

Prashant

**SB/**

**SX**

**KVPY QUESTION PAPER – STREAM SB/SX**

NOVEMBER 1, 2015

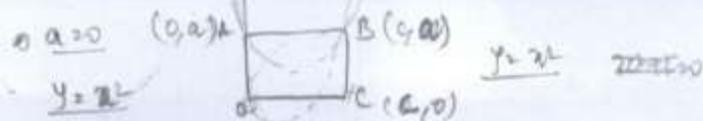
$$\frac{|z_1 - z_2|}{|z_1 + z_2|} \leq \frac{|z_1 - z_2|}{|z_1 - z_2|} \leq \frac{|z_1 - z_2|}{|z_1 + z_2|}$$

$$\frac{|z_1 - z_2|}{|z_1 + z_2|} \leq |z_1 - z_2| \leq |z_1|$$

$$\left| \left| z + \frac{1}{z} \right|^3 - 3 \left| z + \frac{1}{z} \right| \right| \leq 2$$

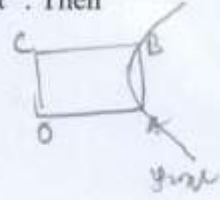
$$-2 \leq \left| z - \frac{1}{z} \right|^3 - 3 \left| z - \frac{1}{z} \right| \leq 2$$





4. Suppose  $OABC$  is a rectangle in the  $xy$ -plane where  $O$  is the origin and  $A, B$  lie on the parabola  $y = x^2$ . Then  $C$  must lie on the curve

- A.  $y = x^2 + 2$       B.  $y = 2x^2 + 1$   
 C.  $y = -x^2 + 2$       D.  $y = -2x^2 + 1$



5. Circles  $C_1$  and  $C_2$ , of radii  $r$  and  $R$  respectively, touch each other as shown in the figure. The line  $\ell$ , which is parallel to the line joining the centres of  $C_1$  and  $C_2$ , is tangent to  $C_1$  at  $P$  and intersects  $C_2$  at  $A, B$ . If  $R^2 = 2r^2$ , then  $\angle AOB$  equals

$\theta = \frac{R}{r} = \sqrt{2}$   
 $R^2 = 2r^2$

$\tan \frac{\theta}{2} = \frac{r}{y}$   
 $\frac{\theta}{2} = 45^\circ$   
 $\theta = 90^\circ$

$\sin \theta = \frac{AO}{R}$   
 $\sin \theta = \frac{r}{R-r}$

$\frac{\sin \theta}{2} = \frac{r}{R}$   
 $\sin \theta = \frac{2r}{R}$

$\frac{2r}{R} = \frac{2r}{\sqrt{2}r}$   
 $\sin \theta = \frac{1}{\sqrt{2}}$   
 $\theta = 45^\circ$

$\frac{\sin(\theta) \cos(\theta) - \cos(\theta) \sin(\theta)}{\sin \theta \cos \theta}$   
 $= \frac{2 \sin \alpha (\lambda - 1)}{2 \sin \alpha \cos \alpha} = \lambda - 1$   
 $\frac{2 \sin \alpha (\lambda - 1)}{\sin 2\alpha} = \lambda - 1$   
 $2 \sin \alpha (\lambda - 1) = \lambda \sin \alpha - \sin \alpha$

A.  $22 \frac{1}{2}^\circ$   
 B.  $45^\circ$   
 C.  $60^\circ$   
 D.  $67 \frac{1}{2}^\circ$



10. The value of the limit

$$\lim_{x \rightarrow 0} \left( \frac{x}{\sin x} \right)^{6/x^2}$$

is

- A.  $e$   
C.  $e^{-1/6}$

- B.  $e^{-1}$   
D.  $e^6$

11. Among all sectors of a fixed perimeter, choose the one with maximum area. Then the angle at the center of this sector (i.e., the angle between the bounding radii) is



- A.  $\frac{\pi}{3}$   
C.  $\sqrt{3}$

- B.  $\frac{3}{2}$   
D. 2



12. Define a function  $f: \mathbb{R} \rightarrow \mathbb{R}$  by

$$f(x) = \max\{|x|, |x-1|, \dots, |x-2n|\},$$

where  $n$  is a fixed natural number. Then  $\int_0^{2n} f(x) dx$  is

- A.  $n$   
C.  $3n$

- B.  $n^2$   
D.  $3n^2$

13. If  $p(x)$  is a cubic polynomial with  $p(1) = 3$ ,  $p(0) = 2$

and  $p(-1) = 4$ , then  $\int_{-1}^1 p(x) dx$  is

- A. 2  
C. 4

- B. 3  
D. 5

$$p(x) = \frac{a}{4}x^4 + bx^3 + c\left(\frac{x^2}{2} + 2x\right) + 2$$

$$p(x) = ax^3 + bx^2 + cx + 2$$

$$p(1) = 3$$

$$p(0) = 2$$

$$p(-1) = 4$$

$$\int_{-1}^1 p(x) dx$$

$$\int_0^x e^{-t}(x-t) dt - \int_0^{\infty} \frac{e^{-t}}{x-t} dt \quad x > 0$$

14. Let  $x > 0$  be a fixed real number. Then the integral  $\int_0^{\infty} e^{-t}(x-t) dt$  is equal to

- A.  $x + 2e^{-x} - 1$       B.  $x - 2e^{-x} + 1$   
~~C.  $x + 2e^{-x} + 1$~~       ~~D.  $-x - 2e^{-x} + 1$~~

$$\int_0^{\infty} e^{-t}(x-t) dt = \int_0^x e^{-t}(x-t) dt - \int_x^{\infty} e^{-t}(x-t) dt$$

15. An urn contains marbles of four colours: red, white, blue and green. When four marbles are drawn without replacement, the following events are equally likely:

- (1) the selection of four red marbles;
- (2) the selection of one white and three red marbles;
- (3) the selection of one white, one blue and two red marbles;
- (4) the selection of one marble of each colour.

The smallest total number of marbles satisfying the given condition is

- A. 19      B. 21  
 C. 46      D. 69

1B, 4R, 4W  
 4 Red

16. There are 6 boxes labelled  $B_1, B_2, \dots, B_6$ . In each trial, two fair dice  $D_1, D_2$  are thrown. If  $D_1$  shows  $j$  and  $D_2$  shows  $k$ , then  $j$  balls are put into the box  $B_k$ . After  $n$  trials, what is the probability that  $B_1$  contains at most one ball?

- A.  $\left(\frac{5^{n-1}}{6^{n-1}}\right) + \left(\frac{5^n}{6^n}\right)\left(\frac{1}{6}\right)$       B.  $\left(\frac{5^n}{6^n}\right) + \left(\frac{5^{n-1}}{6^{n-1}}\right)\left(\frac{1}{6}\right)$   
 C.  $\left(\frac{5^n}{6^n}\right) + n\left(\frac{5^{n-1}}{6^{n-1}}\right)\left(\frac{1}{6}\right)$       D.  $\left(\frac{5^n}{6^n}\right) + n\left(\frac{5^{n-1}}{6^{n-1}}\right)\left(\frac{1}{6^2}\right)$

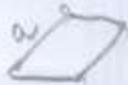
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$$\begin{aligned} a + b + c + 2 &= 3 \\ -a + b - c + 2 &= 4 \end{aligned}$$

$$\begin{aligned} 2b + 4 &= 7 \\ b &= 3/2 \end{aligned}$$

$$\begin{aligned} a + b + c &= -1/2 \\ a + c &= -1/2 \end{aligned}$$

$$\vec{b} = w\vec{i} + v\vec{j} + u\vec{k}$$



$$\vec{a} = b\vec{i}$$

$$\vec{a} = \vec{b} + \vec{c}$$

17. Let  $\vec{a} = 6\vec{i} - 3\vec{j} - 6\vec{k}$  and  $\vec{d} = \vec{i} + \vec{j} + \vec{k}$ . Suppose that  $\vec{a} = \vec{b} + \vec{c}$  where  $\vec{b}$  is parallel to  $\vec{d}$  and  $\vec{c}$  is perpendicular to  $\vec{d}$ . Then  $\vec{c}$  is

A.  $5\vec{i} - 4\vec{j} - \vec{k}$

B.  $7\vec{i} - 2\vec{j} - 5\vec{k}$

C.  $4\vec{i} - 5\vec{j} + \vec{k}$

D.  $3\vec{i} + 6\vec{j} - 9\vec{k}$

$\vec{a} = 6\vec{i} - 3\vec{j} - 6\vec{k}$

18. If  $\log_{(3x-1)}(x-2) = \log_{(9x^2-6x+1)}(2x^2-10x-2)$ , then  $x$  equals

A.  $9 - \sqrt{15}$

B.  $3 + \sqrt{15}$

C.  $2 + \sqrt{5}$

D.  $6 - \sqrt{5}$

19. Suppose  $a, b, c$  are positive integers such that  $2^a + 4^b + 8^c = 328$ . Then  $\frac{a+2b+3c}{abc}$  is equal to

