$\left(10^{5}\right)^{2}=\frac{1}{50 \times 10^{-3} \times C}$
$10^{10}=\frac{1}{5 \times 10^{-2} \mathrm{C}} \Rightarrow \mathrm{c}=2 \times 10^{-9} \mathrm{~F}$
at $\omega=8 \times 10^{4} \mathrm{rad} / \mathrm{s}$
$\mathrm{xL}=\omega \mathrm{L}=8 \times 10^{4} \times 50 \times 10^{-3}=4000 \Omega$
$x c=\frac{1}{\omega C}=\frac{1}{8 \times 10^{4} \times 2 \times 10^{-9}}=6250 \Omega$
$\mathrm{X}=\mathrm{Xc}-\mathrm{XL}=2250 \Omega$
Also 0.05I $0=\frac{45}{z}$
$0.05 \times \frac{45}{R}=\frac{45}{z}$
$z=\frac{R}{0.05}$
$\sqrt{R^{2}+x^{2}}=20 R$
$R^{2}+x^{2}=400 R^{2}$
$\Rightarrow \mathrm{R}=112.6 \Omega \quad$ (as $\mathrm{x}=2250 \Omega)$
(P) $\mathrm{I}_{0}=\frac{45}{112.6} \mathrm{~A}=\frac{45 \times 1000}{112.6} \mathrm{~mA} \approx 400 \mathrm{~mA}$
(Q) $Q_{\text {factor }}=\frac{\omega_{r} \times \mathrm{L}}{R}=\frac{10^{5} \times 50 \times 10^{-3}}{112.6}=44.4$
( R ) B and width $=\mathrm{R} / \mathrm{L}=2250 \mathrm{rad} / \mathrm{s}$
(S) Peak power at resonance $=\frac{(45)^{2}}{R}=\frac{(45)^{2}}{112.6} \approx 18 \omega$

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## Resonance <br> I JEE (ADVANCED) 2023 <br> DATE : 04-06-2023 <br> PAPER-1 | PHYSICS

17. A thin conducting rod MN of mass 20 gm , length 25 cm and resistance $10 \Omega$ is held on frictionless, long, perfectly conducting vertical rails as shown in the figure. There is a uniform magnetic field $B_{0}=4 T$ directed perpendicular to the plane of the rod-rail arrangement. The rod is released from rest at time $\mathrm{t}=0$ and it moves down along the rails. Assume air drag is negligible. Match each quantity in List-I with an appropriate value from List-II, and choose the correct option.
[Given: The acceleration due to gravity $\mathrm{g}=10 \mathrm{~m} \mathrm{~s}^{-2}$ and $\mathrm{e}^{-1}=0.4$ ]

$$
\odot \odot \odot \vec{B}_{0} \odot
$$

## List-I


(P) At $t=0.2 \mathrm{~s}$, the magnitude of the induced emf in Volt
(Q) At $t=0.2 \mathrm{~s}$, the magnitude of the magnetic force in Newton
(2) 0.14
(R) At $t=0.2 \mathrm{~s}$, the power dissipated as heat in Watt
(3) 1.20
(S) The magnitude of terminal velocity of the rod in $\mathrm{m} \mathrm{s}^{-1}$
(4) 0.12
(5) 2.00
(A) $\mathrm{P} \rightarrow 5, \mathrm{Q} \rightarrow 2, \mathrm{R} \rightarrow 3, \mathrm{~S} \rightarrow 1$
(B) $P \rightarrow 3, Q \rightarrow 1, R \rightarrow 4, S \rightarrow 5$
(C) $P \rightarrow 4, Q \rightarrow 3, R \rightarrow 1, S \rightarrow 2$
(D) $P \rightarrow 3, Q \rightarrow 4, R \rightarrow 2, S \rightarrow 5$

Ans. (D)
Sol.


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$m g-i \ell B-m \frac{d v}{d t}$
$\mathrm{mg}-\left(\frac{\mathrm{Bv} \ell}{\mathrm{R}}\right) \mathrm{B} \ell=\mathrm{m} \frac{\mathrm{dv}}{\mathrm{dt}}$
$\frac{m g R}{B^{2} \ell^{2}}-v=\frac{m R}{B^{2} \ell^{2}} \frac{d v}{d t}$
$\frac{B^{2} \ell^{2}}{m R} \int_{0}^{t} d t=\int_{0}^{v} \frac{d v}{\frac{m g R}{B^{2} \ell^{2}}-v}$
$5 t=-\ln \left[\frac{2-v}{2}\right]$
$v=2\left\lfloor 1-e^{-5 t}\right\rfloor$
for $t=0.2 \mathrm{~s}$
$\mathrm{v}=2\left(1-\mathrm{e}^{-1}\right)$
$v=2(1-04)$
$\mathrm{v}=1.2 \mathrm{~ms}^{-1}$
$\mathrm{E}=\mathrm{Bv} \ell=4 \times 1.2 \times \frac{1}{4}=1.2 \mathrm{~V}$
$F=m g-i \ell B=20 \times 10^{-3} \times 10-0.12$
$=0.08 \mathrm{~N}$
$P=i^{2} R=0.12 \times 0.12 \times 10=0.144 \mathrm{~W}$
Terminal velocity $\mathrm{v}=2$ for $\mathrm{t}=\infty$
$B v \ell=i R$
$\frac{\mathrm{B}^{2} \ell^{2}}{m R}=\frac{1}{20 \times 10^{-3} \times 10}=5$
$\frac{\mathrm{mgR}}{\mathrm{B}^{2} \ell^{2}}=\frac{20 \times 10^{-3} \times 10 \times 10}{4 \times 4 \times \frac{1}{4} \times \frac{1}{4}}=2$


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