NATIONAL STANDARD EXAMINATION IN PHYSICS (NSEP) 2022

Organized by
INDIAN ASSOCIATION OF PHYSICS TEACHERS (IAPT)

QUESTIONS, ANSWERS & SOLUTIONS

Saturday, November 27, 2022 | Time: 8:30 PM to 10:30 PM Hours | Max. Marks : 216

Resonance Eduventures Ltd.

Reg. Office & Corp. Office : CG Tower, A-46 & 52, IPIA, Near City Mall, Jhalawar Road, Kota (Raj.) - 324005

Ph. No.: +91-744-2777777, 2777700 | **FAX No. :** +91-022-39167222

To Know more : sms **RESO** at **56677** | **Website :** www.resonance.ac.in | **E-mail :** contact@resonance.ac.in | **CIN :** U80302RJ2007PLC024029

Toll Free : 1800 258 5555 | 7340010333 | facebook.com/ResonanceEdu | twitter.com/ResonanceEdu | www.youtube.com/resowatch | blog.resonance.ac.in

INSTRUCTIONS

Write the question paper code mentioned above on YOUR OMR Answer Sheet (in the space provided), otherwise your Answer Sheet will NOT be evaluated. Note that the same Question Paper Code appears on each page of the question paper.

Instructions to Candidates:

1. Use of mobile phone, smart watch, and iPad during examination is STRICTLY **PROHIBITED**.
2. In addition to this question paper, you are given OMR Answer Sheet along with candidate's copy.
3. On the OMR sheet, make all the entries carefully in the space provided **ONLY** in **BLOCK CAPITALS** as well as by properly darkening the appropriate bubbles.

   Incomplete/ incorrect/ carelessly filled information may disqualify your candidature.
4. On the OMR Answer Sheet, use only **BLUE or BLACK BALL POINT PEN** for making entries and filling the bubbles.
5. Your **Ten-digit roll number and date of birth** entered on the OMR Answer Sheet shall remain your login credentials means login id and password respectively for accessing your performance / result in Indian **NSEA 2022.**
6. Question paper has two parts. In part A1 (Q. No.1 to 48) each question has four alternatives, out of which only one is correct. Choose the correct alternative and fill the appropriate bubble, as shown.

   Q.No.22 (a) ● (c) (d)

   In part A2 (Q. No. 49 to 60) each question has four alternatives out of which any number of alternative(s) (1, 2, 3 or 4) may be correct. You have to choose all correct alternative(s) and fill the appropriate bubble(s), as shown

   Q.No.54 (a) ● (c) ●
7. For **Part A1**, each correct answer carries 3 marks whereas 1 mark will be deducted for each wrong answer. In **Part A2**, you get 6 marks if all the correct alternatives are marked. No negative marks in this part.
8. Rough work should be done only in the space provided. There are 11 printed pages in this paper.
9. Use of **non-programmable scientific** calculator is allowed.
10. No candidate should leave the examination hall before the completion of the examination.
11. After submitting answer paper, take away the question paper & Candidate's copy of OMR Sheet for your reference.

   Please DO NOT make any mark other than filling the appropriate bubbles properly in the space provided on the OMR answer sheet.

   OMR answer sheets are evaluated using machine, hence CHANGE OF ENTRY IS NOT ALLOWED. Scratching or overwriting may result in a wrong score.

   DO NOT WRITE ON THE BACK SIDE OFTHE OMR ANSWER SHEET.

Instructions to Candidates (Continued) :

You may read the following instructions after submitting the answer sheet.

12. Comments/Inquiries/Grievances regarding this question paper, if any, can be shared on the Inquiry/Grievance column on www.iaptexam.in **on the specified format till December 3, 2022**.

13. The answers/solutions to this question paper will be available on the website: www.iapt.org.in.**by December 2, 2022.**

14. CERTIFICATES and AWARDS:

Following certificates are awarded by IAPT to students, successful in the NATIONAL STANDARD EXAMINATION IN ASTRONOMY-2022.

(i) "CENTRETOP10 %" To be downloaded from iapt.org.in after 15.01.23

(ii) "STATETOP1 %" Will be dispatched to the examinee

(iii) "NATIONALTOP1 %" Will be dispatched to the examinee

(iv) "GOLD MEDAL& MERITCERTIFICATE" to all students who attend OCSC-2023 at HBCSE Mumbai

Certificate for centre toppers shall be uploaded on Iapt.org.in

15. List of students (with centre number and roll number only) having score above MAS will be displayed on the website: www.iapt.org.in by **December 25, 2022. See the Minimum Admissible score clause** on the Student's brochure on the web.

16. List of Students eligible to appear for Indian National Physics Olympiad (INPhO - 2023) shall be displayed on www.iapt.org.in by December 30, 2022.

Physical constants you may need....

Magnitude of charge on electron $e = 1.60 \times 10^{-19}$C	Avogadro's constant $A = 6.023 \times 10^{23}$ mol^{-1}
Mass of electron $m_e = 9.10 \times 10^{-31}$ kg	Speed of light in free space $c = 3 \times 10^{8}$ m/s
Mass of proton $m_p = 1.67 \times 10^{-27}$ kg	Permittivity of free space $\varepsilon_0 = 8.85 \times 10^{-12}$ C^2 / Nm^2
Acceleration due to gravity $g = 9.81$ ms^{-2}	Permeability of free space $\mu_0 = 4\pi \times 10^{-7}$ H / m
Universal gravitational constant $G = 6.67 \times 10^{-11}$ Nm^2 / Kg^2	Planck's constant $h = 6.625 \times 10^{-34}$ Js
Universal gas constant R = 8.31 J / molK	Faraday constant = 96,500 C / mol
Boltzmann constant $k = 1.38 \times 10^{-23}$ J/K	Rydberg constant $R = 1.097 \times 10^{7}$ m^{-1}
Stefan's constant $\sigma = 5.67 \times 10^{-8}$ W / m^2 x K^4	Astronomical unit = 1.50×10^{11} m

INDIAN ASSOCIATION OF PHYSICS TEACHERS

NATIONAL STANDARD EXAMINATION IN PHYSICS (NSEP) 2022

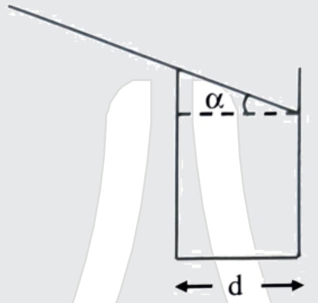
Question Paper Code: 64

Time : 120 Minute **Max. Marks: 216**

PART-A1

ONLY ONE OUT OF FOUR OPTIONS IS CORRECT. BUBBLE THE CORRECT OPTION.

1. A cylindrical tumbler of diameter d has smooth sides and smooth edge. A thin rod of length L is balanced on the edge of the tumbler as shown in figure. The angle α that the rod makes with horizontal for this trick to work is



(a) $\sin^{-1}\left(\frac{d}{L}\right)^{\frac{1}{2}}$ (b) $\cos^{-1}\left(\frac{2d}{L}\right)^{\frac{1}{3}}$ (c) $\cos^{-1}\left(\frac{d}{L}\right)^{\frac{1}{3}}$ (d) $\sin^{-1}\left(\frac{2d}{L}\right)^{\frac{1}{3}}$

Ans. **(b)**

Sol. $N_2 \cos\alpha = mg$ ...(1)

$N_2 \sin\alpha = N_1$ ...(2)

From (1) and (2)

$\frac{N_1}{mg} = \tan\alpha$

$\tau = 0$

$N_1\sin\alpha\ d \sec\alpha = mg\left(\frac{\ell}{2} - d\sec\alpha\right)\cos\alpha$ ...(3)

$mg \tan\alpha\sin\alpha\ d\sec\alpha = mg\left(\frac{\ell}{2}\cos\alpha - d\right)$

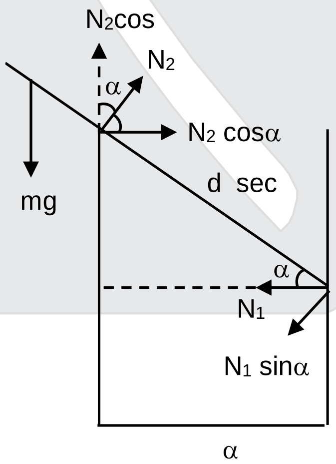
$mg\ d\tan^2\alpha = -mgd + mg\ \frac{\ell}{2}\cos\alpha$

$mgd\ (\sec^2\alpha) = mg\ \frac{\ell}{2}\cos\alpha$

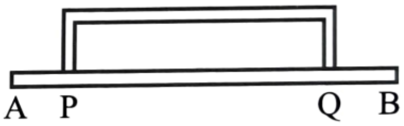
$\frac{2d}{\ell} = \cos^3\alpha$

$\cos\alpha = \left(\frac{2d}{\ell}\right)^{1/3}$

$\alpha = \cos^{-1}\left(\frac{2d}{L}\right)^{1/3}$



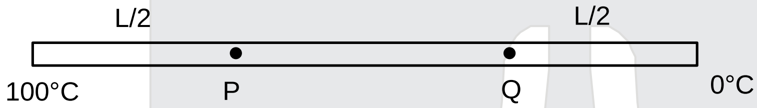
2. End A of a uniform thin rod of length 2L is in boiling water (100ºC) and end B is in melting ice (0ºC). P and Q are two points at distance $\frac{L}{2}$ from A and B respectively. A similar bent rod of length $\frac{3L}{2}$ of same material and equal cross section is joined to rod AB between points P and Q as shown in figure. Then



(a) Temperature at P will increase and that at Q will decrease
(b) Rate of flow of heat will increase by 25%
(c) Rate of flow of heat will decrease by 20%
(d) Rate of heat flow will increase by 37.5%

Ans. **(b)**

Sol.



When bent rod is not connected

then $i_n = \frac{(100-0)kA}{2L} = \frac{100kA}{2L} = \frac{50kA}{L}$

$100 - T_P = i_n \times \frac{L}{2kA}$

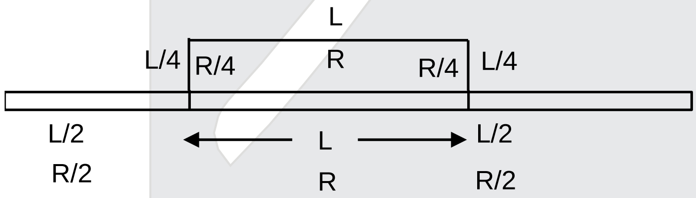
$T_P = 75°$

$T_Q - 0 = i_n \frac{L}{2kA}$

$T_Q - 0 = \frac{100kA}{2L} \times \frac{L}{2kA}$

$T_Q = 25°C$

When bent rod is connected



Where $R = \frac{L}{kA}$

$$R_{eq} = \frac{R}{2} + \frac{R}{2} + \frac{R \times \frac{3R}{2}}{R + \frac{3R}{2}} \quad \Rightarrow R + \frac{3R}{5} = \frac{8R}{5}$$

New Heat flow rate $= i'_n = \frac{(100-0)\times 5}{8R} = \frac{125}{2L}kA$

percent increase in $i_n = \left(\frac{i'_n - i_n}{i_n}\right)\times 100 = \left(\frac{i'_n}{i_n} - 1\right)\times 100$

$$= \left(\frac{125}{100} - 1\right)\times 100$$

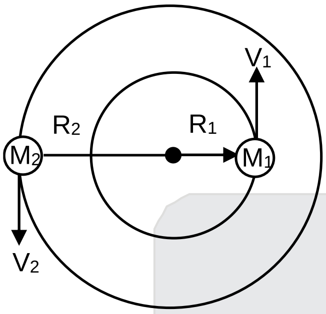
$$\Rightarrow \frac{25}{100}\times 100 = 25\%$$

3. Two stars of masses M and m(M=2m) separated by a distance d = 3 astronomical unit, revolve in circular orbit about their centre of mass with a period of 2 years If M_s is mass of Sum then

(a) $m = 2.25\ M_s$ (b) $m = 1.25\ M_s$ (c) $m = 2.50\ M_s$ (d) $m = 4.50\ M_s$

Ans. **(a)**

Sol.



$$T = \frac{2\pi}{\omega}$$

$$\frac{GM_1M_2}{(R_1+R_2)^2} = M_1\omega^2R_1$$

$$\frac{GM_2}{(R_1+R_2)^2} = \frac{\omega^2M_2D}{(M_1+M_2)}$$

$$\frac{G(M_1+M_2)}{D^3} = \omega^2$$

$$\left(\frac{M_1+M_2}{M_s}\right)\left(\frac{d}{D}\right)^2 = \left(\frac{T_E}{T}\right)^2$$

$$\frac{M_1+M_2}{M_s}\left(\frac{1}{3}\right)^3 = \left(\frac{1}{2}\right)^2$$

$$\frac{M_1+M_2}{M_s} = \frac{27}{4}$$

$M_1+M_2 = 3m$

$$\frac{3m}{M_s} = \frac{27}{4}$$

$$m = \frac{9}{4}M_5 = 2.25M_5$$

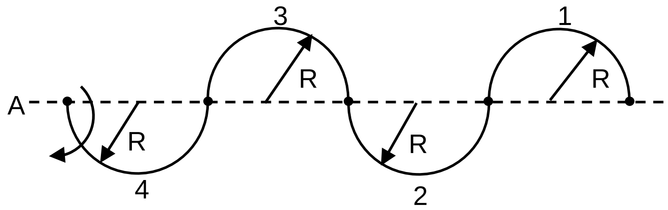
Ans.