A.  $\frac{1}{2}$

B.  $\frac{5}{8}$

C.  $\frac{17}{24}$

D.  $\frac{5}{6}$

$2^a + 4^b + 8^c = 328$   
 $\frac{a+2b+3c}{abc} =$

20. The sides of a right-angled triangle are integers. The length of one of the sides is 12. The largest possible radius of the incircle of such a triangle is

A. 2

B. 3

C. 4

D. 5



6

$$\vec{c} = 2\hat{i} + 4\hat{j} + 2\hat{k}$$

$$0.05$$

$$b / \sqrt{a^2}$$

$$b =$$

$$1 = \frac{1}{2} (4g)(2)$$

$$(2\hat{i} + 4\hat{j} + 2\hat{k}) \cdot (x\hat{i} + y\hat{j} + z\hat{k}) = 0$$

$$\frac{1}{10} \quad \frac{2}{42} = k(10)$$

### PHYSICS

$$x + y + z = 0$$

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21. A small box resting on one edge of the table is struck in such a way that it slides off the other edge, 1 m away, after 2 seconds. The coefficient of kinetic friction between the box and the table

(41)

A x A

$$4 \times 4 = 16$$

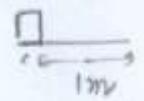
A. must be less than 0.05

$$4 \times 4 = 16$$

$$2 \times 4 = 16$$

$$\frac{328}{4 \times 2} \quad \frac{8(10)}{8} \quad (4)$$

B. must be exactly zero



C. must be more than 0.05

D. must be exactly 0.05

32

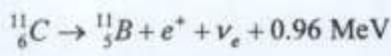
$$\mu mg = ma$$

$$a = (4g)$$

(28)

22. Carbon-11 decays to boron-11 according to the following formula.

$$\frac{328}{8} \quad 41$$



$$\begin{array}{r} 8 \overline{) 328} \\ \underline{41} \end{array}$$

Assume that positrons ( $e^+$ ) produced in the decay combine with free electrons in the atmosphere and annihilate each other almost immediately. Also assume that the neutrinos ( $\nu_e$ ) are massless and do not interact with the environment. At  $t=0$  we have  $1 \mu\text{g}$  of  ${}^{11}_6\text{C}$ . If the half-life of the decay process is  $t_0$ , the net energy produced between time  $t=0$  and  $t=2t_0$  will be nearly

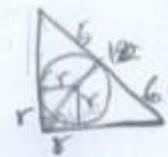
- A.  $8 \times 10^{18} \text{ MeV}$
- B.  $8 \times 10^{16} \text{ MeV}$
- C.  $4 \times 10^{18} \text{ MeV}$
- D.  $4 \times 10^{16} \text{ MeV}$

$$2^2 + 2^{2^2} + 2^{2^3} = 328$$

$$r(1+\sqrt{2})$$

9

$$r \frac{6}{(1+\sqrt{2})} \quad \frac{6}{(1+\sqrt{2})} \quad \frac{r(1+\sqrt{2}) \cdot 6}{(\sqrt{2}r)}$$



$$\tan(\theta) = \frac{6}{r+\sqrt{2}r}$$

$$(r+y)^2 + (r+y)^2 = 12$$

23. Two uniform plates of the same thickness and area but of different materials, one shaped like an isosceles triangle and the other shaped like a rectangle are joined together to form a composite body as shown in the figure. If the centre of mass of the composite body is located at the midpoint of their common side, the ratio between masses of the triangle to that of the rectangle is

Handwritten notes for problem 23:

- $\frac{m_t}{A} = \frac{m_r}{A}$  (since thickness and area are the same)
- $K(h) = b \times h$
- $\frac{L}{2} = \frac{m_t(\frac{h}{3}) + m_r(\frac{h}{2})}{m_t + m_r}$
- $\frac{m_r}{m_t} = \frac{2h}{h} = 2$
- $\frac{m_t}{m_r} = \frac{1}{2}$

Options:

- A. 1:1
- B. 4:3
- C. 3:4
- D. 2:1

24. Two spherical objects each of radii  $R$  and masses  $m_1$  and  $m_2$  are suspended using two strings of equal length  $L$  as shown in the figure ( $R \ll L$ ). The angle,  $\theta$  which mass  $m_2$  makes with the vertical is approximately

Handwritten notes for problem 24:

- $5.65 = \frac{m_1 R}{(m_1 + m_2)L}$
- $\frac{m_1 R}{(m_1 + m_2)L} = \frac{m_2 R}{(m_1 + m_2)L}$
- $\frac{m_1}{m_2} = \frac{m_2}{m_1}$
- $\frac{m_1}{m_2} = \frac{m_2}{m_1}$

Options:

- A.  $\frac{m_1 R}{(m_1 + m_2)L}$
- B.  $\frac{2m_1 R}{(m_1 + m_2)L}$
- C.  $\frac{2m_2 R}{(m_1 + m_2)L}$
- D.  $\frac{m_2 R}{(m_1 + m_2)L}$

Handwritten note:  $\frac{m_1}{m_2} = \frac{m_2}{m_1}$

Handwritten note:  $\frac{m_1}{m_2} = \frac{m_2}{m_1}$

$m_1 \quad I = 4.25$   
 $(I_1 \omega_1) = (I_2 \omega_2)$   
 $(4.25)(15) = (1.8)(25)$   
 $I = 1.80$   
 $(4.25)(15) + (1.8)(25) = (6.05)\omega$

25. A horizontal disk of moment of inertia  $4.25 \text{ kg}\cdot\text{m}^2$  with respect to its axis of symmetry is spinning counter clockwise at 15 revolutions per second about its axis, as viewed from above. A second disk of moment of inertia  $1.80 \text{ kg}\cdot\text{m}^2$  with respect to its axis of symmetry is spinning clockwise at 25 revolutions per second as viewed from above about the same axis and is dropped on top of the first disk. The two disks stick together and rotate as one about their axis of symmetry. The new angular velocity of the system as viewed from above is close to

$$\begin{array}{r} 4.25 \\ 1.80 \\ \hline 6.05 \end{array}$$

$$\begin{array}{r} 2 \\ 4.25 \\ 1.8 \\ \hline 22.25 \\ 425 \times \\ \hline 6475 \end{array}$$

$$\begin{array}{r} 64.75 \\ 45 \\ \hline 109.75 \end{array}$$

$$\begin{array}{r} 109.75 \\ 6.05 \\ \hline 18.14 \end{array}$$

- A. 18 revolutions/second and clockwise.
- B. 18 revolutions/second and counter clockwise.
- C. 3 revolutions/second and clockwise.
- D. 3 revolutions/second and counter clockwise.

$\omega = 15$   
 $I = 4.25$   

$$\begin{array}{r} 4 \\ 25 \\ \hline 100 \\ 200 \\ \hline 300 \end{array}$$

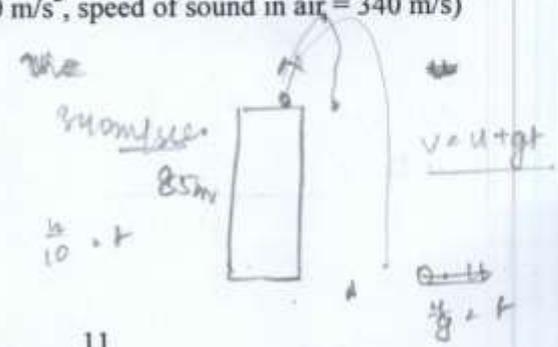
$$\begin{array}{r} 20 \\ 0 \\ \hline 25 \times \\ \hline 44 \end{array}$$

26. A boy is standing on top of a tower of height 85 m and throws a ball in the vertically upward direction with a certain speed. If 5.25 seconds later he hears the ball hitting the ground, then the speed with which the boy threw the ball is (take  $g = 10 \text{ m/s}^2$ , speed of sound in air =  $340 \text{ m/s}$ )

$$\frac{17.75}{608} = 2.92$$

$$\frac{2u}{2g}$$

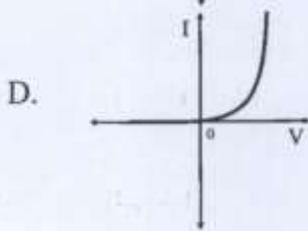
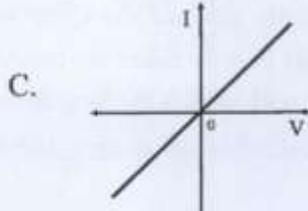
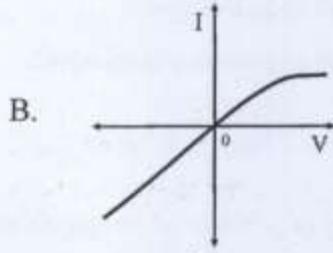
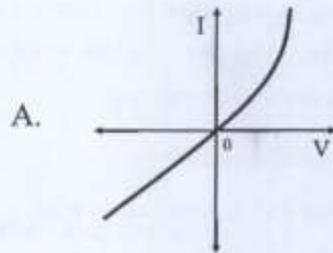
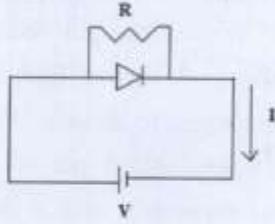
- A. 6 m/s
- B. 8 m/s
- C. 10 m/s
- D. 12 m/s



11

$(m_1 + m_2) (R \omega)$   
 $(m_1 + m_2) R \omega = m_1 r_1 \omega_1 + m_2 r_2 \omega_2$   
 $(m_1 + m_2) (R \omega)$   
 $\frac{2u}{g} = 5.25$

27. For a diode connected in parallel with a resistor, which is the most likely current ( $I$ ) – voltage ( $V$ ) characteristic?



