



Time : 3 Hours

Maximum Marks: 180

BY THE INVIGILATOR

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SEAL WITHOUT BEING INSTRUCTED TO DO

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Please read the instructions carefully. You are allotted 5 minutes specifically for this purpose.

INSTRUCTIONS

A. General

- 1. This booklet is your Question Paper. Do not break the seal of this booklet before being instructed to do so by the invigilators.
- 2. The question paper CODE is printed on the left hand top corner of this sheet and on the back cover page of this booklet.
- Blank spaces and blank pages are provided in the question paper for your rough work. No additional sheets will be provided for rough work.
- 4. Blank papers, clipboards, log tables, slide rules, calculators, cameras, cellular phones, pagers and electronic gadget of any kind are NOT allowed inside the examination hall.
- 5. Write your Name and Roll number in the space provided on the back cover of this booklet.
- 6. Answers to the questions and personal details are to be filled on an Optical Response Sheet, which is provided separately. The ORS is a doublet of two sheets upper and lower, having identical layout. The upper sheet is a machine-gradable Objective Response Sheet (ORS) which will be collected by the invigilator at the end of the examination. The upper sheet is designed in such a way that darkening the bubble with a ball point pen will leave an identical impression at the corresponding place on the lower sheet. You will be allowed to take away the lower sheet at the end of the examination. (see Figure-1 on the back cover page for the correct way of darkening the bubbles for valid answers).
- 7. Use a black ball point pen only to darken the bubbles on the upper original sheet. Apply sufficient pressure so that the impression is created on the lower sheet. See Figure-1 on the back cover page for appropriate way of darkening the bubbles for valid answers.
- 8. DO NOT TAMPER WITH / MUTILATE THE ORS OR THIS BOOKLET.
- On breaking the seal of the booklet check that it contains 28 pages and all the 60 questions and corresponding answer choices are legible. Read carefully the instruction printed at the beginning of each section.

B. Filling the right part of the ORS

- 10. The ORS also has a CODE printed on its left and right parts.
- 11. Verify that the CODE printed on the ORS (on both the left and right parts) is the same as that on this booklet and put your signature in the Box designated as R4.
- 12. IF THE CODES DO NOT MATCH, ASK FOR A CHANGE OF THE BOOKLET / ORS AS APPLICABLE.
- 13. Write your Name, Roll No. and the name of centre and sign with pen in the boxes provided on the upper sheet of ORS. Do not write any of this anywhere else. Darken the appropriate bubble UNDER each digit of your Roll No. In such way that the impression is created on the bottom sheet. (see example in Figure 2 on the back cover)

C. Question Paper Format

- The question paper consists of three parts (Physics, Chemistry and Mathematics). Each part consists of two sections.
- 14. Section 1 contains 10 multiple choice questions? Each question has four choices (A), (B), (C) and (D) out of which ONE OR MORE THAN ONE are correct.
- Section 2 contains 10 questions. The answer to each of the questions is a single-digit integer, ranging from 0 to 9 (both inclusive).

Please read the last page of this booklet for rest of the instructions.

	Subject	Section		Page No.
Part i	Physics	1	One or More Than One Option Correct Type	3 - 7
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Part II	Chemistry	1	One or More Than One Option Correct Type	13 - 17
		2	One Integer Value Correct Type	18 - 19
Part III	Mathematics	1	One or More Than One Option Correct Type	20 - 23
		2	One Integer Value Correct Type	24 - 26

Space for Rough Work



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PARTI : PHYSICS

SECTION – 1 : (One or More Than One Options Correct Type)

This section contains 10 multiple choice questions. Each question has four choices (A), (B), (C) and (D) out of which ONE or MORE THAN ONE are correct.

- Let $E_1(r)$, $E_2(r)$ and $E_3(r)$ be the respective electric fields at a distance r from a 1. point charge Q, an infinitely long wire with constant linear charge density λ , and an infinite plane with uniform surface charge density σ . If $E_1(r_0) = E_2(r_0) = E_3(r_0)$ at a given distance r_0 , then
 - (A) $Q = 4\sigma\pi r_0^2$ (C) $E_1(r_0/2) = 2E_2(r_0/2)$
- (B) $r_0 = \frac{\lambda}{2\pi\sigma}$ (D) $E_2(r_0/2) = 4E_3(r_0/2)$ Heater of an electric kettle is made of a wire of length L and diameter d. It takes 4 minutes to raise the temperature of 0.5 kg water by 40 K. This heater is replaced by a new heater having two wires of the same material, each of length L and diameter
 - 2d. The way these wires are connected is given in the options. How much time in minutes will it take to raise the temperature of the same amount of water by 40 K?