4. A thin uniform rod of mass M is bent in to four adjacent semicircles of radius of curvature R lying in same plane. Moment of inertia of the bent rod about an axis through one end A and perpendicular to plane of rod is

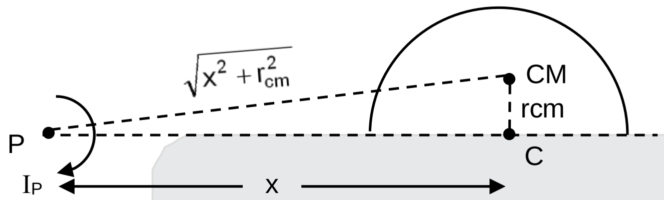
(a) $\frac{17}{2}MR^2$ (b) $44\ MR^2$ (c) $22\ MR^2$ (d) $\frac{43}{2}MR^2$

Ans. **(c)**

Sol.



Concept

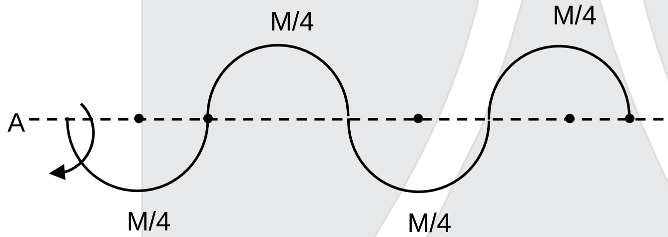


$I_C = I_{cm} + mr_{cm}^2$

$I_{cm} = I_C - mr_{cm}^2 = mR^2 - mR_{cm}^2$

$I_P = I_{cm} + m(x^2 + r_{cm}^2)$

$= mR^2 - mr_{cm}^2 + mx^2 + mr_{cm}^2 = mR^2 + mx^2 = m(R^2 + x^2)$



$$I_A = \frac{MR^2}{4} + \frac{MR^2}{4} + \frac{M}{4}[R^2 + (3R)^2] + \frac{M}{4}[R^2 + (5R)^2] + \frac{M}{4}[R^2 + (7R)^2]$$

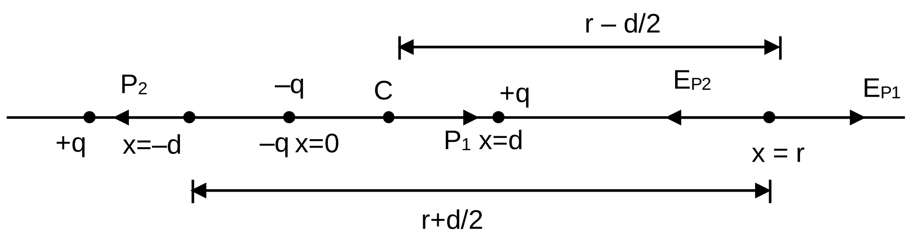
$$\frac{MR^2}{4}[2 + 10 + 26 + 50] = \frac{MR^2}{4} \times 88 = 22MR^2$$

5. Three point charges +q, –2q and + q are placed on x – axis at x = –d, x = 0 and x = +d respectively. The value of electric field at a point P on x axis at x = r (r >>d) is given by $E = \frac{1}{4\pi\varepsilon_0}\frac{aQ}{r^n}$ (here Q = 2qd²) Then

(a) a = 3, n = 3 (b) a = 6, n = 4 (c) a = 3, n = 4 (d) $a = \frac{3}{2}, n = 4$

Ans. (c)

Sol.



$E_{net} = E_{P_1} - E_{P_2}$

$$= \frac{2kP_1}{\left(r-\frac{d}{2}\right)^3} - \frac{2kP_2}{\left(r+\frac{d}{2}\right)^3} = \frac{2kqd}{\left(r-\frac{d}{2}\right)^3} - \frac{2kqd}{\left(r+\frac{d}{2}\right)^3} = \frac{2kqd}{r^3}\left[1+\frac{3d}{2r}-\left(1-\frac{3d}{2r}\right)\right]$$

$$= \frac{2kqd}{r^3} \times \frac{6d}{2r} = \frac{6kqd^2}{r^4} = \frac{3 \times k2qd^2}{r^4} = \frac{3kQ}{r^4} \quad \Rightarrow \frac{3Q}{4\pi\varepsilon_0 r^4} \qquad a = 3, n = 4$$

6. A sound source of fix frequency is in unison with an open end organ pipe of length 30.0 cm and a close end organ pipe of length 23.0 cm (both of same diameter). Both pipes are sounding their first overtone. if velocity of sound is 340 ms^{-1}. frequency of sound source is nearly

(a) 1000Hz (b) 1062 Hz (c) 1100Hz (d) 1018 Hz

Ans. **(b)**

Sol. $f_{\text{Open pipe}} = \dfrac{V}{\ell_1 + 1.2r}$ where l_1 = 30 cm and l_2 = 23.0 cm

$f_{\text{closed pipe}} = \dfrac{3V}{4(\ell_2 + 0.6r)}$

as both are in resonance

$$\frac{V}{\ell_1 + 1.2r} = \frac{3V}{4(\ell_2 + 0.6r)}$$

$4\ell_2 + 2.4r = 3\ell_1 + 3.6r$

$4 \times 23 - 3\ell_1 = 1.2r$

$92 - 3 \times 30 = 1.2r$

$r = 2/1.2$

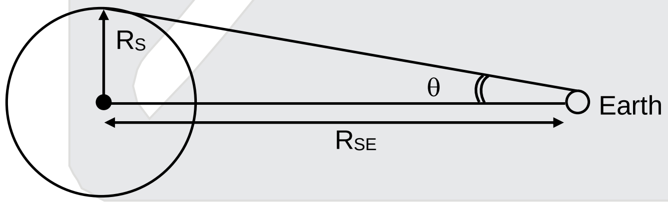
$$f = \frac{V}{\ell_1 + 1.2r} = \frac{340}{30 + 1.2 \times \frac{2}{1.2}} \Rightarrow \frac{340\,m/s}{32cm} = \frac{340\,m/s}{32 \times 10^{-2}\,m} = \frac{34000}{32} = 1062.5 \approx 1062 \text{ Hz}$$

7. Solar constant for Earth is 2.0 cal per cm^2 per minute. [1cal = 4.2J]. Angular diameter of the sun (seen from the Earth) is $\dfrac{1^o}{2}$. (= half a degree). Treating Sun as a black body. its surface temperature is estimated to be nearly.

(a) 6000 K (b) 5800 K (c) 6200 K (d) 5500 K

Ans. **(a)**

Sol. Solar constant = S = $\dfrac{\rho T^4 \times 4\pi R_s^2}{4\pi R_{SE}^2}$



$$S = \rho T^4 \left(\frac{R_S}{R_{SE}}\right)^2$$

$$R_{SE} \times \frac{1}{4} \times \frac{\pi}{180} = R_S$$

$$\frac{R_S}{R_{SE}} = \frac{\pi}{720}$$

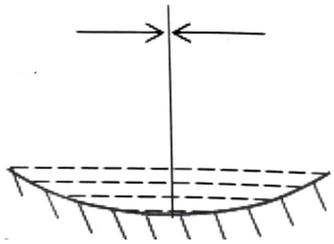
$$S = \sigma T^4 \times \left(\frac{\pi}{720}\right)^2$$

$$\frac{2.0 \times 4.2 \times 10^4}{60} = \frac{5.67 \times 10^{-4} T^4 \times (3.14)^2}{(720)^2}$$

T = 6002.57K

T ≈ 6000K

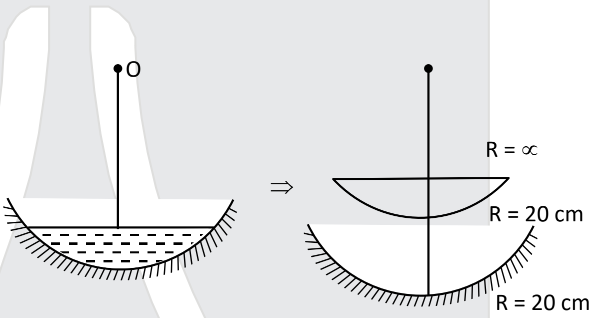
8. A concave mirror when placed in air has a focal length f = 20 cm. The mirror is now placed horizontally and filled with a thin layer of water having refractive index 4/3. The object is placed horizontally near the principal axis at a distance d from the mirror such that a real, inverted image is formed at the same plane as the object, as shown in the figure. What is the value of d?



(a) 30 cm (b) 20 cm (c) 15 cm (d) 40 cm

Ans. **(a)**

Sol.



f = R/2

R = 2f = 40 cm

$$\frac{1}{f_{eq}} = \frac{-2}{f_L} + \frac{1}{f_M} = 2\left[\frac{4}{3} - 1\right]\frac{1}{R} + \frac{1}{20}$$

$$\frac{1}{f_{eq}} = 2 \times \frac{1}{3} \times \frac{1}{40} + \frac{1}{20}$$

$$\frac{1}{f_{eq}} = \frac{1}{60} + \frac{1}{20}$$

f_{eq} = 15 cm

As I coincide with O $\therefore$ d = $2f_{eq}$ = 30 cm

9. When a sample of atoms is irradiated by neutrons, radioactive atoms are produced at a constant rate R, which decay with decay constant λ. The number of radioactive atoms accumulated after an irradiation time is given by

(a) $N(t) = Rte^{-\lambda t}$ (b) $N(t) = \frac{R}{\lambda}e^{-\lambda t}$ (c) $N(t) = \frac{R}{\lambda}\left(1 - e^{-\lambda t}\right)$ (d) $N(t) = Rt\left(1 - e^{-\lambda t}\right)$

Ans. **(c)**

Sol. $\xrightarrow[\text{R Nuclei / sec}]{\text{Production}} A \xrightarrow[\text{Decaying}]{\lambda}$

Let at time t number of nuclei of A = N

$$\frac{dN}{dt} = R - \lambda N$$

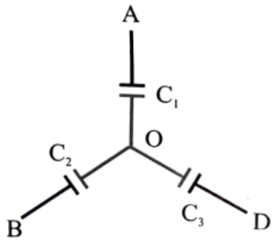
$$\int_0^N \frac{dN}{R - \lambda N} = \int_{t=0}^{t=t} dt$$

$$-\frac{1}{\lambda}\ell n\left(\frac{R - \lambda N}{R}\right) = t$$

$$\frac{R - \lambda N}{R} = e^{-\lambda t}$$

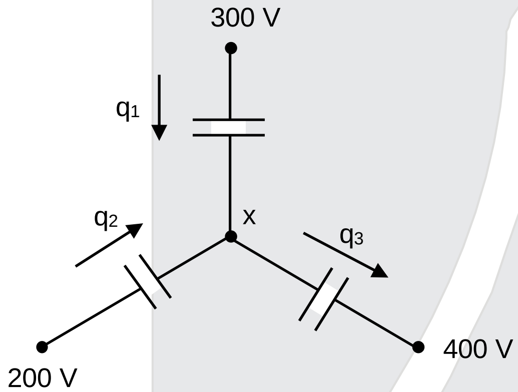
$$N = \frac{R}{\lambda}\left[1 - e^{-\lambda t}\right]$$

10. Three uncharged capacitors of capacitances $C^1 = 2\mu F$, $C^2 = 3\mu F$ and $C^3 = 5\mu F$ are connected as shown in figure to one another at o and to points A,B and D at potentials $V_A = 300V$, $V_B = 200V$ and $V_D = 400$ V respectively the potential V_0 at O is



(a) 300 V (b) 320 V (c) 240 V (d) 280 V

Ans. **(b)**



$q_1 + q_2 + q_3 = 0$

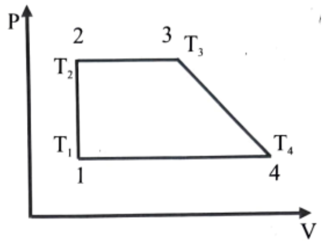
$0 = 2(300 - x) + (200 - x) \times 3 + (400 - x) \times 5$

$0 = 600 - 2x + 600 - 3x + 2000 - 5x$

$3200 - 10x = 0$

$x = 320$ V

11. A cyclic process 1-2-3-4-1 consisting of two isobars 2 – 3 and 4 – 1, an isochor 1 – 2 and a process 3 – 4 represented by straight line on a P-V diagram, as shown in figure, involves n moles of an ideal gas. The gas temperatures at states 1, 2, 3, & 4 are T_1, T_2, T_3, and T_4 respectively. Also points 3 and 4 lie on the same isotherm. The work done by gas during the cycle is

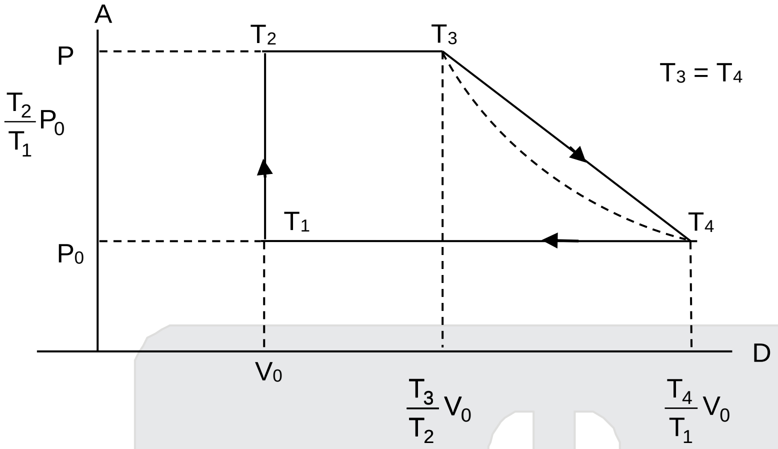


(a) $\frac{1}{2}nR(T_2 - T_1)\left(\frac{T_2}{T_1} + \frac{T_3}{T_4} - 2\right)$ (b) $\frac{1}{2}nR(T_3 - T_2)\left(\frac{T_3}{T_2} + \frac{T_4}{T_1} - 2\right)$

(c) $\frac{1}{2}nR(T_2 - T_1)\left(\frac{T_3}{T_1} + \frac{T_3}{T_2} - 2\right)$ (d) Zero

Ans. **(c)**

Sol.