28. A beam of monoenergetic electrons, which have been accelerated from rest by a potential  $U$ , is used to form an interference pattern in a Young's Double Slit experiment. The electrons are now accelerated by potential  $4U$ . Then the fringe width

- A. remains the same.
- B. is half the original fringe width.
- C. is twice the original fringe width.
- D. is one-fourth the original fringe width.

29. A point charge  $Q (= 3 \times 10^{-12} \text{ C})$  rotates uniformly in a vertical circle of radius  $R = 1 \text{ mm}$ . The axis of the circle is aligned along the magnetic axis of the earth. At what value of the angular speed  $\omega$ , the effective magnetic field at the center of the circle will be reduced to zero? (Horizontal component of Earth's magnetic field is 30 microTesla)

- A.  $10^{11} \text{ rad/s}$
  - B.  $10^9 \text{ rad/s}$
  - C.  $10^{13} \text{ rad/s}$
  - D.  $10^7 \text{ rad/s}$
- B<sub>H</sub> = 30 μT*

*Q = 3 × 10<sup>-12</sup> C*

30. A closed bottle containing water at 30 °C is open on the surface of the moon. Then

- A. the water will boil. Ⓟ
- B. the water will come out as a spherical ball. T<sub>mp</sub>
- C. the water will freeze. T<sub>2</sub>
- D. the water will decompose into hydrogen and oxygen.

$$\frac{g}{10}$$

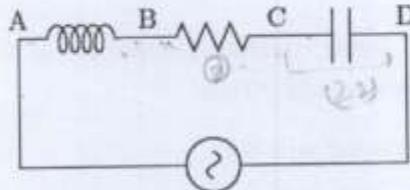
$$T_0 = 2\pi \sqrt{\frac{l}{g}}$$



31. A simple pendulum of length  $l$  is made to oscillate with an amplitude of 45 degrees. The acceleration due to gravity is  $g$ . Let  $T_0 = 2\pi\sqrt{l/g}$ . The time period of oscillation of this pendulum will be

- A.  $T_0$  irrespective of the amplitude.  $T_0 = 2\pi \sqrt{\frac{l}{g}}$   $\theta = 45^\circ$   
B. slightly less than  $T_0$ .  
C. slightly more than  $T_0$ .  
D. dependent on whether it swings in a plane aligned with the north-south or east-west directions.

32. An ac voltmeter connected between points A and B in the circuit below reads 36 V. If it is connected between A and C, the reading is 39 V. The reading when it is connected between B and D is 25 V. What will the voltmeter read when it is connected between A and D? (Assume that the voltmeter reads true rms voltage values and that the source generates a pure ac.)



- A.  $\sqrt{481}$  V  
B. 31 V  
C. 61 V  
D.  $\sqrt{3361}$  V

$$V = \sqrt{(V_2 - V_1)^2 + V_3^2}$$

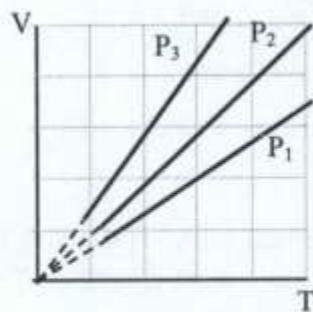
$$V = \sqrt{(36 - 25)^2 + 32^2}$$

$$\sqrt{(11)^2 + 32^2}$$

33. A donor atom in a semiconductor has a loosely bound electron. The orbit of this electron is considerably affected by the semiconductor material but behaves in many ways like an electron orbiting a hydrogen nucleus. Given that the electron has an effective mass of  $0.07m_e$ , (where  $m_e$  is mass of the free electron) and the space in which it moves has a permittivity  $13\epsilon_0$ , then the radius of the electron's lowermost energy orbit will be close to (The Bohr radius of the hydrogen atom is  $0.53\text{\AA}$ )

- A.  $0.53\text{\AA}$                       B.  $243\text{\AA}$   
 C.  $10\text{\AA}$                               D.  $100\text{\AA}$

34. The state of an ideal gas was changed isobarically. The graph depicts three such isobaric lines. Which of the following is true about the pressures of the gas?



$P = \text{const.}$

- ~~A.~~  $P_1 = P_2 = P_3$                       B.  $P_1 > P_2 > P_3$   
 C.  $P_1 < P_2 < P_3$                       ~~D.~~  $P_1/P_2 = P_3/P_1$

19/1  
20



$$\sin \frac{\pi}{n} = \left(\frac{l}{2R}\right) \sin \left(\frac{\pi}{n}\right)$$

$$\frac{\mu_0 I dl \sin \theta}{r^2}$$

38. A wire bent in the shape of a regular  $n$  - polygonal loop carries a steady current  $I$ . Let  $l$  be the perpendicular distance of a given segment and  $R$  be the distance of a vertex both from the centre of the loop. The magnitude of the magnetic field at the centre of the loop is given by

$$\frac{n \mu_0 I l}{2l} \sin \left(\frac{\pi}{n}\right)$$

A.  $\frac{n \mu_0 I}{2\pi l} \sin(\pi/n)$       B.  $\frac{n \mu_0 I}{2\pi R} \sin(\pi/n)$

C.  $\frac{n \mu_0 I}{2\pi l} \cos(\pi/n)$       D.  $\frac{n \mu_0 I}{2\pi R} \cos(\pi/n)$

$$\frac{M}{r^2} = \frac{GMm}{L^2} \quad \frac{n \mu_0 I}{2\pi R}$$

39. The intensity of sound during the festival season increased by 100 times. This could imply a decibel level rise from

A. 20 to 120 dB      B. 70 to 72 dB       $10 \log \left(\frac{I}{I_0}\right)$

C. 100 to 10000 dB      D. 80 to 100 dB       $10 \log \left(\frac{20}{10^{-12}}\right)$

40. One end of a slack wire (Young's modulus  $Y$ , length  $L$  and cross-sectional area  $A$ ) is clamped to a rigid wall and the other end to a block (mass  $m$ ) which rests on a smooth horizontal plane. The block is set in motion with a speed  $v$ . What is the maximum distance the block will travel after the wire becomes taut?

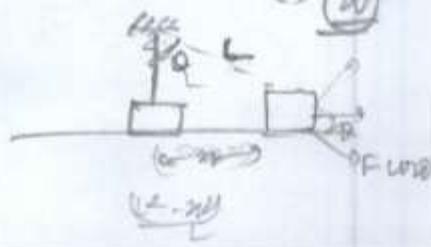
2 $\alpha$  +  $\gamma$  = 0      A.  $v \sqrt{\frac{mL}{AY}}$

B.  $v \sqrt{\frac{2mL}{AY}}$        $3 = \sqrt{4}$

3 $\alpha$  +  $\gamma$  = 2      C.  $v \sqrt{\frac{mL}{2AY}}$

D.  $L \sqrt{\frac{mv}{AY}}$        $10 \log \left(\frac{1000}{10^{-12}}\right)$

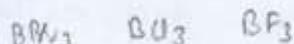
$\alpha = 2$   
 $\beta = 2$   
 $\gamma = 2$   
 $Y = \frac{AY \delta}{mL}$   
 $Y = \frac{Y A \delta L}{L}$   
 $2 \delta = \frac{v^2}{L}$   
 $\delta = \frac{v^2 L}{2}$



## CHEMISTRY

41. The Lewis acid strength of  $\text{BBr}_3$ ,  $\text{BCl}_3$  and  $\text{BF}_3$  is in the order

- A.  $\text{BBr}_3 < \text{BCl}_3 < \text{BF}_3$   
~~B.~~  $\text{BCl}_3 < \text{BF}_3 < \text{BBr}_3$   
 C.  $\text{BF}_3 < \text{BCl}_3 < \text{BBr}_3$   
 D.  $\text{BBr}_3 < \text{BF}_3 < \text{BCl}_3$



42.  $\text{O}^{2-}$  is isoelectronic with

- ~~A.~~  $\text{Zn}^{2+}$                       B.  $\text{Mg}^{2+}$   
 C.  $\text{K}^+$                          D.  $\text{Ni}^{2+}$

18

43. The H-C-H, H-N-H, and H-O-H bond angles (in degrees) in methane, ammonia and water are respectively, closest to

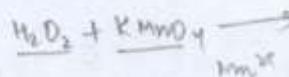
- ~~A.~~ 109.5, 104.5, 107.1  
 B. 109.5, 107.1, 104.5  
 C. 104.5, 107.1, 109.5  
 D. 107.1, 104.5, 109.5