(A) 4 if wires are in parallel

(C) 1 if wires are in series (B) 2 if wires are in series (D) 0.5 if wires are in parallel **PHYSICS**



A transparent thin film of uniform thickness and refractive index $n_1 = 1.4$ is coated on the convex spherical surface of radius R at one end of a long solid glass cylinder of refractive index $n_2 = 1.5$, as shown in the figure. Rays of light parallel to the axis of the cylinder traversing through the film from air to glass get focused at distance f_1 from the film, while rays of light traversing from glass to air get focused at distance f_2

(A)
$$|f_1| = 3R$$

(B) $|f_1| = 2.8R$
(C) $|f_2| = 2R$
(D) $|f_2| = 1.4R$
Air n_2
(D) $|f_2| = 1.4R$

4. A student is performing an experiment using a resonance column and a tuning fork of frequency $244 \, s^{-1}$. He is told that the air in the tube has been replaced by another gas (assume that the column remains filled with the gas). If the minimum height at which resonance occurs is $(0.350 \pm 0.005) \, m$, the gas in the tube is

(Useful information : $\sqrt{167RT} = 640 J^{1/2} mole^{-1/2}$; $\sqrt{140RT} = 590 J^{1/2} mole^{-1/2}$. The molar masses M in grams are given in the options. Take the values of $\sqrt{\frac{10}{M}}$ for each gas as given there.)

(A) Neon
$$(M = 20, \sqrt{\frac{10}{20}} = \frac{7}{10})$$

(B) Nitrogen $(M = 28, \sqrt{\frac{10}{28}} = \frac{3}{5})$
(C) Oxygen $(M = 32, \sqrt{\frac{10}{32}} = \frac{9}{16})$
(D) Argon $(M = 36, \sqrt{\frac{10}{36}} = \frac{17}{32})$

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- A light source, which emits two wavelengths $\lambda_1 = 400 \ nm$ and $\lambda_2 = 600 \ nm$, is used 7. in a Young's double slit experiment. If recorded fringe widths for λ_1 and λ_2 are β_1 and β_2 and the number of fringes for them within a distance y on one side of the central maximum are m_1 and m_2 , respectively, then
 - (A) $\beta_2 > \beta_1$
 - (B) $m_1 > m_2$
 - (C) From the central maximum, 3^{rd} maximum of λ_2 overlaps with 5^{th} minimum of λ_1
 - The angular separation of fringes for λ_1 is greater than λ_2

At time t = 0, terminal A in the circuit shown in the figure is connected to B by a key and an alternating current $I(t) = I_0 \cos(\omega t)$, with $I_0 = 1A$ and $\omega = 500 \text{ rad s}^{-1}$ starts flowing in it with the initial direction shown in the figure. At $t = \frac{2\pi}{6\omega}$, the key is switched from B to D. Now onwards only A and D are connected. A total charge Q flows from the battery to charge the capacitor fully. If $C = 20\mu F$, $R = 10 \Omega$ and the battery is ideal with emf of 50V, identify the correct statement (s).



Magnitude of the maximum charge on the capacitor before $t = \frac{7\pi}{6\omega}$ is 1×10^{-3} C. The current in the left part of the circuit just before $t = \frac{7\pi}{6\omega}$ is clockwise. (B) Immediately after A is connected to D, the current in R is 10A. $Q = 2 \times 10^{-3} C$.



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PHYSICS

9. One end of a taut string of length 3m along the x axis is fixed at x = 0. The speed of the waves in the string is $100 ms^{-1}$. The other end of the string is vibrating in the y direction so that stationary waves are set up in the string. The possible waveform(s) of these stationary waves is(are)

(A)
$$y(t) = A \sin \frac{\pi x}{6} \cos \frac{50\pi t}{3}$$

(C) $y(t) = A \sin \frac{5\pi x}{6} \cos \frac{250\pi t}{3}$

(B) $y(t) = A \sin \frac{\pi x}{3} \cos \frac{100\pi t}{3}$ (D) $y(t) = A \sin \frac{5\pi x}{2} \cos 250\pi t$

VD100

A parallel plate capacitor has a dielectric slab of dielectric constant K between its plates that covers 1/3 of the area of its plates, as shown in the figure. The total capacitance of the capacitor is C while that of the portion with dielectric in between is C_1 . When the capacitor is charged, the plate area covered by the dielectric gets charge Q_1 and the rest of the area gets charge Q_2 . The electric field in the dielectric is E_1 and that in the other portion is E_2 . Choose the correct option/options, ignoring edge effects.