$P_0V_0 = nRT_1$

$$W = \frac{1}{2}\left[\frac{T_4}{T_1}V_0 - V_0 + \frac{T_3}{T_2}V_0 - V_0\right]\left[\frac{T_2}{T_1}P_0 - P_0\right]$$

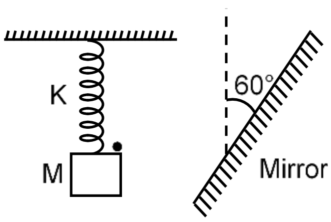
$$W = \frac{P_0V_0}{2}\left[\frac{T_4}{T_1} + \frac{T_3}{T_2} - 2\right]\left[\frac{T_2}{T_1} - 1\right]$$

$$W = \frac{nR(T_2 - T_1)}{2}\left[\frac{T_4}{T_1} + \frac{T_3}{T_2} - 2\right]$$

As $T_3 = T_4$

$$W = \frac{nR(T_2 - T_1)}{2}\left[\frac{T_3}{T_1} + \frac{T_3}{T_2} - 2\right]$$

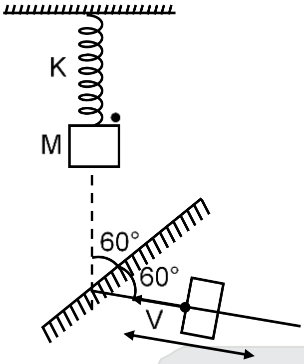
12. A insect of negligible mass is sitting on a block of mass M, tied with a spring of force constant K. The block performs simple harmonic motion vertically with amplitude A in front of a mirror which is inclined at 60º with the vertical as shown. The maximum speed of insect relative to its image will be



(a) $2A\sqrt{\frac{K}{M}}$ (b) $A\sqrt{\frac{3K}{M}}$ (c) $A\sqrt{\frac{K}{M}}$ (d) Zero

Ans. **(b)**

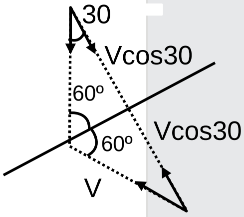
Sol. $V_{relative} = 2V \cos 30$



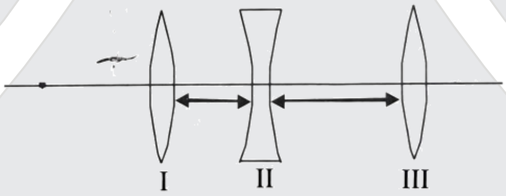
$V_{relative}$ max $= 2\omega A \cos 30$

$= 2\sqrt{\frac{k}{M}} A \frac{\sqrt{3}}{2}$

$\Rightarrow A\sqrt{\frac{3k}{M}}$ Ans. (B)



13. A concave lens of focal length 10 cm is paced between two convex lenses of focal length 10 cm and 20 cm at a separation of 5 cm between the second and third lens. An object is placed at 30 cm in front of the first convex lens. The final image is formed beyond the third lens at a distance v from it. Then

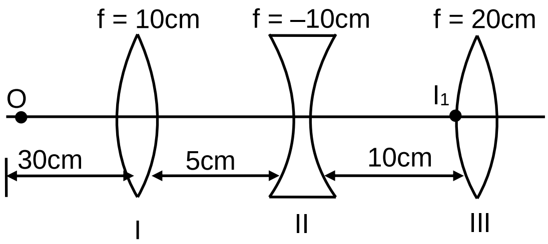


(a) v = 15 cm (b) v = ∞ (c) v = 45 cm (d) V = 20 cm

Ans. **(d)**

Sol. Event -1

object = O Image I_1



$$\frac{1}{10} = \frac{1}{V_1} - \frac{1}{30}$$

$$\frac{1}{10} - \frac{1}{30} = \frac{1}{V_1}$$

$V_1 = 15$

Event-2 Object = I_1

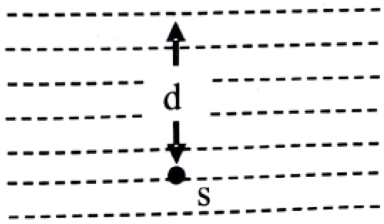
$$\frac{1}{-10} = \frac{1}{V} - \frac{1}{10}$$

$V = \infty$

Event – 3 $\frac{1}{20} = \frac{1}{V} - \frac{1}{\infty}$

V = +20

14. A point source S of light is placed at a depth d below the surface of water in a large and deep lake. Fraction of light that escapes in space above directly from water (refractive index = μ) surface is given by



(a) $\sqrt{1-\frac{1}{\mu^2}}$

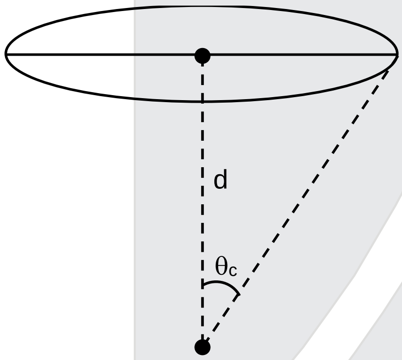
(b) $\frac{1}{2}\sqrt{1-\frac{1}{\mu^2}}$

(c) $\frac{1}{2}\left\{1-\sqrt{1-\frac{1}{\mu^2}}\right\}$

(d) depends on d and increases with increasing d.

Ans. **(c)**

Sol.



P = Power of light source

Energy escape per sec = $\frac{P}{2}[1 - \cos\theta_c]$

fraction of energy escape $= \dfrac{\frac{P}{2}[1-\cos\theta_c]}{P}$

$= \frac{1}{2}[1-\cos\theta_c]$

$\sin\theta_c = \frac{1}{\mu}$

$\cos\theta_c = \sqrt{1-\frac{1}{\mu^2}}$

fraction of energy escape $= \frac{1}{2}\left[1-\sqrt{1-\frac{1}{\mu^2}}\right]$

15. A convex lens is held 45 cm above the bottom of an empty tank. The image of a point object at bottom of tank is formed 36 cm above the lens. Now a liquid is poured into the tank upto a height of 40 cm above the bottom. It is found that distance of image of same point object at the bottom of the tank is 60 cm above the lens. Refractive index of liquids is :

(a) 1.33 (b) 1.37 (c) 1.40 (d) 1.60

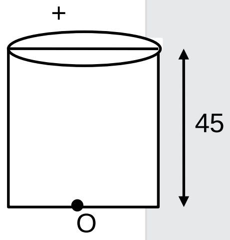
Ans. **(d)**

Sol. $\frac{1}{f} = \frac{1}{V} - \frac{1}{u}$

$\frac{1}{f} = \frac{1}{36} - \frac{1}{-45}$

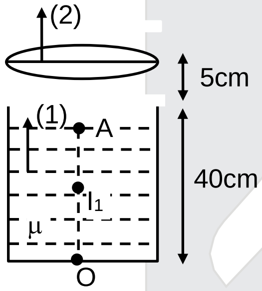
$\frac{1}{f} = \frac{1}{36} + \frac{1}{45}$

$f = \frac{36 \times 45}{81} \Rightarrow 20\text{cm}$



event (I) object = 0
image = I_1

$AI_1 = \frac{A_0}{\mu} = \frac{40}{\mu}$



event – 2 object $\Rightarrow I_1$
Image $= I_2$
V = + 60

$\frac{1}{f} = \frac{1}{V} - \frac{1}{\mu}$

$$\frac{1}{20} = \frac{1}{60} - \left(\frac{-1}{\left(5 + \frac{40}{\mu}\right)}\right)$$

$$\frac{1}{20} - \frac{1}{60} = \frac{1}{5 + \frac{40}{\mu}}$$

$$\frac{1}{30} = \frac{1}{5 + \frac{40}{\mu}}$$

$$30 = 5 + \frac{40}{\mu} \Rightarrow \mu = 1.60$$

16. A potential of 5V is applied across the faces of a pure germanium plate of area 2×10^{-4} m^2 and of thickness 1.2×10^{-3} m. Concentration of carriers in germanium at room temperature is 1.6×10^6 m^{-3}. Mobility of electrons and holes are 0.4 m^{2}V^{-1}s^{-1} and 0.2 m^{2}V^{-3}s^{-3} respectively. The current produced in germanium plate at room temperature, is :

(a) 1.28×10^{-13} (b) 1.28×10^{-9} A (c) 1.536×10^{-13}A (d) 6.4×10^{-10} A

Ans. **(a)**

Sol. $i_n = n_h eAV_d$

$i_e = n_e eAV_d$

$V_d = \mu E = \mu \frac{\Delta V}{d}$

where $\Delta V = 5$ volt

$d = 1.2 \times 10^{-3}$ m

$n_n = n_e = 1.6 \times 10^6$ m^{-3}

$I = An_n\mu_n Ee + n_e A\mu_e Ee$

$= AEe[n_n\mu_n + n_e\mu_e]$

$= 2 \times 10^{-4} \times \frac{\Delta V}{d}[1.6 \times 10^6 \times 0.2 + 1.6 \times 10^6 \times 0.4] \times 1.6 \times 10^{-19}$

$= \frac{2\times10^{-4}\times5}{1.2\times10^{-3}}[32\times10^4 + 64\times10^4]\times1.6\times10^{-19}$

$= \frac{10\times10^3}{1.2}[96]\times1.6\times10^{-19}$

$= 1.28 \times 10^{-13}$A

17. Fission of one nucleus of ^{235}U releases 200 MeV energy in average. Minimum amount of ^{235}U required to run 1000 MW reactor per year of continuous operation (assuming 30% efficiency) is

(a) 1280 ton (b) 1.28 ton (c) 1.1 ton (d) 1.1×10^5 ton

Ans. **(b)**

Let say amount of V = x gram

Number of Uranium atom $= \frac{x}{M}N_A$

$= \frac{x}{235}\times 6.023\times10^{23}$

Uranium give energy $= 200 \times 10^6 \times 1.6 \times 10^{-19}$

$= 3.2 \times 10^{-11}$ J

Amount of electrical energy in one year $= 1000 \times 10^6 \times 3600 \times 24 \times 365$

total energy $\times \frac{30}{100}$ = electrical energy

$\frac{x\times6.023\times10^{23}}{235} \times 3.2 \times 10^{-11} \times \frac{30}{100} = 10^9 \times 3600 \times 24 \times 365$

x = 1281711 gram

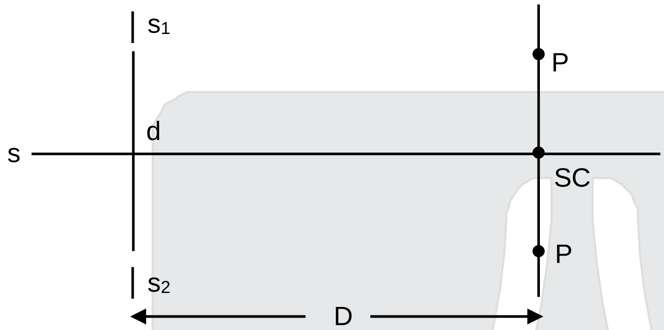
= 1.28 ton

18. In a young's double slit experiment distance between slits is d = 1 mm, Wavelength of light used is 600 nm and distance of screen from the plane of slits is D = 1m. The minimum distance between two points on the screen where intensity falls to 75% of maximum intensity will be (assume both sources of equal power)

(a) 0.1 mm (b) 0.2 mm (c) 0.45 mm (d) 0.9 mm

Ans. **(b)**

Sol.



Maximum intensity = $I_m = 4I_0$

Intensity at point P = 75% of $I_m = \frac{75}{100} \times 4I_0 = 3I_0$

$\Rightarrow I_0 + I_0 + 2\sqrt{I_0}\sqrt{I_0}\cos\phi = 3I_0$

$\Rightarrow \cos\phi = \frac{1}{2}$

$\Rightarrow \phi = 60°$

$= \frac{\pi}{3}, 2\pi - \frac{\pi}{3}, \frac{5\pi}{3}$

$\Rightarrow \phi = \frac{2\pi}{\lambda}\Delta x$

$\Delta x = \frac{\phi\lambda}{2\pi} = \frac{\pi\lambda}{3 \times 2\pi} = \frac{\lambda}{6}$

$\Rightarrow \Delta x = \frac{dx}{D} = \frac{\lambda}{6}$

$x = \frac{\lambda D}{6d}$

There is also another point below the screen centre which is at $\frac{\lambda D}{6d}$ from SC where intensity is 75 % of I_m

separation = $\frac{\lambda D}{6d} + \frac{\lambda D}{6d} = \frac{\lambda D}{3d}$

$= \frac{1}{3} \times \frac{600 \times 10^{-9} \times 1}{1 \times 10^{-3}}$

$= 200 \times 10^{-6}$ meter

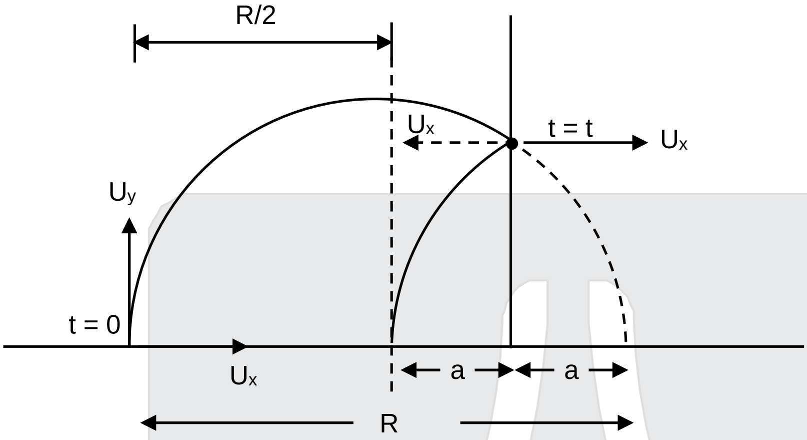
$= 200 \times 10^{-6} \times 10^{3}$ mm = 0.2 mm

19. A ball is projected from horizontal ground. It attains a maximum height H on its projectile path and there after strikes a stationary smooth vertical wall and falls on ground vertically below the point of maximum height. Assume the collision with wall to be perfectly elastic, the height of the point on the wall where the ball strikes is

(a) 3H/4 (b) 2H/3 (c) H/2 (d) 4H/5

Ans. **(a)**

Sol.