Low

44. In alkaline medium, the reaction of hydrogen peroxide with potassium permanganate produces a compound in which the oxidation state of Mn is

- A. 0                                 ~~B.~~ +2  
 C. +3                               D. +4



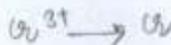
45. The rate constant of a chemical reaction at a very high temperature will approach
- Arrhenius frequency factor divided by the ideal gas constant
  - activation energy
  - Arrhenius frequency factor
  - activation energy divided by the ideal gas constant

$$k = A e^{-R}$$

46. The standard reduction potentials (in V) of a few metal ion/metal electrodes are given below.

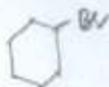
$\text{Cr}^{3+}/\text{Cr} = -0.74$ ;  $\text{Cu}^{2+}/\text{Cu} = +0.34$ ;  $\text{Pb}^{2+}/\text{Pb} = -0.13$ ;  
 $\text{Ag}^+/\text{Ag} = +0.8$ . The reducing strength of the metals follows the order

- ~~A~~  $\text{Ag} > \text{Cu} > \text{Pb} > \text{Cr}$
- B.  $\text{Cr} > \text{Pb} > \text{Cu} > \text{Ag}$
- C.  $\text{Pb} > \text{Cr} > \text{Ag} > \text{Cu}$
- D.  $\text{Cr} > \text{Ag} > \text{Cu} > \text{Pb}$

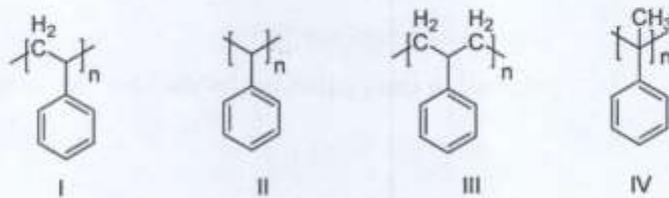
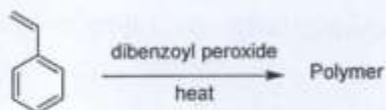


47. Which of the following molecules can exhibit optical activity?

- 1-bromopropane
- ~~B~~ 2-bromobutane
- C. 3-bromopentane
- D. bromocyclohexane



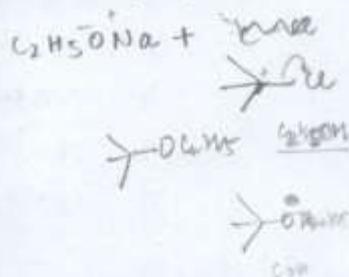
48. The structure of the polymer obtained by the following reaction is



- A. I                      B. II  
C. III                    D. IV

49. The major product of the reaction between  $\text{CH}_3\text{CH}_2\text{ONa}$  and  $(\text{CH}_3)_3\text{CCl}$  in ethanol is

- A.  $\text{CH}_3\text{CH}_2\text{OC}(\text{CH}_3)_3$   
 B.  $\text{CH}_2=\text{C}(\text{CH}_3)_2$   
 C.  $\text{CH}_3\text{CH}_2\text{C}(\text{CH}_3)_3$   
 D.  $\text{CH}_3\text{CH}=\text{CHCH}_3$



50. When  $\text{H}_2\text{S}$  gas is passed through a hot acidic aqueous solution containing  $\text{Al}^{3+}$ ,  $\text{Cu}^{2+}$ ,  $\text{Pb}^{2+}$  and  $\text{Ni}^{2+}$ , a precipitate is formed which consists of

- A.  $\text{CuS}$  and  $\text{Al}_2\text{S}_3$        B.  $\text{PbS}$  and  $\text{NiS}$   
 C.  $\text{CuS}$  and  $\text{NiS}$        D.  $\text{PbS}$  and  $\text{CuS}$



$n(n+1)$  or  $\frac{n(n+1)}{2}$  3l 3e 3m  
 $3d^5$   
 $3d^4$   
 $3d^3$   

n	1	2	3	4	5
---	---	---	---	---	---

51. The electronic configuration of an element with the largest difference between the 1<sup>st</sup> and 2<sup>nd</sup> ionization energies is

- A.  $1s^2 2s^2 2p^6$       ~~B.~~  $1s^2 2s^2 2p^6 3s^1$   
 C.  $1s^2 2s^2 2p^6 3s^2$       D.  $1s^2 2s^2 2p^1$  1<sup>st</sup>    2<sup>nd</sup>

52. The order of electronegativity of carbon in  $sp$ ,  $sp^2$  and  $sp^3$  hybridized states follows

- A.  $sp > sp^2 > sp^3$       B.  $sp^3 > sp^2 > sp$   $sp, sp^2, sp^3$   
~~C.~~  $sp > sp^3 > sp^2$       D.  $sp^2 > sp > sp^3$

53. The most abundant transition metal in human body is

- A. copper      B. iron  
~~C.~~ zinc      ~~D.~~ manganese

54. The molar conductivities of HCl, NaCl, CH<sub>3</sub>COOH, and CH<sub>3</sub>COONa at infinite dilution follow the order

- ~~A.~~ HCl > CH<sub>3</sub>COOH > NaCl > CH<sub>3</sub>COONa  $\lambda_m^\infty = b \sqrt{c}$   
 B. CH<sub>3</sub>COONa > HCl > NaCl > CH<sub>3</sub>COOH  $\lambda_m^\infty =$   
 C. HCl > NaCl > CH<sub>3</sub>COOH > CH<sub>3</sub>COONa molar conductivity  
 D. CH<sub>3</sub>COOH > CH<sub>3</sub>COONa > HCl > NaCl -ty

55. The spin only magnetic moment of  $[ZCl_4]^{2-}$  is 3.87 BM where Z is

- A. Mn      B. Ni  $[ZCl_4]^{2-}$   
 C. Co      D. Cu  $\sqrt{n(n+2)} = (3.87)^2$

$n(n+2) = 16$   
 $n^2 + 2n - 16 = 0$   
 $n = 4$   
 $n(n+2) = 2$   
 $n^2 + 2n - 16 = 0$   
 $n = 4$

$n(n+2) = 16$   
 $n^2 + 2n - 16 = 0$   
 $n(n+2) = 2$   
 $n^2 + 2n - 16 = 0$   
 $n = 4$

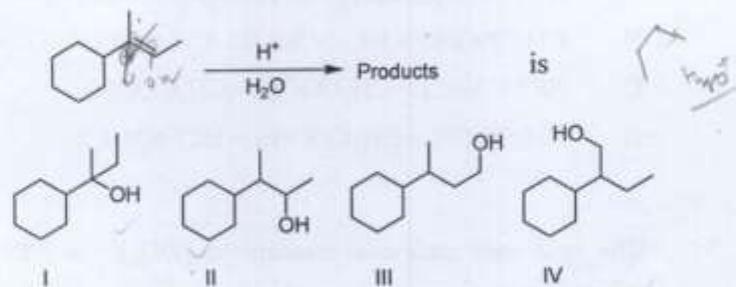
56. If  $\alpha$ -D-glucose is dissolved in water and kept for a few hours, the major constituent(s) present in the solution is (are)

- A.  $\alpha$ -D-glucose  $\alpha$ -D  
 B. mixture of  $\beta$ -D-glucose and open chain D-glucose  
 C. open chain D-glucose  
 D. mixture of  $\alpha$ -D-glucose and  $\beta$ -D-glucose

57. The pH of 1N aqueous solutions of HCl, CH<sub>3</sub>COOH and HCOOH follows the order

- A. HCl > HCOOH > CH<sub>3</sub>COOH  $pH = -\log[H^+]$   
 B. HCl = HCOOH > CH<sub>3</sub>COOH  $HCl \rightarrow H^+ + Cl^-$   
 C. CH<sub>3</sub>COOH > HCOOH > HCl  $1 \quad 1$   
 D. CH<sub>3</sub>COOH = HCOOH > HCl  $pH = -\log[1] = 0$
- $\frac{CH_3COOH}{H^+} = \frac{K_a}{\alpha}$   $CH_3COOH \rightarrow CH_3COO^- + H^+$   
 $(\alpha)$   $\alpha \quad \alpha$

58. The major product of the reaction



- A. I B. II  
 C. III D. IV

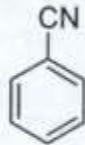
59. Reaction of aniline with  $\text{NaNO}_2 + \text{dil. HCl}$  at  $0^\circ\text{C}$  followed by reaction with  $\text{CuCN}$  yields



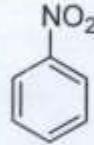
I



II



III



IV

A. I

B. II

C. III

D. IV

(1) (CN)  $\text{NO}_2$

60. Schottky defect in a crystal arises due to

- A. creation of equal number of cation and anion vacancies
- B. creation of unequal number of cation and anion vacancies
- C. migration of cations to interstitial voids
- D. migration of anions to interstitial voids