SECTION – 2 : (One Integer Value Correct Type)

This section contains 10 questions. Each question, when worked out will result in one integer from 0 to 9 (both inclusive).

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A galvanometer gives full scale deflection with 0.006 A current. By connecting it to a 4990 Ω resistance, it can be converted into a voltmeter of range 0 - 30 V. If connected to a $\frac{2n}{249}\Omega$ resistance, it becomes an ammeter of range 0 - 1.5 A. The value of *n* is

12. To find the distance *d* over which a signal can be seen clearly in foggy conditions, a railways engineer uses dimensional analysis and assumes that the distance depends on the mass density ρ of the fog, intensity (power/area) *S* of the light from the signal and its frequency *f*. The engineer finds that *d* is proportional to $S^{1/n}$. The value of n^{-1} is



8



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A uniform circular disc of mass 1.5 kg and radius 0.5 m is initially at rest on a horizontal frictionless surface. Three forces of equal magnitude F = 0.5 N are applied simultaneously along the three sides of an equilateral triangle XYZ with its vertices on the perimeter of the disc (see figure). One second after applying the forces, the angular speed of the disc in $rad \ s^{-1}$ is

x vw El

NDOI

Consider an elliptically shaped rail PQ in the vertical plane with OP = 3 m and OQ = 3 m an 16 4 m. A block of mass 1 kg is pulled along the rail from P to Q with a force of 18 N, which is always parallel to line PQ (see the figure given). Assuming no frictional losses, the kinetic energy of the block when it reaches Q is $(n \times 10)$ Joules. The value of *n* is (take acceleration due to gravity = $10 m s^{-2}$)

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4 m

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3 m

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Matt Pres PHYSICS A thermodynamic system is taken from an initial state i with internal energy $U_i = 100 J$ to the final state f along two different paths iaf and ibf as schematically shown in the figure. The work done by the system along the paths af, is and bf are **PHYSICS** $W_{af} = 200 J, W_{ib} = 50 J$ and $W_{bf} = 100 J$ respectively. The heat supplied to the system along the path iaf, ib and bf are Q_{taf} , Q_{ib} and Q_{bf} respectively. If the internal energy of the system in the state b is $U_b = 200 \int$ and $Q_{iaf} = 500 f$, the ratio Q_{bf}/Q_{ib} X 2 HE ras 1605 0:10-120 а fer x N NO \sim Two parallel wires in the plane of the paper are distance X_0 apart. A point charge is 18. moving with speed u between the wires in the same plane at a distance X1 from one of the wires. When the wires carry current of magnitude / in the same direction, the radius of curvature of the path of the point charge is R_1 . In contrast, if the currents 7 in the two wires have directions opposite to each other, the radius of curvature of the path is R_2 . If $\frac{X_0}{X_1} = 3$, the value of $\frac{R_1}{R_2}$ is Space for Rough Work NOMIN 5 Fam ? Mo RE Mb * 0 11

Airplanes A and B are flying with constant velocity in the same vertical plane a angles 30° and 60° with respect to the horizontal respectively as shown in figure. The speed of A is $100\sqrt{3} ms'^{-1}$. At time t = 0 s, an observer in A finds B at a distance of A is $100\sqrt{3} ms'^{-1}$. 500 m. This observer sees B moving with a constant velocity perpendicular to the line of motion of A. If at $t = t_0$, A just escapes being hit by B, t_0 in seconds is

19.

* 0



A rocket is moving in a gravity free space with a constant acceleration of 2 ms^{-2} along + x direction (see figure). The length of a chamber inside the rocket is 4 m. A ball is thrown from the left end of the chamber in + x direction with a speed of 0.3 ms^{-1} relative to the rocket. At the same time, another ball is thrown in -xdirection with a speed of 0.2 ms^{-1} from its right end relative to the rocket. The time in seconds when the two balls hit each other is



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PART II : CHEMISTRY

SECTION – 1: (One or More Than One Options Correct Type)

This section contains 10 multiple choice type questions. Each question has four choices (A), (B), (C) and (D) out of which ONE or MORE THAN ONE are correct.