Maximum height = H = $\frac{U_y^2}{2g}$

$U_y = \sqrt{2gH}$

$\frac{R}{2} + a + a = R$

$\frac{R}{2} + 2a = R$

$R = 4a \qquad \therefore a = \frac{R}{4}$

$T = \frac{2U_y}{g}$

$\Rightarrow \qquad U_x t = \frac{R}{2} + a$

$U_x t = \frac{R}{2} + \frac{R}{4}$

$U_x t = \frac{3R}{4}$

$U_x t = \frac{3}{4} \times \frac{2U_xU_y}{g}$

$t = \frac{3}{2}\frac{U_y}{g}$

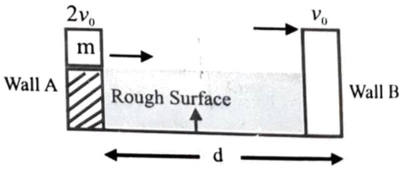
At this time t particle hit the wall

$\therefore \qquad h = U_y t - \frac{1}{2} gt^2$

$= U_y \times \frac{3}{2}\frac{U_y}{g} - \frac{1}{2} \times \frac{g \times 9U_y^2}{4g^2} = \frac{U_y^2}{g}\left[\frac{3}{2} - \frac{g}{8}\right]$

$= \frac{U_y^2}{g}\left[\frac{3}{8}\right] = \frac{2gH}{g}\left[\frac{3}{8}\right] = \frac{3H}{4}$

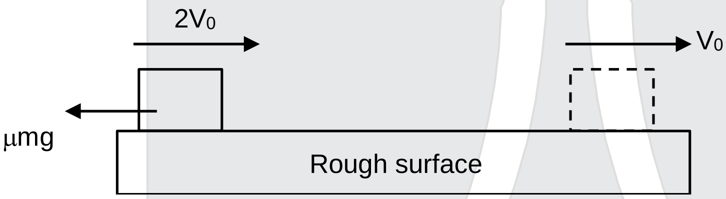
20. As shown in figure, a block of mass m is projected from wall A with velocity $2v_0$ on the rough surface with constant sliding friction to hit the wall B with velocity v_0. With what velocity same mass m should be projected to hit the wall B with same velocity v_0 if the surface is now moving upward with an acceleration of a = 4g



(a) $2v_0$ (b) $3v_0$ (c) $4v_0$ (d) $5v_0$

Ans. **(c)**

Sol.



WET :

$$-\mu mgd = = \frac{1}{2}mV_0^2 - \frac{1}{2}m(2V_0)^2$$

$$\mu mgd = \frac{3}{2}mV_0^2$$

N – mg = ma

N = mg + ma = mg + m4g = 5 mg

WET :

$$-\mu 5mgd = \frac{1}{2}mV_0^2 - \frac{1}{2}mV^2$$

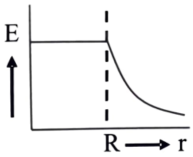
$$-5 \times \frac{3}{2}mV_0^2 = \frac{1}{2}mV_0^2 - \frac{1}{2}mV^2$$

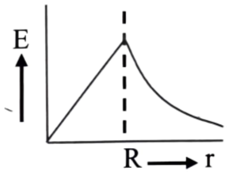
$$\frac{(-15-1)(mV_0^2)}{2} = -\frac{1}{2}mV^2$$

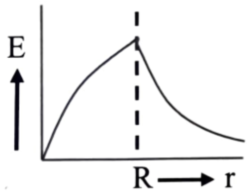
$$V^2 = 16\ V_0^2$$

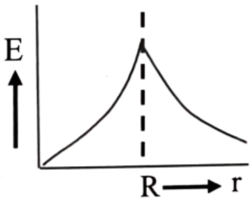
$$V = 4V_0$$

21. A sphere of radius R, is charged with volume charge density ρ such that $\rho \propto r$ (r is distance from centre). Variation of electric field E with r (for all values of r : $r \le R$ and $r > R$) is best represented by

(a) 

(b) 

(c) 

(d) 

Ans. **(d)**

Sol. $\rho \propto r$

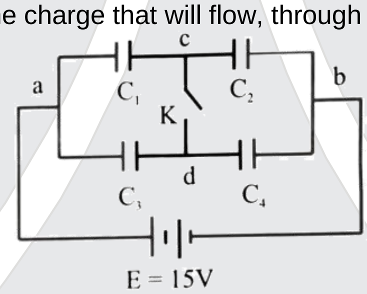
$\rho = kr$

for r < R $\quad E_{in} = \dfrac{k}{r^2}\displaystyle\int_0^2 k(r)4\pi r^2 dr$

$= \dfrac{k}{r^2} 4\pi k \dfrac{r^4}{4} \Rightarrow E_{in} \propto r^2$

$E_{out} \propto \dfrac{1}{r^2}$

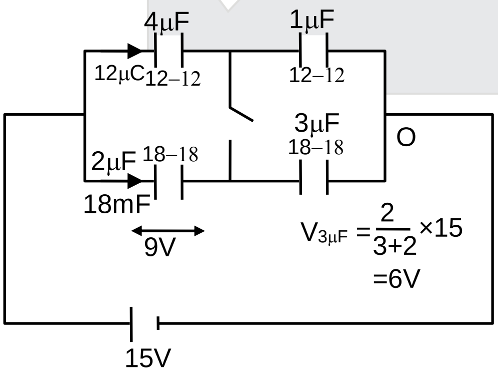
22. A system of capacitors $C_1 = 4\ \mu F$, $C_2 = 1\ \mu F$, $C_3 = 2\mu F$ and $C_4 = 3\mu F$ connected across a battery of emf E = 15 V is shown in figure. The charge that will flow, through the switch K, when it is closed, is

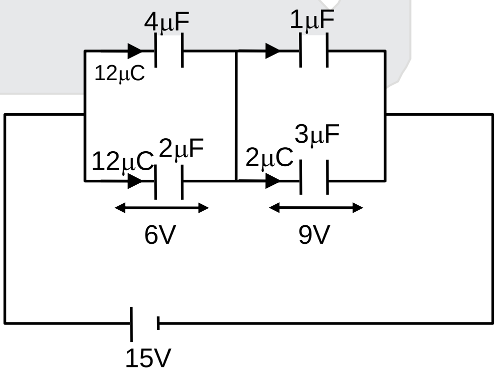


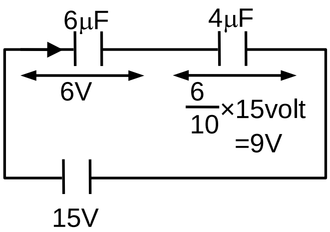
(a) 15 μC c to d (b) 12 μC c to d (c) 6 μC d to e (d) 9 μC d to c

Ans. **(a)**

Sol. $V_{imF} = \dfrac{4}{1+4} \times 15 = 12\text{volt}$



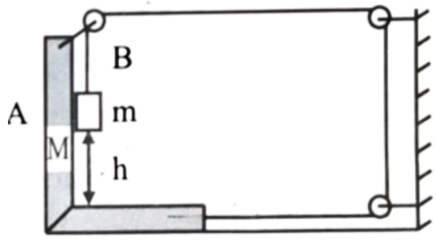




$\Delta Q_{switch} = 24 - 9$

$= 15\ \mu C$

23. A simplification of a kind of interlock is shown in figure. All surfaces are smooth and frictionless. The body m has a mass m = 1kg and the block M = 15 kg. The time 'm' takes to reach the base if it is released at height h = 4 meter above the base of M, is [use g = 10 ms^{-2}]



(a) 1 s (b) $\sqrt{3}$ s (c) 2s (d) $2\sqrt{2}$

Ans. **(c)**

Sol. 2T = 15a + 1(a) ......(1)

(1) g – T = (m) a_{rel} ....(2)

constraint

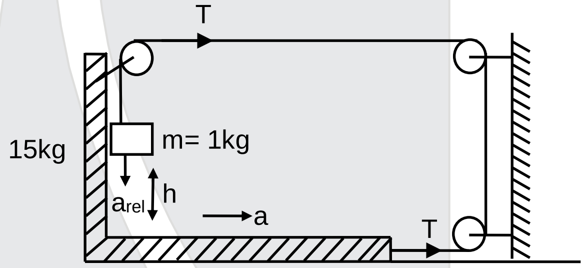
$-a - a + a_{rel} = 0$ ...... (3)

from (1)(2)(3)

1(g) – 8a = 1(2a)

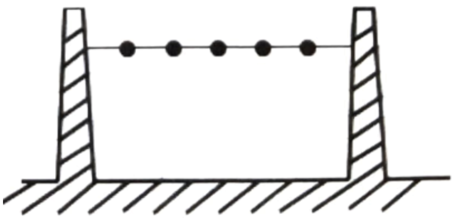
10a = g

a = 1



$S_{rel} = \frac{1}{2}(a_{rel.}) \times t^2 \Rightarrow 4 = \frac{1}{2} \times 2t^2 \Rightarrow t = 2$

24. A number n of identical balls, each of mass m and radius r, are stringed like beads at random and at rest along a smooth, rigid horizontal rod of length L, mounted between immovable supports, r/L is small but not negligible. Collision between balls, or between balls and supports, are perfectly elastic. One of the balls is struck horizontally so as to acquire a speed v, Resulting outward force felt by supports, averaged over a long time, is :



(a) $\frac{mv^2}{2(L-2nr)}$ (b) $\frac{mv^2}{(L-2nr)}$ (c) $\frac{2mv^2}{(L-2nr)}$ (d) $\frac{mv^2}{L}$

Ans. **(b)**

Sol. $\Delta P = 2mv$

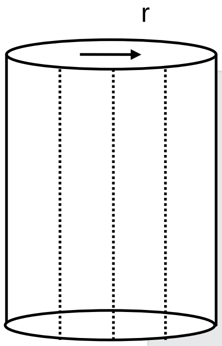
$\Delta t = \frac{2(L-2r.n)}{v} \Rightarrow f = \frac{\Delta p}{\Delta t} = \frac{mv^2}{L-2nr}$

25. The frequency of the transverse oscillations of a proton (mass M) trapped in a cylindrical relativistic electron beam of circular cross section of radius R and current I is given by {assume that speed v of relativistic electrons $\approx$ c (the speed of light in vacuum) and ignore magnetic effect])

(a) $\frac{1}{2\pi R}\sqrt{\frac{eI}{2\pi\varepsilon_e Mc}}$ (b) $\frac{1}{2\pi R}\sqrt{\frac{2\pi\varepsilon_e I}{Mc}}$ (c) $\frac{1}{R}\sqrt{\frac{2\pi\varepsilon_e Mc}{eI}}$ (d) $\frac{1}{2\pi\varepsilon_0}\sqrt{\frac{2\pi\varepsilon_e Mc}{eI}}$

Ans. **(a)**

Sol. F =eE



$$\lambda_{in} = \frac{\eta\pi r^2\lambda e}{\lambda} = n\pi r^2 e$$

$$I = neAV_D = ne\pi R^2 C$$

$$\frac{\lambda_{in}}{I} = \frac{r^2}{R^2 C}$$

$$F = e\left(\frac{2k\lambda_{in}}{r}\right)$$

$$F = e\frac{2}{4\pi\varepsilon_0}\left(\frac{Ir^2}{R^2 C}\right)\times\frac{1}{r} = \frac{eIr}{2\pi\varepsilon_0 R^2 C}$$

$$f = \frac{1}{T} = \frac{1}{2\pi}\sqrt{\frac{k}{M}} = \frac{1}{2\pi}\sqrt{\frac{eI}{2\pi\varepsilon_0 R^2 CM}}$$

$$F = \frac{1}{2\pi R}\sqrt{\frac{eI}{2\pi\varepsilon_0 CM}}$$

26. Current I flows through a long thin walled metallic cylinder of radius R with a thin longitudinal slit of width $\xi(\xi \ll R)$ running parallel to the axis of the cylinder. The magnetic induction B produced at any point on the axis of the cylinder is approximately :

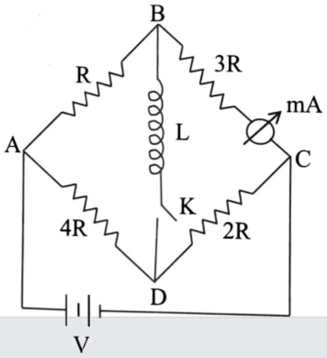
(a) B = zero (b) $B = \frac{\mu_0 I}{2\pi R^2}$ (c) $B = \frac{\mu_0 I\xi}{4\pi^2 R^2}$ (d) $B = \frac{\mu_0 I\xi}{2\pi R^2}$

Ans. **(c)**

Sol. $B = \frac{2R_m}{R}(di) = \frac{2Ib}{4\pi}\frac{1}{R}\cdot\frac{\ell}{2\pi R}\xi$

$= \frac{\mu_0 I\xi}{4\pi^2 R^2}$

27. The reading of the ammeter, used in the electrical network shown below, is 20 mA, as long time after the key K is closed.