## BIOLOGY

61. Immunosuppressive drugs like cyclosporin delay the rejection of graft post organ transplantation by
- A. inhibiting T cell infiltration
  - B. killing B cells
  - C. killing macrophages
  - D. killing dendritic cells
62. Which one of these substances will repress the *lac* operon?
- A. Arabinose
  - B. Glucose
  - C. Lactose
  - D. Tryptophan
63. Assume a spherical mammalian cell has a diameter of 27 microns. If a polypeptide chain with alpha helical conformation has to stretch across the cell, how many amino acids should it be comprised of?
- A. 18000
  - B. 1800
  - C. 27000
  - D. 12000
64. Which one of the following has phosphoric acid anhydride bonds?
- A. Deoxy ribonucleic acid
  - B. Ribonucleic acid
  - C. dNTPs
  - D. Phospholipids

65. The two components of autonomous nervous system have antagonistic actions. But in certain cases their effects are mutually helpful. Which of the following statement is correct?
- A. At rest, the control of heart beat is not by the vagus nerve
  - B. During exercise the sympathetic control decreases
  - C. During exercise the parasympathetic control decreases
  - D. Stimulation of sympathetic system results in constriction of the pupil
66. In a random DNA sequence, what is the lowest frequency of encountering a stop codon?
- A. 1 in 20
  - B. 1 in 3
  - C. 1 in 64
  - D. 1 in 10
67. The two alleles that determine the blood group AB of an individual are located on
- A. two different autosomes
  - B. the same autosome
  - C. two different sex chromosomes
  - D. one on sex chromosome and the other on an autosome

68. In biotechnology applications, a selectable marker is incorporated in a plasmid
- A. to increase its copy number
  - B. to increase the transformation efficiency
  - C. to eliminate the non-transformants
  - D. to increase the expression of the gene of interest
69. Spermatids are formed after the second meiotic division from secondary spermatocytes. The ploidy of the secondary spermatocytes is
- A.  $n$
  - B.  $2n$
  - C.  $3n$
  - D.  $4n$
70. Phospholipids are formed by the esterification of
- A. three ethanol molecules with three fatty acid molecules.
  - B. one glycerol and two fatty acid molecules.
  - C. one glycerol and three fatty acid molecules.
  - D. one ethylene glycol and two fatty acids molecules.
71. Given the fact that histone binds DNA, it should be rich in
- A. arginine, lysine
  - B. cysteine, methionine
  - C. glutamate, aspartate
  - D. isoleucine, leucine

72. If molecular weight of a polypeptide is 15.3 kDa, what would be the minimum number of nucleotides in the mRNA that codes for this polypeptide? Assume that molecular weight of each amino acid is 90 Da.
- A. 510                      B. 663  
C. 123                        D. 170
73. Melting temperature for double stranded DNA is the temperature at which 50% of the double stranded molecules are converted into single stranded molecules. Which one of the following DNA will have the highest melting temperature?
- A. DNA with 15% guanine  
B. DNA with 30% cytosine  
C. DNA with 40% thymine  
D. DNA with 50% adenine
74. Following are the types of immunoglobulin and their functions. Which one of the following is INCORRECTLY paired?
- A. IgD: viral pathogen  
B. IgG: phagocytosis  
C. IgE: allergic reaction  
D. IgM: complement fixation
75. Which one of the following can be used to detect amino acids?
- A. Iodine vapour            B. Ninhydrin  
C. Ethidium bromide      D. Bromophenol blue

76. Mutation in a single gene can lead to changes in multiple traits. This is an example of
- A. Heterotrophy      B. Co-dominance  
C. Penetrance      D. Pleiotropy
77. Which one of the following is used to treat cancers?
- A. Albumin      B. Cyclosporin A  
C. Antibodies      D. Growth hormone
78. Which of the following processes leads to DNA ladder formation?
- A. Necrosis      B. Plasmolysis  
C. Apoptosis      D. Mitosis
79. Co-enzymes are components of an enzyme complex which are necessary for its function. Which of these is a known co-enzyme?
- A. Zinc      B. Vitamin B<sub>12</sub>  
C. Chlorophyll      D. Heme
80. The peptidoglycans of bacteria consist of
- A. sugars, D-amino acids and L-amino acids  
B. sugars and only D-amino acids  
C. sugars and only L-amino acids  
D. sugars and glycine

$$2 \left[ nC_1 + nC_3 + nC_5 + \dots + nC_{n-1} \right] x = 2 \left[ \binom{n}{1} (\sqrt{10})^{n-1} (7) + \binom{n}{3} (\sqrt{10})^{n-3} (7)^3 + \dots \right]$$

PART II

Two-Mark Questions

MATHEMATICS

81. Let  $x = (\sqrt{50+7})^{1/3} - (\sqrt{50-7})^{1/3}$ . Then

- A.  $x = 2$
- B.  $x = 3$
- C.  $x$  is a rational number, but not an integer
- D.  $x$  is an irrational number

$$x = (\sqrt{50+7})^{1/3} - (\sqrt{50-7})^{1/3}$$

$$x = \binom{1/3}{0} (\sqrt{50})^{1/3} + \dots$$

82. Let

$$(1+x+x^2)^{2014} = a_0 + a_1x + a_2x^2 + a_3x^3 + \dots + a_{4028}x^{4028},$$

and let

$$A = a_0 - a_3 + a_6 - \dots + a_{4026},$$

$$B = a_1 - a_4 + a_7 - \dots - a_{4027},$$

$$C = a_2 - a_5 + a_8 - \dots + a_{4028}.$$

Then

- A.  $|A| = |B| > |C|$
- B.  $|A| = |B| < |C|$
- C.  $|A| = |C| > |B|$
- D.  $|A| = |C| < |B|$

83. A mirror in the first quadrant is in the shape of a hyperbola whose equation is  $xy = 1$ . A light source in the second quadrant emits a beam of light that hits the mirror at the point  $(2, 1/2)$ . If the reflected ray is parallel to the  $y$ -axis, the slope of the incident beam is

- A.  $\frac{13}{8}$                       B.  $\frac{7}{4}$   
C.  $\frac{15}{8}$                       D. 2

84. Let

$$C(\theta) = \sum_{n=0}^{\infty} \frac{\cos(n\theta)}{n!}.$$

Which of the following statements is FALSE?

- A.  $C(0) \cdot C(\pi) = 1$   
B.  $C(0) + C(\pi) > 2$   
C.  $C(\theta) > 0$  for all  $\theta \in \mathbb{R}$   
D.  $C'(\theta) \neq 0$  for all  $\theta \in \mathbb{R}$
85. Let  $a > 0$  be a real number. Then the limit

$$\lim_{x \rightarrow 2} \frac{a^x + a^{3-x} - (a^2 + a)}{a^{3-x} - a^{x/2}}$$

is

- A.  $2 \log a$                       B.  $-\frac{4}{3}a$   
C.  $\frac{a^2 + a}{2}$                       D.  $\frac{2}{3}(1-a)$

86. Let  $f(x) = \alpha x^2 - 2 + \frac{1}{x}$  where  $\alpha$  is a real constant. The smallest  $\alpha$  for which  $f(x) \geq 0$  for all  $x > 0$  is

- A.  $\frac{2^2}{3^3}$   
B.  $\frac{2^3}{3^3}$   
C.  $\frac{2^4}{3^3}$   
D.  $\frac{2^5}{3^3}$

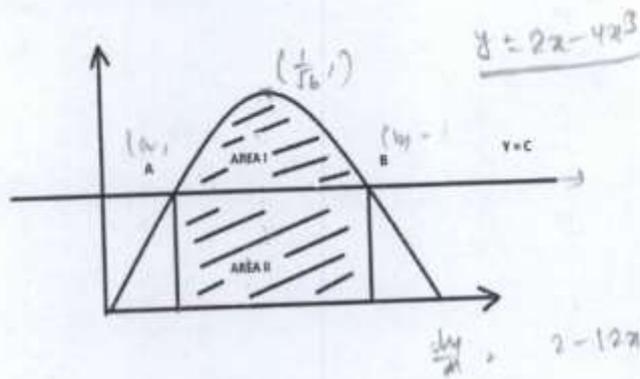
87. Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be a continuous function satisfying

$$f(x) + \int_0^x f(t) dt + x^2 = 0,$$

for all  $x \in \mathbb{R}$ . Then

- A.  $\lim_{x \rightarrow \infty} f(x) = 2$   
B.  $\lim_{x \rightarrow -\infty} f(x) = -2$   
C.  $f(x)$  has more than one point in common with the  $x$ -axis  
D.  $f(x)$  is an odd function

88. The figure shows a portion of the graph  $y = 2x - 4x^3$ . The line  $y = c$  is such that the areas of the regions marked I and II are equal. If  $a, b$  are the  $x$ -coordinates of  $A, B$  respectively, then  $a + b$  equals