CHEMISTRY

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- the electronic effect of the tert-butyl group (D)

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CHEMISTRY In the reaction shown below, the major product(s) formed is/are 28⁄. NH₂ acetic anhydride product(s) CH₂Cl₂ NH₂ 0 CH₃ NH_2 + CH₃COOH + CH₃COOH NH₂ CH_3 0 || 0 0 **(**B) ⊕ ⊝ .NH₃ CH₃COO + H₂O CH₃ CH₃ (C) Ö ö

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CHEMISTRY

An ideal gas in a thermally insulated vessel at internal pressure = P_1 , volume = V_1 and absolute temperature = T_1 expands irreversibly against zero external pressure, as shown in the diagram. The final internal pressure, volume and absolute temperature of the gas are P_2 , V_2 and T_2 , respectively. For this expansion,



SECTION – 2 : (One Integer Value Correct Type)

This section contains 10 questions. Each question, when worked out will result in one integer from 0 to 9 (both inclusive).

31. The total number of <u>distinct naturally occurring amino acids</u> obtained by complete acidic hydrolysis of the peptide shown below is



- **32.** MX_2 dissociates into M^{2+} and X^- ions in an aqueous solution, with a degree of dissociation (α) of 0.5. The ratio of the observed depression of freezing point of the aqueous solution to the value of the depression of freezing point in the absence of ionic dissociation is
- **33.** If the value of Avogadro number is 6.023×10^{23} mol⁻¹ and the value of Boltzmann constant is 1.380×10^{-23} J K⁻¹, then the number of significant digits in the calculated value of the universal gas constant is
- **34.** A compound H_2X with molar weight of 80 g is dissolved in a <u>solvent having density</u> of 0.4 g ml⁻¹. Assuming no change in volume upon dissolution, the **molality** of a 3.2 molar solution is
- 35. In an atom, the total number of electrons having quantum numbers n = 4, $|m_l| = 1$ and $m_s = -\frac{1}{2}$ is

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***** Rand Britis CHEMISTRY 36. Consider the following list of reagents : Acidified $K_2Cr_2O_7$, alkaline KMnO₄, CuSO₄, H₂O₂, Cl₂, O₃, FeCl₃, HNO₃ and Na₂S₂O₃. The total number of reagents that can oxidise aqueous iodide to iodine is m)] A list of species having the formula XZ₄ is given below. XeF₄, SF₄, SiF₄, BF₄, BrF₄, [Cu(NH₃)₄]²⁺, [FeCl₄]²⁻, [CoCl₄]²⁻ and [PtCl₄]²⁻. Defining shape on the basis of the location of X and Z atoms, the total number of species having a square planar shape is **CHEMISTRY** Consider all possible isomeric ketones, including stereoisomers of MW = 100. All these isomers are independently reacted with NaBH4 (NOTE: stereoisomers are also reacted separately). The total number of ketones that give a racemic product(s) is/are The total number(s) of stable conformers with non-zero dipole moment for the following compound is (are) Br -CH₃ Br--CI ĊH₃ Among PbS, CuS, HgS, MnS, Ag₂S, NiS, CoS, Bi₂S₃ and SnS₂, the total number of **BLACK** coloured sulphides is Space for Rough Work Ut73 CrCr F.F.1-P 100-28 12x2n+Un+1 2(+(2n+1)b2b)11 Dun + Umi-2 0 19 * 0 29-5270

PART III : MATHEMATICS

SECTION – 1 : (One or More Than One Options Correct Type)

This section contains 10 multiple choice questions. Each question has four choices (A), (B), (C) and (D) out of which ONE or MORE THAN ONE are correct.



MATHEMATICS From a point $P(\lambda, \lambda, \lambda)$, perpendiculars PQ and PR are drawn respectively on the 43. lines y = x, z = 1 and y = -x, z = -1. If P is such that $\angle QPR$ is a right angle, then the possible value(s) of λ_{λ} is(are) (A) $\sqrt{2}$ (B) 1 (C) -1 __√2 Let \vec{x} , \vec{y} and \vec{z} be three vectors each of magnitude $\sqrt{2}$ and the angle between each pair of them is $\frac{\pi}{2}$. If \vec{a} is a nonzero vector perpendicular to \vec{x} and $\vec{y} \times \vec{z}$ and \vec{b} is a nonzero vector perpendicular to \vec{y} and $\vec{z} \times \vec{x}$, then $(A) \vec{b} = (\vec{b} \cdot \vec{z})(\vec{z} - \vec{x})$ $(B) \langle \vec{a} = (\vec{a} \cdot \vec{y})(\vec{y} - \vec{z})$ $\vec{a} \cdot \vec{b} = -(\vec{a} \cdot \vec{y}) (\vec{b} \cdot \vec{z})$ $\gamma(\mathbf{D}) \vec{a} = (\vec{a} \cdot \vec{y})(\vec{z} - \vec{y})$ Let $f: \left(-\frac{\pi}{2}, \frac{\pi}{2}\right) \to \mathbb{R}$ be given by $\overline{f(x)} = (\log(\sec x + \tan x))^3.$ TR. Mpz)nD. Then (A) f(x) is an odd function **(B)** f(x) is a one-one function f(x) is an onto function f(x) is an even function $f(x) \neq f(x)$ (D) <u>MATHEMATICS</u> Space for Rough Work THO, M. ADA + 1 -2 M + 42 = 16 W12-211+42-15-20; Qu-Art: Blog (Scontten) se M2442-120. E G, -15 - (Dean tun) ræg, bri -Qbg,br C LTK 2'2'-8 m2 ty ATUNITZYY # 1= D. C. T. ina 1+24+1=0 dy = -2dy =* 0