The reading of the same ammeter, immediately after the key was closed was

(a) zero (b) 16 mA (c) 25 mA (d) 32 mA

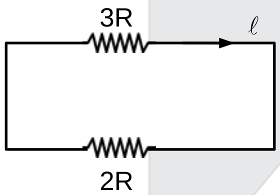
Ans. **(c)**

Sol. After long time

Req. $\dfrac{4R \times R}{5R} + \dfrac{3R \times 2R}{5R}$

= 2R

$I = \dfrac{V}{2R}$



$$e(\text{in } 3R) = \frac{\frac{V}{2R}.2R}{3R + 2R} = \frac{V}{5R}$$

$$\text{Just after } I = \frac{V}{4R} = \frac{V}{4}\left(\frac{V}{5R}\right) = \frac{5}{4} \times 20\text{mA}$$

= 25 mA

28. At the Earth's surface, a projectile is launched straight up at a speed of 10.0 km/s. Height to which it will rise is [g at surface of Earth = 9.8 ms^{-2} and radius of earth R = 6400 km]

(a) 1.63×10^3 km (b) 1.56×10^4 km (c) 2.52×10^4 km (d) 5.1×10^3 km

Ans. **(c)**

Sol. $$\frac{GMm}{R} + \frac{1}{2}mv^2 = -\frac{GMm}{R+h}$$

$$\Rightarrow GM\left(\frac{1}{R} - \frac{1}{R+h}\right) = \frac{v^2}{2}$$

= 2.52×10^4 km

29. A small sphere of mass 2.00g is released from rest in a large cylindrical vessel filled with oil. The resistive force due to viscosity of oil acting on sphere is proportional to tits velocity. Sphere approaches a terminal speed of 5.00 cm/s. The time it takes the sphere to reach 90.0% of it terminal speed is approximately.

(a) 3.22 ms (b) 5.10 m/s (c) 10.2 ms (d) 11.7 ms

Ans. **(d)**

Sol. $mg - B = 6\pi\eta r V_T$ .....(1)

$$\& \ a = \frac{dv}{dt} = \frac{(mg - B) - 6\pi\eta r V}{m}$$

$$\frac{dv}{dt} = \frac{6\pi\eta r}{m}(V_T - V)$$

$$= \frac{6\pi\eta r V_T}{m.V_T}(V_T - V)$$

$$= \frac{mg - B}{m.V_T}$$

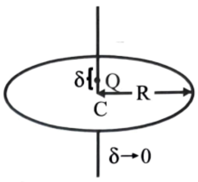
$$\approx \frac{mg}{m.V_T}(V_T - V)$$

$$\Rightarrow \frac{dv}{v_T - v} = \frac{g}{v_T}dt$$

$$v = v_T\left(1 - e^{\frac{-g}{v_T}}\right) = 0.9V_T$$

$$\Rightarrow t = \frac{v_T}{g}\log_e 10 = 11.5 \text{ ms}$$

30. A static point charge Q is located just above the centre C (δ-0) of a horizontal circle of radius R on its geometric axis, as shown in figure. The magnitude of electric flux through this circle is



(a) zero (b) $\frac{Q}{4\epsilon_0}$ (c) $\frac{Q}{2\epsilon_0}$ (d) $\frac{Q}{\epsilon_0}$

Ans. **(c)**

Sol. for $n = \delta \to O$

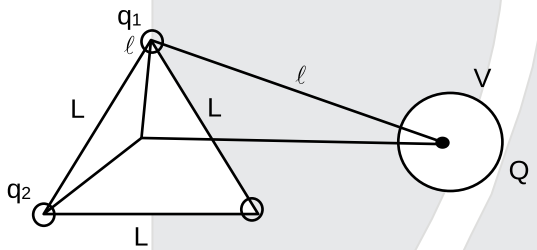
$$Q = \frac{q}{2\varepsilon_0}\left(1 - \frac{x}{x^2 + R^2}\right) = \frac{q}{2\varepsilon_0}$$

31. Three small identical neutral metal balls are at the vertices of an equilateral triangle. The balls are in turn touched to an isolated large charged conducting sphere whose centre is on a line perpendicular to the plane of triangle and passing through its centre. As a result the first and second balls have acquired charges q_1 and q_2 respectively. The charge acquired by the third ball is [Assume that charge and potential of large spherical conductor change insignificantly in charging of the balls and that charges on balls are spherically symmetric]

(a) $\frac{q_1^2}{q_2}$ (b) $\frac{q_2^2}{q_1}$ (c) $2q_2 - q_1$ (d) $q_3 = q_2 = q_1$

Ans. **(b)**

Sol. $\frac{kQ}{\ell} + \frac{kq_1}{r} = v$



$$\frac{kQ}{\ell} + \frac{kq_1}{L} + \frac{kq_2}{r} = v$$

$$\frac{kQ}{\ell} + \frac{kq_1}{L} + \frac{kq_2}{L} + \frac{kq_3}{r} = v$$

$$q_1\left(\frac{q_2}{L} + \frac{q_3}{r} - \frac{q_2}{r}\right) = 0$$

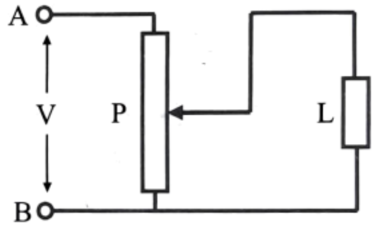
$$q_2\left(\frac{q_1}{L} + \frac{q_2}{r} - \frac{q_1}{r}\right) = 0$$

$$\frac{q_1q_3}{r} - \frac{q_2^2}{r} = 0$$

$$q_1q_3 = q_2^2$$

$$q_3 = \frac{q_2^2}{q_1}$$

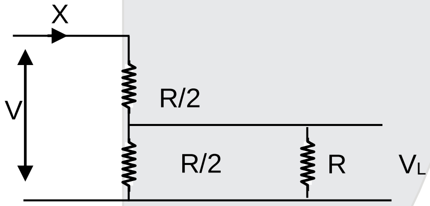
32. Voltage across the load L is controlled by using circuit as shown in figure. P is a potentiometer. Resistance R_L, of the load and R_P, of the potentiometer are equal to R. Load L is connected to the middle of potentiometer. Input voltage V is constant. If now R_L, is doubled, the voltage across load will change by a factor



(a) $\frac{5}{4}$ (b) $\frac{7}{5}$ (c) $\frac{8}{9}$ (d) $\frac{10}{9}$

Ans. **(d)**

Sol. case-1

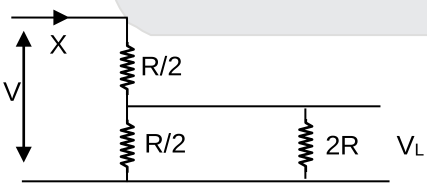


$$\frac{R}{2}x + \frac{R.\frac{R}{2}}{R+\frac{R}{2}}x = V$$

$$\Rightarrow x = \frac{6V}{5R}$$

$$\Rightarrow (\Delta V)_2 = x . \frac{R.\frac{R}{2}}{3\frac{R}{2}} = \frac{2v}{5}$$

case-2



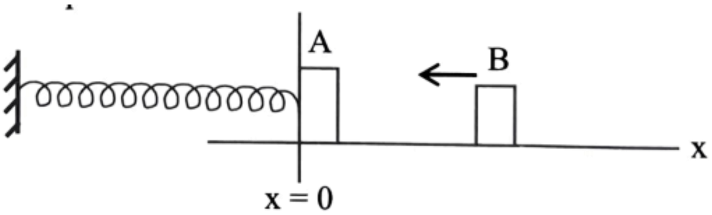
$$\frac{R}{2}x + \frac{\frac{R}{2}.2R}{\frac{5R}{2}}x = V$$

$$x = \frac{10V}{9R}$$

$$\Delta V_2^1 = \frac{2R}{5} . x = \frac{4}{9}V$$

$$\frac{\Delta V_2^1}{\Delta V_2} = \frac{4/9}{4/5} = \frac{10}{9}$$

33. A small block A of mass 2 kg is attached to a spring of force constant 1200 Nm^{-1}, and rests on a smooth horizontal surface at x = 0 as shown in figure. A second block B of mass 1 kg slides along the surface towards A at 6 m/s and sticks to it. Assuming that the collision occurs at t = 0, position x (in meter) of block A as a function of time t is expressed as



(a) x = 0.173 cos 20t (b) x = 0.1 cos 40 Tt (c) $x = -0.173 \sin \frac{\pi}{10} t$ (d) x = – 0.1 sin 20t

Ans. **(d)**

Sol. 1(6) = (2+1)V

V = 2m/s

$\frac{1}{2}1200\,A^2 = \frac{1}{2}(3)2^2$

$A^2 = \frac{1}{100}$

A = 0.1

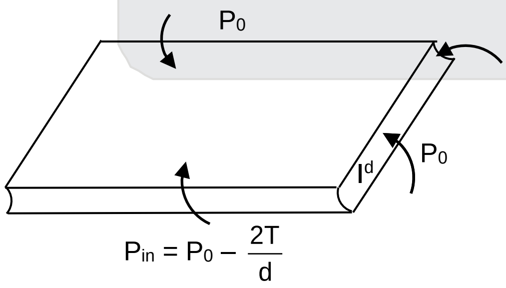
$\omega = \sqrt{\frac{k}{m}} = \sqrt{\frac{1200}{3}} = 20 = 0.1 \sin(20t + \pi) = -0.1 \sin 20\,t$

34. Two plane glass testing slides each of surface area A are stuck with each other by a small water drop squeezed between them as an extremely thin film of thickness d. If the surface tension of water be T and the angle of contact be zero, then the force required to pull apart the two glass plates will be

(a) $\frac{8TA}{d}$ (b) $\frac{4TA}{d}$ (c) $\frac{2TA}{d}$ (d) $\frac{TA}{d}$

Ans. **(c)**

Sol.



Shape is 4 linotcal

so $OP = \frac{T}{R}$

$OP = P_0 = \frac{2T}{d}$

$F = OPA = \frac{2TA}{d}$

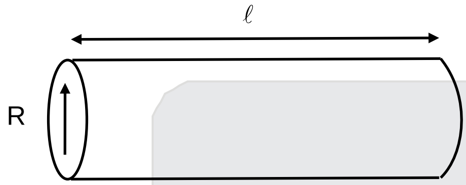
$F = \frac{2TA}{d}$

35. The rate of flow of a certain liquid of viscosity η through a horizontal capillary of length ℓ and radius r is Q when the pressure head at the inlet is just twice the atmospheric pressure. The rate of flow of the same liquid through another capillary of length 2ℓ and radius 2r when the inlet pressure head is 4 times the atmospheric pressure will be (The outlet being open to atmosphere in each case)

(a) 24 Q (b) 16Q (c) 8Q (d) 4Q

Ans. **(a)**

Sol. $Q = \dfrac{\pi R^4 \sigma P}{8\eta\ell}$



$$Q = \frac{\pi r^4 (2P_0 - P_0)}{8\eta\ell}$$

$$Q^1 = \frac{\pi (2r)^4 (4P_0 - P_0)}{8\eta(2\ell)}$$

$$\frac{Q^1}{Q} = \frac{16 \times 3}{2} = 8 \times 3 = 24$$

$Q^1 = 24Q$

Ans. (a)

36. A uniform rod of the material of Young's modulus Y is pushed over a smooth horizontal surface by a constant horizontal force F. The area of cross-section of the rod is A. The compressional strain in the rod is

(a) $\dfrac{F}{AY}$ (b) $\dfrac{F}{2AY}$ (c) $\dfrac{3F}{2AY}$ (d) $\dfrac{2F}{AY}$

Ans. **(b)**

Sol.

$$\frac{\Delta\ell}{\ell/2} = \frac{F}{AY}$$

$$\frac{\Delta\ell}{\ell} = \frac{F}{2AY}$$

37. A total charge Q is uniformly distributed over a non-conducting ring of radius r. There is time varying magnetic field perpendicular to its plane and changing at the uniform rate of $\dfrac{dB}{dt}$. The magnitude of induced tangential electric field E on the ring is

(a) $r\dfrac{dB}{dt}$ (b) $r^2\dfrac{dB}{dt}$ (c) $\dfrac{1}{2}r\dfrac{dB}{dt}$ (d) $\dfrac{1}{2}r^2\dfrac{dB}{dt}$

Ans. **(c)**

Sol $E.2\pi r = \pi r^2\, dB/dt$

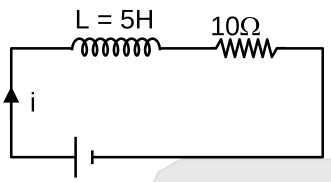
$$E = \frac{r}{2}\frac{dB}{dt}$$

38. DC emf of 15 V is applied to a circuit containing 5 H inductance and 10Ω resistance in series at t = 0. The ratio of the currents in the circuit at t = 0.5 sec and at t = 1.0 sec is

(a) $\frac{e^2}{e^2-1}$ (b) $\frac{\sqrt{e}}{\sqrt{e}-1}$ (c) $\frac{e}{e+1}$ (d) $\frac{1}{e}$

Ans. **(c)**

Sol.