- A.  $\frac{2}{\sqrt{7}}$   
 B.  $\frac{3}{\sqrt{7}}$   
 C.  $\frac{4}{\sqrt{7}}$   
 D.  $\frac{5}{\sqrt{7}}$

$$\begin{aligned}
 \frac{dy}{dx} &= 2 - 12x^2 = 0 \\
 2 &= 12x^2 \\
 \frac{1}{6} &= x \\
 y &= \frac{2}{6} - \frac{4}{216} \\
 \frac{2}{\sqrt{6}} - \frac{1}{9\sqrt{6}} &= \frac{2}{\sqrt{6}} - \frac{1}{9\sqrt{6}} \\
 \frac{1}{12} \left( 2 - \frac{1}{9} \right) &= \left( \frac{17}{9\sqrt{6}} \right)
 \end{aligned}$$

89. Let  $X_n = \{1, 2, 3, \dots, n\}$  and let a subset  $A$  of  $X_n$  be chosen so that every pair of elements of  $A$  differ by at least 3. (For example, if  $n=5$ ,  $A$  can be  $\emptyset$ ,  $\{2\}$  or  $\{1, 5\}$  among others). When  $n=10$ , let the probability that  $1 \in A$  be  $p$  and let the probability that  $2 \in A$  be  $q$ . Then

- A.  $p > q$  and  $p - q = \frac{1}{6}$   
B.  $p < q$  and  $q - p = \frac{1}{6}$   
C.  $p > q$  and  $p - q = \frac{1}{10}$   
D.  $p < q$  and  $q - p = \frac{1}{10}$

90. The remainder when the determinant

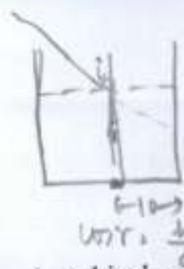
$$\begin{vmatrix} 2014^{2014} & 2015^{2015} & 2016^{2016} \\ 2017^{2017} & 2018^{2018} & 2019^{2019} \\ 2020^{2020} & 2021^{2021} & 2022^{2022} \end{vmatrix}$$

is divided by 5 is

- A. 1                                      B. 2  
C. 3                                      D. 4

2014<sup>2015</sup>

$\tan \theta = \frac{z+10}{h}$   
 $\tan r = \frac{z}{h}$   
 COSY  
 $\cos r = \frac{z}{h}$



**PHYSICS**

$\sin(i-r) = \frac{z}{d}$

91. A cubical vessel has opaque walls. An observer (dark circle in figure below) is located such that she can see only the wall CD but not the bottom. Nearly to what height should water be poured so that she can see an object placed at the bottom at a distance of 10 cm from the corner C? Refractive index of water is 1.33.

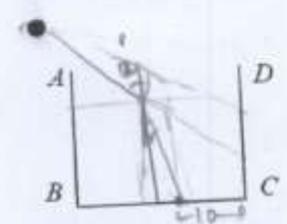
$\tan i = \frac{h \tan r + 10}{h}$

$\tan i = \tan r + \frac{10}{h}$

$\tan i - \tan r = \frac{10}{h}$

$\frac{\sin i}{\cos i} - \frac{\sin r}{\cos r} = \frac{10}{h}$

$\frac{\sin(i-r)}{\cos i \cos r}$



$\sin i = 1.33 \sin r$

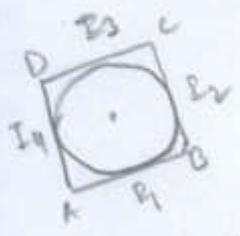
$\sin i = 1.33 \sin r$

$\frac{\sin i}{\sin r} = 1.33$

- A. 10 cm
- B. 16 cm
- C. 27 cm
- D. 45 cm

92. The moments of inertia of a non-uniform circular disc (of mass  $M$  and radius  $R$ ) about four mutually perpendicular tangents AB, BC, CD, DA are  $I_1, I_2, I_3$  and  $I_4$ , respectively (the square ABCD circumscribes the circle). The distance of the center of mass of the disc from its geometrical center is given by

- A.  $\frac{1}{4MR} \sqrt{(I_1 - I_3)^2 + (I_2 - I_4)^2}$
- B.  $\frac{1}{12MR} \sqrt{(I_1 - I_3)^2 + (I_2 - I_4)^2}$
- C.  $\frac{1}{3MR} \sqrt{(I_1 - I_2)^2 + (I_3 - I_4)^2}$
- D.  $\frac{1}{2MR} \sqrt{(I_1 + I_3)^2 + (I_2 + I_4)^2}$



$\frac{3MR^2}{2}$   
 $\frac{MR^2}{2} + MR^2 = I$

$\frac{\Delta L}{L} = 1.03 \text{ mm/r}$

$\frac{\Delta L}{L} = \alpha \Delta T$



$\frac{F}{A} = \frac{Y \Delta L}{L}$

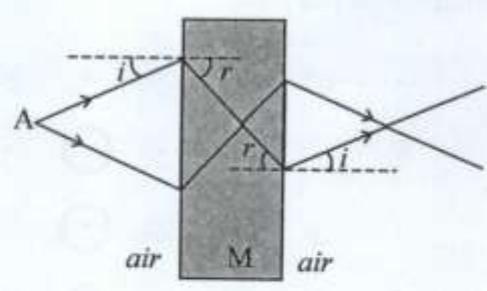
$= (1.1 \times 10^{-5}) (40)$

93. A horizontal steel railroad track has a length of 100 m when the temperature is 25 °C. The track is constrained from expanding or bending. The stress on the track on a hot summer day, when the temperature is 40 °C, is (Note: the linear coefficient of thermal expansion for steel is  $1.1 \times 10^{-5}/^\circ\text{C}$  and the Young's modulus of steel is  $2 \times 10^{11}$  Pa)

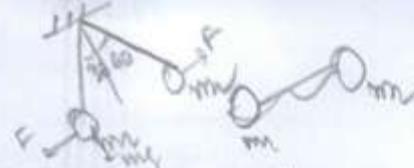
- A.  $6.6 \times 10^7$  Pa
- B.  $8.8 \times 10^7$  Pa
- C.  $3.3 \times 10^7$  Pa
- D.  $5.5 \times 10^7$  Pa

$1.5(1.1 \times 10^{-5}) \times (2 \times 10^{11})$   
 $\approx 3.3 \times 10^6$

94. Electromagnetic waves emanating from a point A (in air) are incident on a rectangular block of material M and emerge from the other side as shown. The angles  $i$  and  $r$  are angles of incidence and refraction when the wave travels from air to the medium. Such paths for the rays are possible

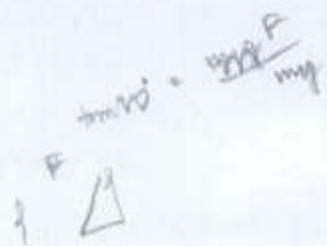


- A. if the material has a refractive index very nearly equal to zero.
- B. only with gamma rays with a wavelength smaller than the atomic nuclei of the material.
- C. if the material has a refractive index less than zero.
- D. only if the wave travels in M with a speed faster than the speed of light in vacuum.

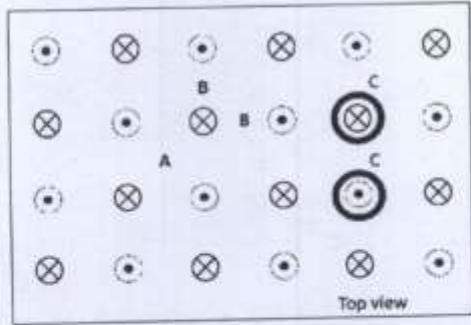


95. Two small metal balls of different mass  $m_1$  and  $m_2$  are connected by strings of equal length to a fixed point. When the balls are given equal charges, the angles that the two strings make with the vertical are  $30^\circ$  and  $60^\circ$ , respectively. The ratio  $m_1/m_2$  is close to

- A. 1.7
- B. 3.0
- C. 0.58
- D. 2.0



96. Consider the regular array of vertical identical current carrying wires (with direction of current flow as indicated in the figure below) protruding through a horizontal table. If we scatter some diamagnetic particles on the table, they are likely to accumulate

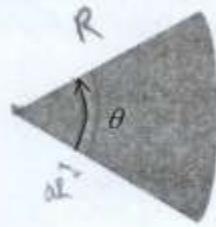


- A. around regions such as A.
- B. around regions such as B.
- C. in circular regions around individual wires such as C.
- D. uniformly everywhere.

$$\frac{m_1 g}{\sqrt{3}} = \sqrt{3} m_2 g \quad \frac{1}{\sqrt{3}} = \frac{F}{m_1 g}$$

$$\frac{F}{m_2 g} = \sqrt{3} \frac{m_1}{m_2} = 3$$

97. The distance between the vertex and the center of mass of a uniform solid planar circular segment of angular size  $\theta$  and radius  $R$  is given by



$$COM = \frac{\int z \cdot dm}{\int dm}$$

$z$

$$dm = (\rho \cdot dr)$$

A.  $\frac{4}{3} R \frac{\sin(\theta/2)}{\theta}$

B.  $R \frac{\sin(\theta/2)}{\theta}$

C.  $\frac{4}{3} R \cos\left(\frac{\theta}{2}\right)$

D.  $\frac{2}{3} R \cos(\theta)$

98. An object is propelled vertically to a maximum height of  $4R$  from the surface of a planet of radius  $R$  and mass  $M$ . The speed of object when it returns to the surface of the planet is