- there is a 3×3 non-zero matrix U such that $(M^2 + MN^2)U$ is the zero matrix
- (C) determinant of $(M^2 + MN^2) \ge 1$
- (D) for a 3×3 matrix U, if $(M^2 + MN^2)U$ equals the zero matrix then U is the zero matrix



SECTION – 2 : (One Integer Value Correct Type)

This section contains 10 questions. Each question, when worked out will result in one integer from 0 to 9 (both inclusive).

- **51.** For a point P in the plane, let $d_1(P)$ and $d_2(P)$ be the distances of the point P from the lines x y = 0 and x + y = 0 respectively. The area of the region R consisting of all points P lying in the first quadrant of the plane and satisfying $2 \le d_1(P) + d_2(P) \le 4$, is
- 52. Let \vec{a} , \vec{b} , and \vec{c} be three non-coplanar unit vectors such that the angle between every pair of them is $\frac{\pi}{3}$. If $\vec{a} \times \vec{b} + \vec{b} \times \vec{c} = p\vec{a} + q\vec{b} + r\vec{c}$, where p, q and rare scalars, then the value of $\frac{p^2 + 2q^2 + r^2}{q^2}$ is
- **53.** The largest value of the non-negative integer a for which $\sum_{i=1}^{n}$

lim	$\left(\frac{-ax + sin(x-1) + a}{1 - \sqrt{x}}\right)^{\frac{1-x}{1 - \sqrt{x}}} - 1$	
$x \rightarrow 1$	$\frac{1}{x+\sin(x-1)-1} = \frac{1}{4}$	
\sim		

is

Let $f:[0,4\pi] \rightarrow [0,\pi]$ be defined by $f(x) = \cos^{-1}(\cos x)$. The number of $x \in [0, 4\pi]$ satisfying the equation points $f(x) = \frac{10-x}{10-x}$ $\frac{10}{10}$ Sin . is



a dense fo **MATHEMATICS**-Let $f: \mathbb{R} \to \mathbb{R}$ and $g: \mathbb{R} \to \mathbb{R}$ be respectively given 55. bγ $f(\mathbf{x})$ |x| + 1 and $g(x) = x^2 + 1$. Define $h: \mathbb{R} \to \mathbb{R}$ by $h(x) = \begin{cases} \max & \{f(x), g(x)\} \end{cases}$ 10 if $x \leq 0$, $(\min \{f(x), g(x)\}\)$ if x > 0. 7:23.4 The number of points at which h(x) is not differentiable is Let $n_1 > n_2 < n_3 < n_4 < (n_5)$ be positive integers such that 56. $n_1 + n_2 + n_3 + n_4 + n_5 < 20$ Then the number of such distinct arrangements $(n_1, n_2, n_3, n_4, n_5)$ is Let $n \ge 2$ be an integer. Take *n* distinct points on a <u>circle and join each pair</u> of 57 points by a line segment. Colour the line segment joining every pair of adjacent points by blue and the rest by red. If the number of red and blue line segments are equal, then the value of n is (b Space for Rough Work \overline{m} , \overline{p} \overline{m} , \overline{m} , \overline{p} \overline{m} , \overline{m} , \overline{p} \overline{m} , \overline MATHEMATICS TO mr-2 NOME C B63.14 9.14

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MATHEMATICS

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- 58. The slope of the tangent to the curve $(y x^5)^2 = x(1 + x^2)^2$ at the point (1, 3) is
- **59.** Let *a*, *b*, *c* be positive integers such that $\frac{b}{a}$ is an integer. If *a*, *b*, *c* are in geometric progression and the arithmetic mean of *a*, *b*, *c* is *b* + 2, then the value of

$$\frac{a^2+a-14}{a+1}$$

is

60. The value of
$$\int_{0}^{1} 4x^{3} \left\{ \frac{d^{2}}{dx^{2}} (1-x^{2})^{5} \right\} dx$$
is

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