$$i = \frac{E}{r}(1 - e^{-\frac{Rt}{L}})$$

$$= \frac{15}{10}\left[1 - e^{-\frac{10}{5}\times t}\right]$$

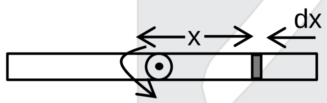
$$= \frac{1.5(1 - e^{-2(0.5)})}{1.5(1 - e^{-2})} = \frac{1 - e^{-1}}{1 - e^{-2}} = \frac{e}{e+1}$$

39. An insulating rod of length ℓ carries a charge q distributed uniformly all over its length. The rod is pivoted at its midpoint and is rotated at a frequency f(in Hz) about an axis perpendicular to the rod passing through the point at the pivot. The magnetic moment of the system is

(a) $\frac{1}{12}\pi q f \ell^2$ (b) $\frac{1}{6}\pi q f \ell^2$ (c) $\frac{1}{3}\pi q f \ell^2$ (d) $\pi q f \ell^2$

Ans. **(a)**

Sol.



$$M = \int_0^{\ell/2} \frac{\omega}{2\pi} \times (2\lambda dx)\pi x^2$$

$$M = \frac{\omega 2\pi}{2\pi} \times \left(\frac{q}{\ell}\right)\left[\frac{(\ell/2)^3}{3}\right]$$

$$M = \frac{\omega q \ell^2}{8 \times 3}$$

$$M = \frac{f q \ell^2}{12}$$

40. A circular loop of radius r is placed inside another circular loop of radius R (R>>r). The loops are coplanar and concentric. The mutual inductance (M) of the system is proportional to

(a) $\frac{r}{R}$ (b) $\frac{r^2}{R}$ (c) $\frac{R^2}{r}$ (d) $\frac{r^2}{R^2}$

Ans. **(b)**

Sol. $M = \left(\frac{\mu_0 I}{2R}\right)\frac{\pi r^2}{I}$; $M \propto \frac{r^2}{R}$

41. The amplitude of the electric and magnetic fields associated with a beam of light of intensity 477.9 W/m^2 are, respectively,

(a) 6x 10^2V/m and 2 × 10^{-6} T
(b) 3 × 10^2 V /m and 1 × 10^{-6}T
(c) 12 × 10^2 V /m and 4 × 10^{-6} T
(d) 9 × 10^2 V /m and 3 × 10^{-6} T

Ans. **(a)**

Sol. $\frac{dU}{dv} = \frac{I}{C}$

$\frac{1}{2}\varepsilon_0 E_0^2 = \frac{477.9}{C}$

$E_0 = \sqrt{\frac{2\times 477.9}{\varepsilon_0 \times 3\times 10^8}} = \sqrt{\frac{2\times 477.9\times 4\pi\times 9\times 10^9\times 10}{3\times 10^8}} = \sqrt{2\times 477.9\times 4\pi\times 30}$

E_0 = 600.12

$B_0 = \frac{E_0}{C} = \frac{600}{3\times 10^8}$ = 2 × 10^{-6}

42. Given that the critical angle of incidence for total internal reflection within a transparent material when placed in air is 45°. The Brewster's angle of incidence for light propagating from air to the transparent material will be

(a) 54. 74°
(b) 35 .26°
(c) 25. 26°
(d) 44.74°

Ans. **(a)**

Sol. r = tan θ_c

$\sqrt{2} = \tan\theta_c$

$\theta_C = \tan^{-1}\sqrt{2}$

= 54.74°

43. A parrticle moves along a straight line. Its displacement S varies with time t according to the law $S^2 = at^2 + 2bt + c$ (a, b and c are constants) The acceleration of this particle varies as

(a) S^0
(b) S^{-1}
(c) S^{-2}
(d) S^{-3}

Ans. **(d)**

Sol. $s^2 = at^2 + 2bt + c$

$s = \sqrt{at^2 + 2bt + c}$

$v = \frac{ds}{dt}$

$v = \frac{1}{2}(at^2 + 2bt + c)^{\frac{1}{2}-1}$ × (2at + 2b)

$v = \frac{2at + 2b}{2s}$

acceleration = $\frac{dv}{dt} = \frac{1}{2}\left[\frac{2a}{s^2} + \frac{2at + 2b(-1)}{s^2}\frac{ds}{dt}\right]$

acceleration = $\frac{1}{2}\left[\frac{2a}{s^2} - \frac{2at + 2b)\times(2at + 2b)}{2s}\right]$

$= \left[\frac{a}{s} - \frac{(at+b)^2}{s^3}\right] = \left[\frac{as^2 - (at+b)^2}{s^3}\right] = \frac{a[at^2 + 2bt + c] - [a^2 + t^2 + b^2 + 2abt]}{s^3}$

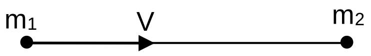
acceleration $\frac{ac - b^2}{s^3}$; acceleration α s^{-3}

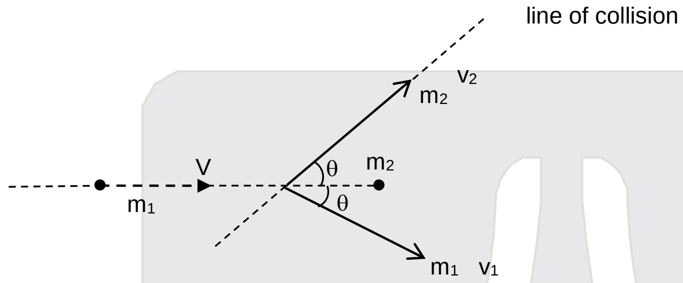
44. A ball a (mass m_1) moving with velocity V experiences an elastic collision with another stationary ball B (mass m_2). Each ball flies apart symmetrically relative to the initial direction of motion of ball A. at an angle θ. Ratio of the masses of balls $\frac{m_1}{m_2}$ is

(a) $1 + 2\cos\theta$ (b) $2\cos 2\theta$ (c) $1 + 2\cos 2\theta$ (d) $1 + \cos 2\theta$

Ans. **(c)**

Sol.





$p_i = p_f$ in perpendicular direction

$0 = m_2 v_2 \text{ sn } \theta - m_1 v_1 \text{ sn } \theta$ .....(1)

$m_2 v_2 = m_1 v_1$

$p_i = p_f$ in horigantal direction

$m_1 v = m_2 v_2 \cos\theta + m_1 v_1 \cos\theta$

$m_1 v = m_1 v_1 \cos\theta \times 2$

$\therefore v_1 = \dfrac{v}{2\cos\theta}$

$e = 1$

$$-\left|\frac{v_2 - v_1\cos2\theta}{0 - v\cos\theta}\right| = 1$$

$v_2 - v_1 \cos 2\theta = v\cos\theta$

$v_2 = v\cos\theta + \cos 2\theta \times \dfrac{v}{2\cos\theta}$

$$\frac{m_1}{m_2} = \frac{v^2}{v^1} = \frac{v\cos\theta + \cos 2\theta \times \frac{v}{2\cos\theta}}{\frac{v}{2\cos\theta}}$$

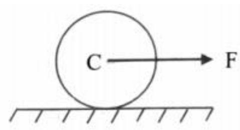
$= 2\cos^2\theta + \cos\theta$

$\cos 2\theta = 2\cos^2\theta - 1$

$2\cos^2\theta = 1 + 2\cos 2\theta$

$\therefore \dfrac{m_1}{m_2} = 1 + \cos\theta + \cos 2\theta = 1 + 2\cos 2\theta$

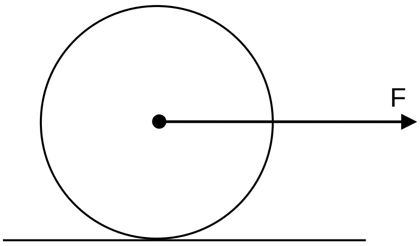
45. A solid cylinder of mass m is rolling without slipping on a rough horizontal surface, under the action of a horizontal force F such that the line of action of F passes through centre C of the cylinder. Choose the correct alternative



(a) acceleration of centre of cylinder is F/m
(b) Frictional force on cylinder acts forward
(c) Magnitude of friction force is F/3
(d) None of the above

Ans. **(c)**

Sol.



$\tau_0 = I_0\,\alpha$

$$FR = \left(\frac{mR^2}{2} + mR^2\right)\alpha$$

$$\alpha = \frac{2F}{3mR}$$

$a = \alpha R$

$$a = \frac{2F}{3m}$$

$F - f_s = ma$

$f_s = F - ma$

$$\Rightarrow f_s = F - \frac{m2f}{3m} \Rightarrow \frac{F}{3}$$

46. A motor pump is used to deliver water at a certain rate r from a given pipe. To obtain thrice as much water from the same pipe in the same time, the power of the motor has to be increased to

(a) 3 times (b) 9 times (c) 27 times (d) 81 times

Ans. **(3)**

Sol. $\frac{dm}{dt} = Avp = r$

worh done by pump per unit time = $\frac{d}{dt}\left(\frac{1}{2}mv^2\right)$

$$= \frac{1}{2}\frac{dm}{dt}v^2 = \frac{1}{2}avp \times v^2 = \frac{Av^3p}{2}$$

pome of pump = $\frac{Av^3p}{2}$

$$= \frac{Ap}{2}\left(\frac{r}{Ap}\right)^3 = \frac{r^3}{2A^2p^2}$$

as power α r^3

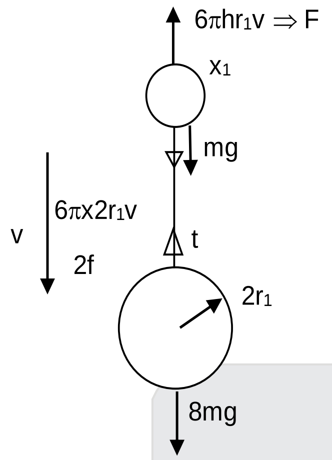
so when r in made three times needed power become 3^3 times in 27 times

47. Two small solid balls of masses m and 8 m made up of same material are tied at the two ends of a thin weightless thread. They are dropped from a balloon in air. The tension T of thread during fall, after the motion of balls has reached steady state is

(a) 2 mg (b) 3.5 mg (c) 4.5 mg (d) zero

Ans. **(a)**

Sol.



$m = \frac{4}{3}\pi r^3 \rho$

$\frac{m}{8m} = \left(\frac{r_1}{r_2}\right)^3$

$\therefore \frac{r_1}{r_2} = \frac{1}{2}$

$r_2 = 2r_1$

At steady stale

$f_{net} = 0$

$8mg + mg - 2f - f = 0$

$9\ mg = 3f$

$f = 3mg$

NLM equation of 8 m ball

$T + 2f - 8mg = 0$

$T + 2 \times 3\ mg - 8mg = 0$

$T = 2\ mg$

48. Obtain the value of $\frac{e^2}{2 \in_0 hc}$

(a) 0.0073 (b) 0.0073 m (c) 0.073 s^{-1} (d) 0.0346 m^{-1}

Ans. **(a)**

Sol. Put

$C = 3 \times 10^8$

$e = 1.6 \times 10^{-19}$

$\varepsilon_0 = 8.85 \times 10^{-12}$

$h = 6.6 \times 10^{-34}$

Get the ans = 0.0073

PART-A2

ANY NUMBER OF OPTIONS 4, 3, 2 or 1 MAY BE CORRECT

MARKS WILL BE AWARDED ONLY IF ALL CORRECT OPTIONS ARE BUBBLED.

49. A hydrogen atom is in ground state (n = 1). The magnetic field produced by revolving electron, at centre of atom is B_0 Atom is excited to state n = 4, According to Bohr model, the correct alternatives is/are

(a) magnetic field at centre of atom for (n = 4) becomes $B_A = \frac{B_0}{64}$

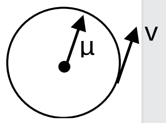
(b) Energy absorbed by atom in going from (n = 1) to (n = 4) is 12.75 eV

(c) Change in magnitude of angular momentum of electron is $\frac{3h}{2\pi}$

(d) Assume that this excited atom (n = 4) is at rest and it makes transition to ground state (n = 1) in a single quantum jump of an electron, (Take mass of atom $M_H = 1.67 \times 10^{-27}$) kg) the recoil speed of atom will be nearly $v = 4.1\ ms^{-1}$

Ans. **(b,c,d)**

Sol.



$$B = \frac{\mu_0 I}{2\pi r} = \frac{\mu_0}{2\pi r}\frac{e}{T} = \frac{\mu_0}{2\pi r}\cdot\frac{eV}{2\pi r}$$

$r \propto n^2$

$v = \frac{1}{n}$

$B \propto \frac{1}{n^5}$

so when n change from n = 1 to n = 4

B at centre = $\frac{B_0}{4^5}$

option (a) is wrong

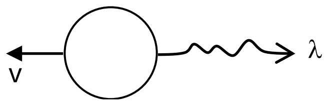
Energy absorbed $E_4 - E_1$

$$= 13.6\left[\frac{1}{1^2} - \frac{1}{4^2}\right] = 12.75 \text{ ev}$$

option (b) is correct

change in angular momentum = $\frac{4h}{2\pi} - \frac{h}{2\pi} = \frac{3h}{2\pi}$

option (c) is correct



$mv = \frac{h}{\lambda}$

$v = \frac{h}{m\lambda}$

$$v = \frac{6.67\times 10}{1.67\times 10^{-27}\lambda} \Rightarrow 12.75 = \frac{12400}{\lambda}$$

$\lambda = 972.5 \times 10^{-10}$ m

$$v = \frac{6.67\times 10^{-34}}{1.67\times 10^{-27}\times 972.5\times 10^{-10}} = 4.1 \text{ m/s}$$