A.  $2\sqrt{\frac{2GM}{5R}}$

B.  $\sqrt{\frac{GM}{2R}}$

$$v = \sqrt{2gR}$$

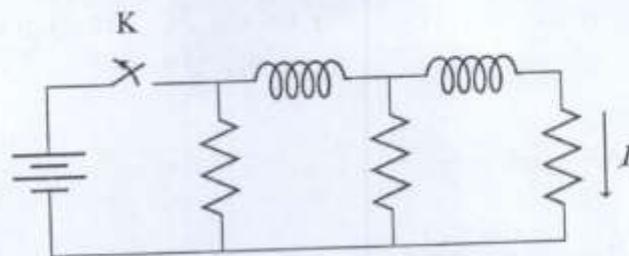
$$v = \sqrt{2gR}$$

C.  $\sqrt{\frac{3GM}{2R}}$

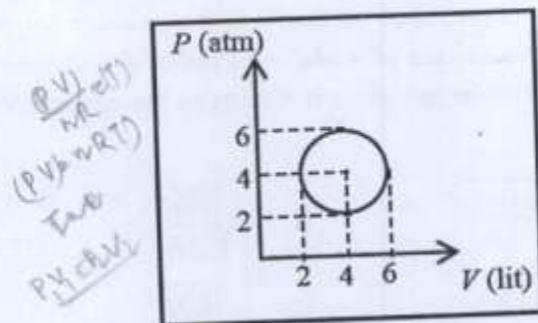
D.  $\sqrt{\frac{GM}{5R}}$

$$v = \sqrt{\frac{GM}{R}}$$

99. In the circuit shown below, all the inductors (assumed ideal) and resistors are identical. The current through the resistance on the right is  $I$  after the key  $K$  has been switched on for a long time. The currents through the three resistors (in order, from left to right) immediately after the key is switched off are



- A.  $2I$  upwards,  $I$  downwards and  $I$  downwards.  
 B.  $2I$  downwards,  $I$  downwards and  $I$  downwards.  
 C.  $I$  downwards,  $I$  downwards and  $I$  downwards.  
 D.  $0$ ,  $I$  downwards and  $I$  downwards.
100. An ideal gas undergoes a circular cycle centered at  $4 \text{ atm}$ ,  $4 \text{ lit}$  as shown in the diagram. The maximum temperature attained in this process is close to



- A.  $30/R$   
 B.  $36/R$   
 C.  $24/R$   
 D.  $16/R$

$$\frac{PV}{nR} = T$$

$$(PV)_{\text{max}} = nRT_{\text{max}}$$

$$T_{\text{max}} = \frac{PV_{\text{max}}}{nR}$$

$$PV = nRT$$

$$R = \frac{PV}{nT}$$

$$= \frac{P(V)}{nT}$$

$$\left( \frac{PV}{nT} \right)$$

$$2R \perp$$

# CHEMISTRY

101. For the reaction  $N_2 + 3X_2 \rightarrow 2NX_3$ , where  $X = F, Cl$  (the average bond energies are  $F-F = 155 \text{ kJ mol}^{-1}$ ,  $N-F = 272 \text{ kJ mol}^{-1}$ ,  $Cl-Cl = 242 \text{ kJ mol}^{-1}$ ,  $N-Cl = 200 \text{ kJ mol}^{-1}$ , and  $N \equiv N = 941 \text{ kJ mol}^{-1}$ ), the heats of formation of  $NF_3$  and  $NCl_3$  in  $\text{kJ mol}^{-1}$ , respectively, are closest to

- A. -226 and +467      B. +226 and -467  
 C. -151 and +311      D. +151 and -311

102. The equilibrium constants for the reactions  $X = 2Y$  and  $Z = P + Q$  are  $K_1$  and  $K_2$ , respectively. If the initial concentrations and the degree of dissociation of  $X$  and  $Z$  are the same, the ratio  $K_1/K_2$  is

- A. 4                              B. 1                               $X = 2Y$   
 C. 0.5                            D. 2                               $Z = P + Q$

103. The geometry and the number of unpaired electron(s) of  $[MnBr_4]^{2-}$ , respectively, are

- A. tetrahedral and 1      B. square planar and 1  
 C. tetrahedral and 5      D. square planar and 5

104. The standard cell potential for  $Zn|Zn^{2+}||Cu^{2+}|Cu$  is 1.10 V. When the cell is completely discharged,  $\log [Zn^{2+}]/[Cu^{2+}]$  is closest to

- A. 37.3                            B. 0.026                             $Zn \rightarrow Zn^{2+} + 2e^-$   
 C. 18.7                            D. 0.052                             $Cu^{2+} + 2e^- \rightarrow Cu$

Handwritten calculations for question 104:

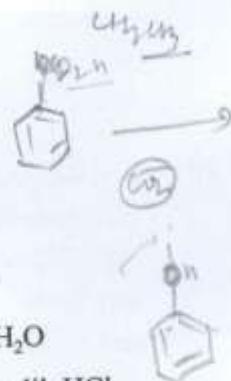
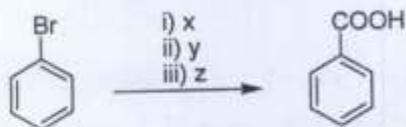
$$0 = 1.1 - \frac{0.0591}{2} \log \frac{[Zn^{2+}]}{[Cu^{2+}]}$$

$$\frac{1.1 (2)}{0.0591} = \log \frac{[Zn^{2+}]}{[Cu^{2+}]}$$

$$37.3 = \log \frac{[Zn^{2+}]}{[Cu^{2+}]}$$

Other notes:  $[MnBr_4]^{2-}$ ,  $14d^5$ ,  $sp^3$ ,  $10$ ,  $39$ ,  $59 \overline{) 2200}$ ,  $177$ ,  $11(200)$ ,  $59$ ,  $127$ .

105. In the reaction

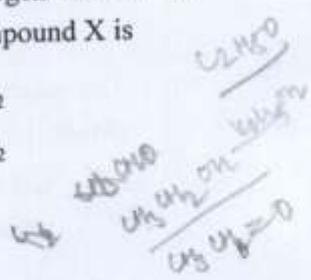


x, y and z are

- A. x = Mg, dry ether; y = CH<sub>3</sub>Cl; z = H<sub>2</sub>O
- B. x = Mg, dry methanol; y = CO<sub>2</sub>; z = dil. HCl
- C. x = Mg, dry ether; y = CO<sub>2</sub>; z = dil. HCl
- D. x = Mg, dry methanol; y = CH<sub>3</sub>Cl; z = H<sub>2</sub>O

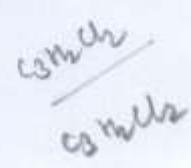
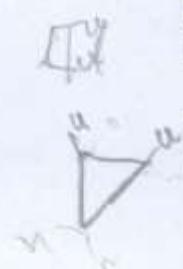
106. An organic compound having molecular formula C<sub>2</sub>H<sub>6</sub>O undergoes oxidation with K<sub>2</sub>Cr<sub>2</sub>O<sub>7</sub>/H<sub>2</sub>SO<sub>4</sub> to produce X which contains 40% carbon, 6.7% hydrogen and 53.3% oxygen. The molecular formula of the compound X is

- A. CH<sub>2</sub>O
- B. C<sub>2</sub>H<sub>4</sub>O<sub>2</sub>
- C. C<sub>2</sub>H<sub>4</sub>O
- D. C<sub>2</sub>H<sub>6</sub>O<sub>2</sub>

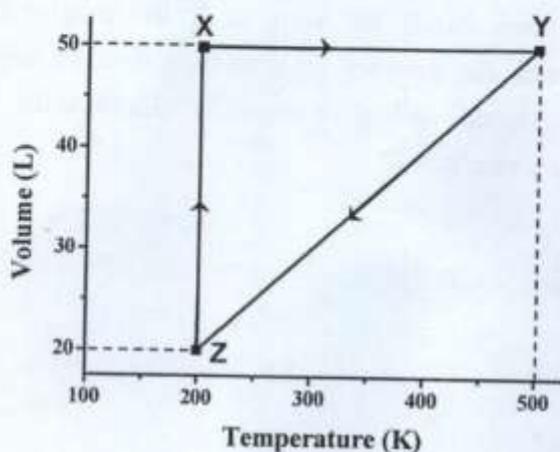


107. The maximum number of cyclic isomers (positional and optical) of a compound having molecular formula C<sub>3</sub>H<sub>2</sub>Cl<sub>2</sub> is

- A. 2
- B. 3
- C. 4
- D. 5



108. The volume vs. temperature graph of 1 mole of an ideal gas is given below

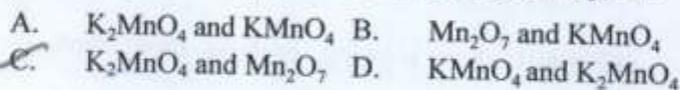


The pressure of the gas (in atm) at X, Y and Z, respectively, are

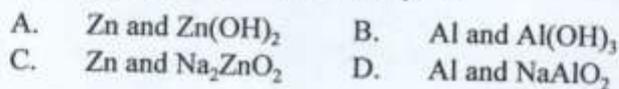
A. 0.328, 0.820, 0.820 - B. 3.28, 8.20, 3.28