50. In an experimental set up to study the photoelectric effect a point source of light of power 3.2 mW is used. The source emits mono energetic photons of energy 5eV and is located at a distance d = 0.8 mm from centre of a stationary metallic sphere of work function W = 3.0 eV. The radius of the sphere is R = 8. Assume that the sphere is isolated and photo electrons are instantly away after emission. Also assume that the efficiency of photoelectric emission is one for every 10^6 photons. In the present set up

(a) The de Broglie wave length of fastest moving photoelectron is nearly 8.7A°

(b) It is observed that after some time emission of photoelectrons from the surface of metakl sphere is stopped, the charge on sphere just when the electron emission stops is 64 $\pi\epsilon_0 \times 10^{-3}$C

(c) Time after which photo electric emission stops is nearly 111s

(d) The light source emits 4×10^{15} photons per sec

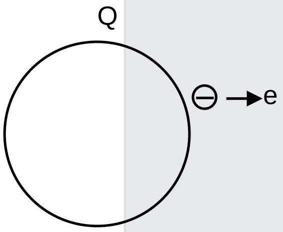
Ans. **(a,b,c,d)**

Sol. **(A)** $\lambda = \dfrac{h}{\sqrt{2m(KE)}} = \dfrac{h}{\sqrt{2m(hf-w)}} = \dfrac{h}{\sqrt{2m(2ev)}}$

$$\lambda = \frac{6.625\times10^{-34}}{\sqrt{4\times9\times10^{-31}\times1.6\times10^{-19}}} = \frac{6.625\times10^{-34}}{2\times3\times4\times10^{-26}\sqrt{10}}$$

$$\lambda = \frac{6.625\times10^{-8}}{24\times3.162} = 0.087\times10^{-8} = 8.7\ \text{Å}$$

(B)



$K_\ell + V_\ell = K_f + V_f$

$$KE_{max} + \frac{KQ}{R}(-e) = O + O$$

$$Q = \frac{(KE_{max})R}{Ke}$$

$$Q = \frac{(2e)\times8\times10^{-3}}{e}(4\pi\varepsilon_0)$$

$Q = 64\pi\varepsilon_0 \times 10^{-3}$C

(C) $\eta_e = \left(\dfrac{P}{4\pi d^2}\right)\dfrac{(\pi R^2)}{E}\times\dfrac{1}{10^6} = \dfrac{3.2\times10^{-3}\times(8\times10^{-3})^2}{4(0.8)^2\times5e\times10^6}$

$e(\eta_e t) = Q$

$$t\left(\frac{8\times10^{-8}}{5\times10^6}\right) = 64\pi\varepsilon_0\times10^{-3} \qquad \frac{3.2\times10^{-3}\times(8\times10^{-3})^2}{4\times(0.8)^2 5e\times10^6}$$

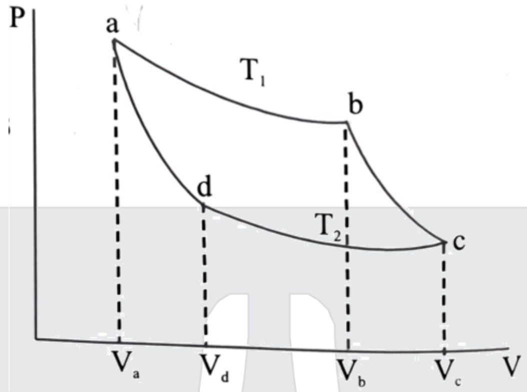
$$t = \frac{1000}{9} = 111\ \text{sec}$$

(D) $n_e = \dfrac{3.2\times10^{-3}}{5\times1.6\times10^{-19}} = \dfrac{2}{5}\times10^{16}$

$= 4 \times 10^{15}$ photon/sec

So, (D) is correct.

51. Two identical Carnot (cycles) engines opterate between maximum and minimum temperatures T_1 and T_2 and volume limits V_a, V_b, V_c & V_4 as shown in figure, Given that $\frac{V_e}{V_a} = e^3$ and $\frac{T_1}{T_2} = e$ (e is the base of natural logarithm). Engine 1 operates on mono atomic gas while the engine 2 on diatomic gas. Choose correct alternatives.



(a) Ratio of volumes $\frac{V_{b.1}}{V_{b.2}} = e$

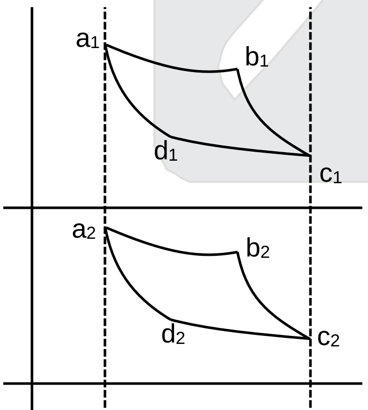
(b) Ratio of work done per cycle of the two is $\frac{W_1}{W_2} = 3$

(c) Ratio of work per cycle for the two is $\frac{W_1}{W_2} = 1$

(d) Ratio of efficiencies (η) of two engines $\frac{\eta_1}{\eta_2} = 1$

Ans. **(a,b,d)**

Sol.



$V_a = V_0$ $\qquad$ $V_c = e^3V_0$

$T_1V_0^{r-1} = T_2V_d^{r-1}$ $\qquad$ $T_1V_0^{r-1} = T_2(e^3V_0)^{r-1}$

$V_d = \left(\frac{T_1}{T_2}V_0^{(r-1)}\right)^{\frac{1}{r-1}}$ $\qquad$ $V_b = \left(\frac{T_2}{T_1}(e^3V_0)^{r-1}\right)^{\frac{1}{r-1}}$

$V_d = e^{\frac{1}{r-1}}V_0$ $\qquad$ $V_b = \left(\frac{1}{e}\right)^{\frac{f}{2}}e^3V_0$

$V_d = e^{f/2}V_0$ $\qquad$ $V_b = e^{(3-f/2)}V_0$

For monoatomic $\qquad$ $V_{b1} = e^{3/2}V_0$

For diatomic $\qquad$ $V_{b2} = e^{1/2}V_0$

$\frac{V_{b1}}{V_{b2}} = e$ so, (a) is correct

(b) $W_{net} = Q_{net} = nRTln\left(\frac{V_b}{V_a}\right) + nRT_2\ell n\left(\frac{V_d}{V_c}\right)$

as $\left(\frac{V_b}{V_a}\right) = \left(\frac{V_c}{V_d}\right)$

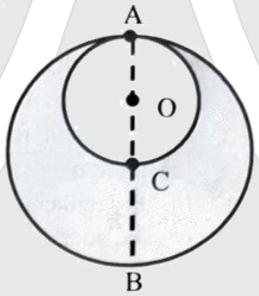
$W_{net} = nR(T_1 - T_2)\ ln(V_b/V_a)$

$$\frac{W_1}{W_2} = \frac{\ell n\left(\frac{V_{b1}}{V_a}\right)}{\ell n\left(\frac{V_{br}}{V_a}\right)} = \frac{\ell n(e^{3/2})}{\ell n(e^{1/2})} = \frac{\frac{3}{2}}{\frac{1}{2}} = 3$$

(d) $h = 1 - \frac{T_2}{T_1}$ same for both

So, (d) is correct.

52. In an isolated asteroid of radius R and uniform density ρ.a spherical cavity of diameter AC = R is excavated, where C is centre of asteroid. Choose correct alternative (s)



(a) A ball just dropped from A will strike C with speed $v = 2R\sqrt{\frac{\pi\rho G}{3}}$

(b) A ball dropped from A will reach C after time $t = \sqrt{\frac{3}{\pi\rho G}}$

(c) Acceleration of ball dropped from A varics as its distance from O (centre of cavity)

(d) Wight of a body placed at B (diametrically opposite to A) on surface of asteroid decreases by a factor $\frac{7}{8}$ due to excavation of cavity.

Ans. **(a,b)**

Sol. (a) $\frac{\rho R/2}{3\varepsilon_0} = \frac{4\pi G\rho}{3}\frac{R}{2}$

$\frac{1}{2}mv^2 = mE.R$

$\frac{1}{2}mv^2 = \frac{m4GpG\,\rho}{3}\frac{R}{2}.R$

$v = 2R\sqrt{\frac{\pi\rho G}{3}}$

(b) $R = \frac{1}{2}at^2$

$$R = \frac{1}{2}\left(\frac{4\pi G\rho R}{6}\right).t^2$$

$$t = \sqrt{\frac{3}{\pi G\rho}}$$

(c) out

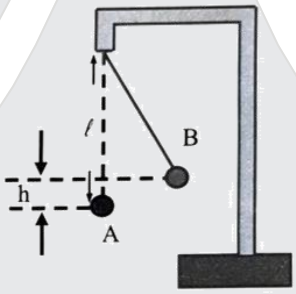
(d) $\frac{GMM}{R^2} = W_1$

& $W_2 = \frac{GMm}{R^2} - \frac{GM'M}{\left(\frac{3R}{2}\right)^2}$

here $M' = \frac{M}{\frac{4}{3}\pi R^3}.\frac{4}{3}\pi\left(\frac{R}{2}\right)^3 = \frac{M}{8}$

$W_2 = \frac{GMm}{R^2} - \frac{GMm}{8\times\frac{9}{4}R^2} = \frac{17}{18}\frac{GMm}{R^2}$

53. A small positively charged ball of mass m is suspended by a long insulating thread of negligible mass. Other positively charged small ball is moved very slowly from a large distance (along horizontal direction) until it is at orginal position A of first ball. As a result the first ball rises by h to position B such that h << ℓ. Choose the correct statement (s)



(a) Electrostatic energy of system of charges is 2 mgh.
(b) Total work done on system to bring two balls in their final position is mgh.
(c) Total work done on the system to bring two balls in their final position is 3 mgh.
(d) Work done on system to bring two balls in their final position does not depend on the magnitude of charges explicitly.

Ans. (a,c,d)

54. A rope of mass m and length L is suspended vertically. A mass M is suspended from bottom of the rope. A transverse wave is produced on the rope, which travels the length of rope in time t choose the correct statement (s)

(a) $t = 2\sqrt{\frac{L}{mg}}\left(\sqrt{M+m} - \sqrt{M}\right)$

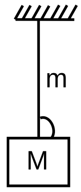
(b) For m << M The time $t = \sqrt{\frac{mL}{Mg}}$

(c) For M = 0 (i.e. no mass hanging) the time $t = \sqrt{\frac{L}{g}}$

(d) Time to travel the lower half of the rope by the wave is less than that to travel the upper half.

Ans. (a,b)

Sol. (a) $V = \frac{T}{\mu}$



$$V = \sqrt{\frac{Mg + \mu xg}{\mu}}$$

$$a = \frac{vdv}{dx} = \frac{g}{2}$$

$$V = \mu + at$$

$$t = \frac{v-\mu}{g/2} = \frac{2}{g}(v-\mu)$$

$$t = \frac{2}{g}\left[\sqrt{\frac{mg+mg}{\mu}} - \sqrt{\frac{Mg}{\mu}}\right]$$

$$= \frac{2\sqrt{g}}{g\sqrt{\mu}}\left[\sqrt{(M+m)} - \sqrt{M}\right]$$

$$= 2\sqrt{\frac{L}{mg}}\left[\sqrt{M+m} - \sqrt{M}\right]$$

(b) $V = \sqrt{\frac{I}{\mu}}$

m<< M

L = vt

$$t = \frac{L}{V} \quad = L\sqrt{\frac{M}{T}} \quad = L\sqrt{\frac{m}{LMg}} = \sqrt{\frac{mL}{Mg}}$$

(c) M = 0

$$V = \sqrt{\frac{T}{\mu}} = \sqrt{\frac{\mu xg}{\mu}} = \sqrt{gx}$$

$$V^2 = gx$$

$$2V = \frac{dv}{dx} = g$$

$$2V = \frac{dv}{d\lambda} = g/2$$

$$L = \frac{1}{2}at^2$$

$$t = \sqrt{\frac{2L}{q}} = \sqrt{\frac{2Lx_2}{g}} = 2\sqrt{\frac{L}{g}}$$

(d) $V = \sqrt{\frac{T}{M}}$

tension in upper half is more

∴ Velocity of upper half is more

$t_{\text{upper half}} < t_{\text{lower half}}$

55. A long solenoid having 1000 turns per meter camies a current of 1 A. It has a soft iron core of μ_r = 1000. The core is heated beyond the Curie temperature (T_c). Then

(a) The H field in the solenoid is nearly uchanged but the B field decreases drastically.
(b) The H and B fields in the solenoid are nearly unchanged.
(c) The magnetization in the core reverses direction
(d) The magnetization in the core diminishes by a factor of about 10^8

Ans. **(a)**

Sol. n = 1000 turns/m, H = nI

I = 1A

μ_r 1000 B = $\mu_0\mu_r$H

H = nI

$x = \dfrac{C}{T - T_C}$ $x + 1 = \mu r$

I = xH   H = nI

As x & I x main same

H x main same

bot μr = 1000 to μr = 1

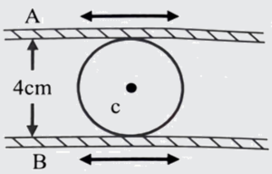
so B changes

& magnetization red vees by

factor of 10^3

correct Answer is (A)

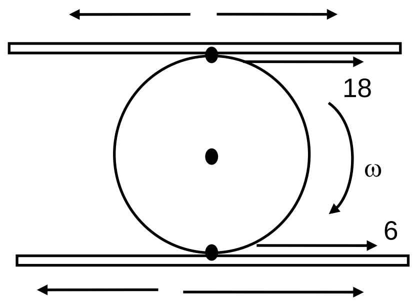
56. In a certain machine two steel paltes are spearated by a hardened steel cylindrical roller (see fig). In operation, the plates move back and forth horizontally, perpendicular to the axis of roller, and the roller rolls freely between plates without slipping on either one . At a particular instant plate A is moving with a speed of 18 cm sec^{-1} to the right and an acceleration of 30 cm sec^{-2} to the left, and the plate B is moving with a speed of 6 cm sec^{-1} to the right and an acceleration of 8 cm sec^{-2} to the left. At that instant, for the roller



(a) Its angular speed is 3 rad sec^{-1} clockwise
(b) Its angular acceleration is 6 rad sec^{-2} clockwise
(c) The liner speed of its axis is 12 cm sec^{-1} towards right
(d) The linear acceleration of its axis is 20 cm sec^{-2} towards left

Ans. **(a,c)**

Sol.