C. 0.238, 0.280, 0.280 - D. 32.8, 0.280, 82.0

109.  $\text{MnO}_2$  when fused with  $\text{KOH}$  and oxidized in air gives a dark green compound X. In acidic solution, X undergoes disproportionation to give an intense purple compound Y and  $\text{MnO}_2$ . The compounds X and Y, respectively, are



110. A metal (X) dissolves both in dilute  $\text{HCl}$  and dilute  $\text{NaOH}$  to liberate  $\text{H}_2$ . Addition of  $\text{NH}_4\text{Cl}$  and excess  $\text{NH}_4\text{OH}$  to an  $\text{HCl}$  solution of X produces Y as a precipitate. Y is also produced by adding  $\text{NH}_4\text{Cl}$  to the  $\text{NaOH}$  solution of X. The species X and Y, respectively, are



## BIOLOGY

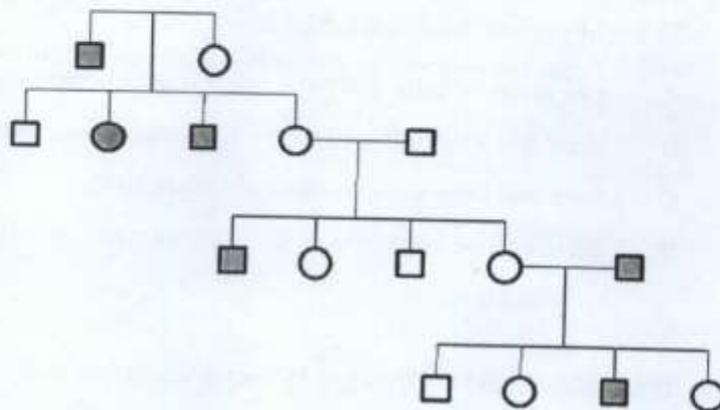
111. How many bands are seen when immunoglobulin G molecules are analysed on a sodium dodecyl sulphate-polyacrylamide gel electrophoresis (SDS-PAGE) under reducing conditions?

- A. 6
- B. 1
- C. 2
- D. 4

112. In a mixed culture of slow and fast growing bacteria, penicillin will

- A. kill the fast growing bacteria more than the slow growing
- B. kill slow growing bacteria more than the fast growing
- C. kill both the fast and slow growing bacteria equally
- D. will not kill bacteria at all

113. Consider the following pedigree over four generations and mark the correct answer below about the inheritance of haemophilia.



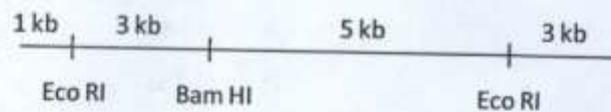
- Normal male
- Haemophilic male
- Normal female
- Haemophilic female

- A. Haemophilia is X-linked dominant  
 B. Haemophilia is autosomal dominant  
 C. Haemophilia is X-linked recessive  
 D. Haemophilia is Y-linked dominant
114. A person has 400 million alveoli per lung with an average radius of 0.1 mm for each alveolus. Considering the alveoli are spherical in shape, the total respiratory surface of that person is closest to
- A. 500 mm<sup>2</sup>                      B. 200 mm<sup>2</sup>  
 C. 100 mm<sup>2</sup>                      D. 1000 mm<sup>2</sup>

115. A mixture of equal numbers of fast and slow dividing cells is cultured in a medium containing a trace amount of radioactively labeled thymidine for one hour. The cells are then transferred to regular (unlabelled) medium. After 24 hrs of growth in regular media
- A. fast dividing cells will have maximum radioactivity
  - B. slow dividing cells will have maximum radioactivity
  - C. both will have same amount of radioactivity
  - D. there will be no radioactivity in either types of cells
116. If a double stranded DNA has 15% cytosine, what is the % of adenine in the DNA?
- A. 15 %
  - B. 70 %
  - C. 35 %
  - D. 30 %
117. The mitochondrial inner membrane consists of a number of infoldings called cristae. The increased surface area due to cristae helps in:
- A. Increasing the volume of mitochondria
  - B. Incorporating more of the protein complexes essential for electron transport chain
  - C. Changing the pH
  - D. Increasing diffusion of ions

118. The activity of a certain protein is dependent on its phosphorylation. A mutation in its gene changed a single amino acid which affected the function of the molecule. Which amino acid change is most likely to account for this observation?
- A. Tyrosine to Tryptophan
  - B. Lysine to valine
  - C. Leucine to isoleucine
  - D. Valine to alanine

119. Consider the linear double stranded DNA shown below. The restriction enzyme sites and the lengths demarcated are shown. This DNA is completely digested with both *EcoRI* and *BamHI* restriction enzymes. If the product is analyzed by gel electrophoresis, how many distinct bands would be observed?



- A. 5
  - B. 2
  - C. 3
  - D. 4
120. Enzyme X catalyzes hydrolysis of GTP into GDP. The GTP-bound form of X transmits a signal that leads to cell proliferation. The GDP-bound form does not transmit any such signal. Mutations in X are found in many cancers. Which of the following alterations of X are most likely to contribute to cancer?
- A. Mutations that increase the affinity of X for GDP.
  - B. Mutations that decrease the affinity of X for GTP.
  - C. Mutations that decrease the rate of GTP hydrolysis.
  - D. Mutations that prevent expression of enzyme X.

ROUGH WORK

$$+ \int_0^{\infty} e^{-at} - \frac{(e^{-at})}{a} - \frac{(e^{-at})}{a}$$

$$\frac{a}{14} + \frac{b}{3} + \frac{c}{2} + 2 -$$

$$\frac{2a}{11} + \frac{b}{3} - \frac{c}{2} + 2$$

$$\left(\frac{2b}{3} + 4\right)$$

$$\frac{2(3)}{2(3)} + 4 = 5$$

$$(2 - 2e^{-2}) -$$

$$\int_2^{\infty} e^{-t}(2-t) dt$$

ROUGH WORK

$$(-2e^{-2} + 2)$$

$$(-2e^{-2})_2^{\infty}$$

$$-2e^{-2} + \int_0^2 e^{-t} dt$$

$$\int_2^{\infty} t e^{-t} dt + \int_0^2 e^{-t}(2-t) dt$$

$$2 \int_0^2 e^{-t} dt - \int_0^2 t e^{-t} dt$$

$$(2e^{-2})_2^{\infty} - 2e^{-2} + (2e^{-2})$$

$$-2(e^{-t})_0^2$$

$$+ \int_0^2 e^{-t} dt$$

$$-2e^{-2} -$$

$$-2e^{-2} + (1 - e^{-2})$$

$$-e^{-2} - \int_2^{\infty} e^{-t}(2-t) dt$$

$$- +1$$

$$2 \int_2^{\infty} e^{-t} dt - \int_2^{\infty} t e^{-t} dt$$

$$\underline{(e^{-2})}$$

$$-2(1 - e^{-2}) -$$

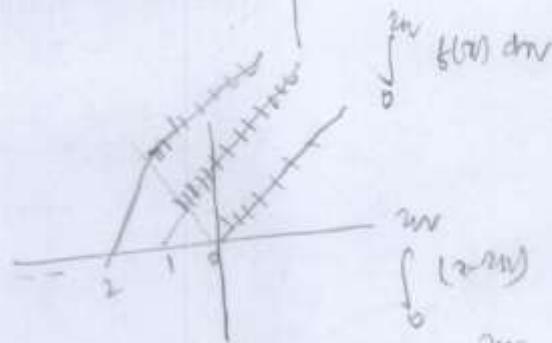
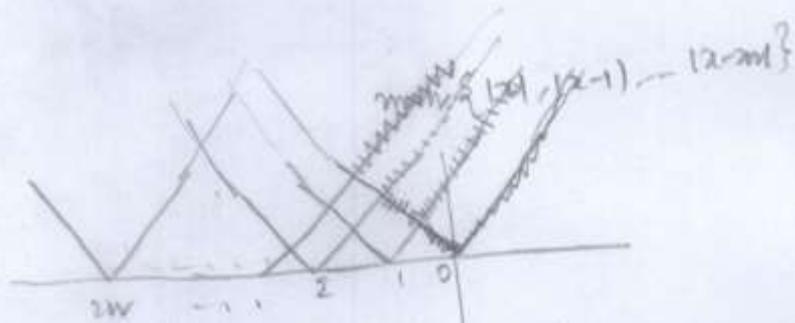
$$(2e^{-2})_0^{\infty}$$

$$+ \int_2^{\infty} e^{-t} dt$$

$$\underline{2 - 2e^{-2} + 1}$$

$$e^{-2} - (1 - e^{-2})$$

ROUGH WORK



$$\int_0^{2w} (2-w) dx$$

$$\frac{2w^2}{2} = 2w^2 - 2w(2)$$

$$2w^2 - 4w$$

$$\frac{2w^2}{2}$$