$\omega = \frac{18-6}{2r} = \frac{12}{2r} = \frac{6}{r} = \frac{6}{2} = 3$ rad/s

option (a) is correct

$\propto = \frac{30-8}{2r} = \frac{2r}{2r} = \frac{11}{r} = \frac{11}{2} \Rightarrow 6.5$ rad/s^2

Option (b) is incorrect

$V_C = \omega r + 6$

$3 \times 3 + 6$

$\Rightarrow$ 12 cm/s

option (c) is correct

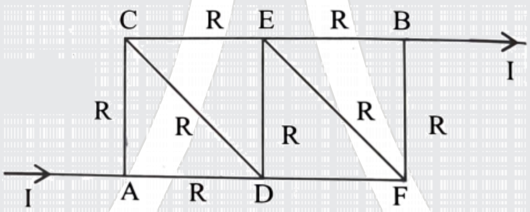
$a_c = \alpha r + 8$

$= 6.5 \times 2 + 8$

$\Rightarrow$ 13 + 8 $\Rightarrow$ 21 cm/s^2

option (d) is incorrect

57. Each of 9 sides of frame ACDEFB has resistance R (Nine in all) A current I centres at A and leaves at B Choose the correct alternatives.



(a) Current in branches CD and EF are zero.

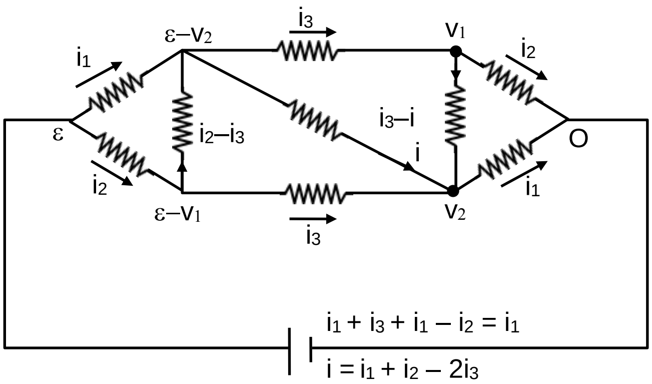
(b) Currents in branches CE and DF are each equal to $\frac{4}{11}$ I

(c) Effective resistance between A and B is $\frac{15}{11}$ R

(d) Effective resistance between A and B is $\frac{3}{4}$ R

Ans. **(b,c)**

Sol. $I = \frac{\varepsilon}{3R} + \frac{2\varepsilon}{5R}$



$I = \frac{5R\varepsilon + 6\varepsilon R}{15R}$

$= \frac{11R\varepsilon}{15R} \Rightarrow \frac{\varepsilon}{I} = \frac{15}{11} \Rightarrow V_2 = \frac{2\varepsilon}{5}$

$$\frac{\varepsilon - v_2 - v_1}{R} = \frac{v_1 - v_2}{R} + \frac{v_1 - 0}{R}$$

$\varepsilon - v_2 - v_1 = 2v_1 - v_2$

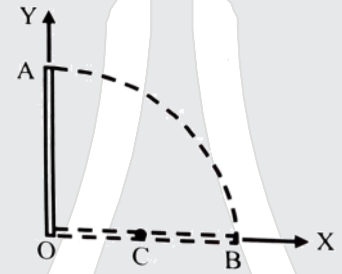
$$v_1 = \frac{\varepsilon}{3}$$

$$\frac{\varepsilon - v_2 - v_2}{R} + \frac{\varepsilon - v_1 - v_2}{R} + \frac{v_1 - v_2}{R} = \frac{v_2 - 0}{R}$$

$\varepsilon - 2v_2 + \varepsilon - v_1 - v_2 + v_1 - v_2$

$2\varepsilon = 5v_2 \;\; = v_2$

58. A long uniform rod of length L and mass M is pivoted vertically on a horizontal, friction less pivot at its lower end. The rod is released from rest in its vertical position OA (see figure). It falls off without slipping at O. At the instant the rod is horizontal.



(a) Its angular speed is $\sqrt{\frac{3g}{L}}$

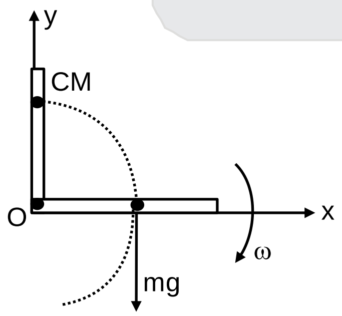
(b) Magnitude of its angular acceleration is $\frac{3g}{2L}$

(c) Acceleration of its centre of mass $\overrightarrow{a_{CM}} = -\frac{3g}{4}\hat{j}$ ($\hat{j}$ unit vector in Y direction)

(d) Reaction force at pivot = $\frac{Mg}{4}\hat{j}$ (Take X, Y axis as shown)

Ans. **(a,b)**

Sol. WET

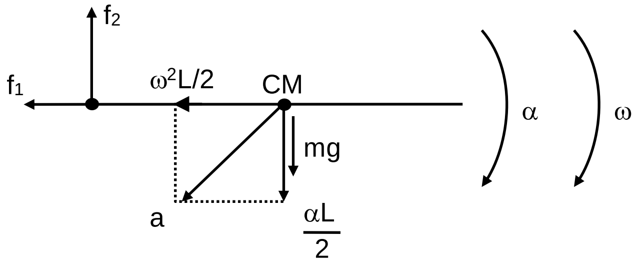


$$mg\frac{1}{2} = \frac{1}{2}\frac{ML^2w^2}{3}$$

$w = \sqrt{\frac{39}{L}}$ option (a) is correct

$$\tau_0 = mg\frac{\ell}{2}\frac{m\ell^2}{3}\alpha$$

$\alpha = \frac{39}{2\ell}$ option (b) is correct



$a_{cm} = -\dfrac{w2\ell}{2} + \dfrac{\alpha\ell}{2}(-\hat{j})$ option (c) is incorrect

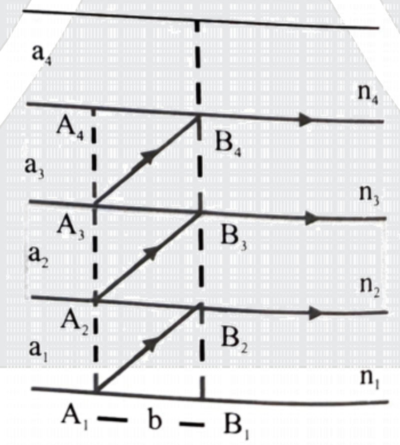
$f_1 = m\omega^2L/2$

$f1 = m \times \dfrac{39}{L} \times \dfrac{L}{2} = \dfrac{3mg}{2}$

$mg - f_2 = m \propto \dfrac{L}{2}$ Reaction force = $\dfrac{3mg\hat{i}}{2} + \dfrac{mg\hat{j}}{4}$

$f2 = mg - \dfrac{m39}{4} = \dfrac{mg}{4}$ = option (d) is incorrect

59. There are four layers of glass plates, placed on top of each other such that bottom one has thickness a_1 and refractive index n_4 = 2.7. Next one has thickness a_2 and refractive index n_2 = 2.43 . The third one and the top one have thickness a_3 and a_4 and refractive indices n_3 and n_4 respectively. Three rays starting at the same moment from A_2, A_2 and A_3 reach points B_2, B_3 B_4 at rthe same time with their angles of incidence being critical angle. You are given $A_3 B_1 = A_2 B_2 = A_3 B_4 = b = 10$ mm. Choose correct statement (s)

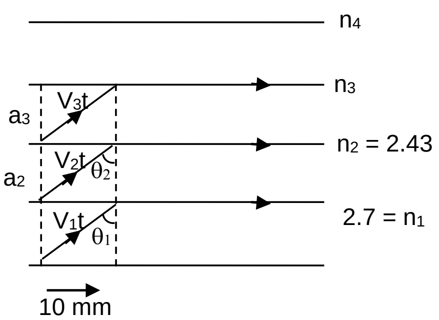


(a) n_1 = 1.968 (b) b_4 = 1.291 (c) a_2 = 7.243 mm (d) a_3 = 11.51 mm

[In four significant figures]

Ans. **(a,b,c,d)**

Sol.



$\mu = \dfrac{C}{V}$

$n_1 \sin\theta_1 = n_2 \sin\theta_2$

$2.7 \times \dfrac{10\times10^{-3}}{v_1 t} = 2.43 \sin$

$2.7 \times 10 \times 10^{-3} = = 2.43 \times V_1 t$

$2.7 \times 10^{-2} = \dfrac{3\times10^{8}\times2.43\times t}{2.7}$

$\dfrac{2.7\times2.7\times10^{-2}}{3\times2.43\times108} = t$

$t = 10^{-10}$ sec

$n_2 \sin\theta_2 = n_3 \sin 90$

$(2.43)^2 \times \dfrac{10\times10^{-3}}{3\times10^{8}\times10^{-10}} = n_3$

$\dfrac{2.43\times2.43}{3} = n_3$

$0.81 \times 2.43 = n_3$

$n_3 = 1.968$

$n_3 \sin\theta_3 = n_4 \sin 90^o$

$n_3^2 \dfrac{b}{ct} = n_4$

$n_4 = \dfrac{n_3^2 b}{ct} = \dfrac{1.968\times1.968\times10\times10^{-3}}{3\times10^{8}\times10^{-10}}$

$n_4 = 0.656 \times 1.968 = 1.291$

$a_2 = v_2 + \cos\theta_2$

$= \dfrac{c}{n_2} + \sqrt{1-\sin^2\theta_2}$

$= \dfrac{ct}{x_2}\sqrt{1-\left(\dfrac{x^3}{x^2}\right)^2} = \dfrac{ct}{x_2^2}\sqrt{n_2^2-n_3^2} = 7.2419$

$= 3\times10^{8}\times10^{-10} = 03$

$a_3 = v_3 t \cos\theta_3$

$= v_3 t\sqrt{1-\sin^2\theta_3} = v_3 t\sqrt{1-\left(\dfrac{n_4}{n_3}\right)^2}$

$= \dfrac{c}{n_3} t\sqrt{1-\left(\dfrac{n_4}{n_3}\right)^2} = \dfrac{3\times10^{-2}\sqrt{(1.968)^2-(1.291)^2}}{(1.968)^2} = \dfrac{3\times10^{-2}\times1.4853}{(1.968)^2}$

$= 10.505$

$= 11.51$ mm

$\dfrac{P_A V_A}{T_A} = \dfrac{P_C V_C}{T_2}$

$\dfrac{P_A}{e} = P_C$

$1 - \dfrac{T^2}{T_1}$

$1 - \dfrac{1}{e}$

60. A thin and infinitely long metal sheet of appreciable finite width b carrying current I (distributed uniformly through out of its cross section) parallel to its length is placed in an external magnetic field B parallel to its plane and perpendicular to the direction of current.

(a) The thin metal sheet experiences a mechanical pressure $P = \frac{IB_e}{b}$ perpendicular to its face.

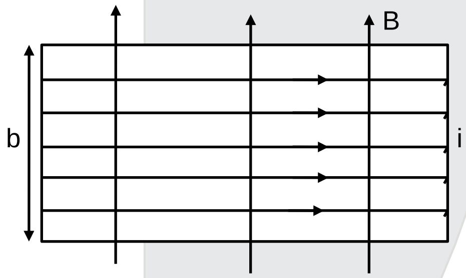
(b) The direction of the pressure does not change if the direction of current is reversed.

(c) In case the external magnetic field B_e is switched off, a magnetic field $B = \frac{\mu_0 I}{2b}$ is observed parallel to the plane of the sheet but perpendicular to the direction current

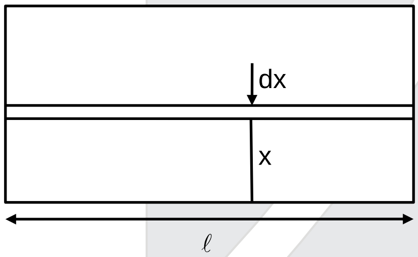
(d) The magnetic field produced in part (e) is $B = \frac{2\mu_0 I}{b}$

Ans. (a,b)

Sol.



Force



$df - i\ell B_0$

$\frac{I}{\ell} dx \ell B_0$

$f = \frac{I\ell B_0}{\ell}\int_0^b dx$

$\Rightarrow \frac{I\ell B_0 b}{b} = I\ell B$

$\text{Preserve} = \frac{f}{\text{area}} = \frac{I\ell B_0}{\ell b}$

$= \frac{IB_0}{b}$ option (a) is correct

pressure as a scalar has no deration so no charge in pressure direction

option (b) is in correct

when external B is absent then B is still there due to current I

$B = \frac{\mu_0}{2} = \frac{\mu_0}{2}\frac{I}{b}$

option (c) is correct

option (d) is incorrect