## Series JBB/5

## SET-2

Code No. 430/5/2
Roll No. $\square$

## Note:

(I) Please check that this question paper contains 20 printed pages.
(II) Code number given on the right hand side of the question paper should be written on the title page of the answer-book by the candidate.
(III) Please check that this question paper contains 40 questions.
(IV) Please write down the Serial Number of the questions in the answer book before attempting it.
(V) 15 minute time has been allotted to read this question paper. The question paper will be distributed at 10.15 a.m. From 10.15 a.m. to 10.30 a.m., the students will read the question paper only and will not write any answer on the answer-book during this period.

# MATHEMATICS (BASIC) HINTS \& SOLUTIONS 

## Time allowed: 3 hours <br> General Instructions:

Maximum Marks : 80

Read the following instructions very carefully and strictly follow them.
(i) This question paper comprises Four Sections - A, B, C and D There are 40 questions in the question paper. All questions are compulsory.
(ii) Section A - Questions no. 1 to 20 comprises of 20 questions of one mark each.
(iii) Section B - Questions no. 21 to $\mathbf{2 6}$ comprises of $\mathbf{6}$ questions of two mark each.
(iv) Section C - Questions no. 27 to 34 comprises of 8 questions of three mark each.
(v) Section D - Questions no. $\mathbf{3 5}$ to $\mathbf{4 0}$ comprises of $\mathbf{6}$ questions of four mark each.
(vi) There is no overall choice in the question paper. However, an internal choice has been provided in 2 questions of one mark, 2 questions of two marks, 3 questions of three marks and 3 questions of four marks. You have to attempt only one of the choices in such questions.
(vii) In addition to this, separate instructions are given with each section and question, wherever necessary.
(viii) Use of calculators is not permitted.

## SECTION-A

## Question numbers 1 to 20 carry 1 mark each.

## Choose the correct option in question numbers 1 to 10.

1. For the following frequency distribution:

| Class: | $0-5$ | $5-10$ | $10-15$ | $15-20$ | $20-25$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency : | 8 | 10 | 19 | 25 | 8 |

The upper limit of median class is
(A) 15
(B) 10
(C) 20
(D) 25

Sol. (A)

| Class | $0-5$ | $5-10$ | $10-15$ | $15-20$ | $20-25$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 8 | 10 | 19 | 25 | 8 |
| C.F. | 8 | 18 | 37 | 62 | 70 |

$N=70$ and $\frac{N}{2}=35$ So just greater to 35 is 37 So median class is $10-15$ upper limit of median class is 15
2. The probability of an impossible event is
(A) 1
(B) $\frac{1}{2}$
(C) not defined
(D) 0

Sol. (D) 0
3. If $(3,-6)$ is the mid-point of the line segment joining $(0,0)$ and $(x, y)$, then the point $(x, y)$ is
(A) $(-3,6)$
(B) $(6,-6)$
(C) $(6,-12)$
(D) $\left(\frac{3}{2},-3\right)$

Sol. (C) Co-ordinate of midpoint $=\left(\frac{x_{1}+x_{2}}{2}, \frac{y_{1}+y_{2}}{2}\right)$
So,

$$
3=\frac{0+x}{2} \Rightarrow x=6
$$

And

$$
-6=\frac{0+y}{2} \Rightarrow y=-12
$$

So $(x, y)=(6,-12)$
4. The discriminant of the quadratic equation $4 x^{2}-6 x+3=0$ is
(A) 12
(B) 84
(C) $2 \sqrt{3}$
(D) -12

Sol. (D) Discriminant $D=b^{2}-4 a c$

$$
\begin{aligned}
& =(-6)^{2}-4(4)(3) \\
& =36-48=-12
\end{aligned}
$$

5. In the given circle in Figure-1, number of tangents parallel to tangent $P Q$ is


Figure-1
(A) 0
(B) many
(C) 2
(D) 1

Sol.
(D) 1
6. $8 \cot ^{2} \mathrm{~A}-8 \operatorname{cosec}^{2} \mathrm{~A}$ is equal to
(A) 8
(B) $\frac{1}{8}$
(C) -8
(D) $-\frac{1}{8}$

Sol. $\quad(C)=8\left[\operatorname{Cot}^{2} A-\operatorname{Cosec}^{2} A\right]$
$=8\left[-\left\{\operatorname{Cosec}^{2} A-\operatorname{Cot}^{2} A\right\}\right]$
$=8[-1]=-8$
7. The point on $x$-axis which divides the line segment joining $(2,3)$ and $(6,-9)$ in the ratio $1: 3$ is
(A) $(4,-3)$
(B) $(6,0)$
(C) $(3,0)$
(D) $(0,3)$

Sol. (C) Let solid is ( $x, 0$ )
$\mathrm{x}=\frac{\mathrm{mx} 2+\mathrm{nx}_{1}}{\mathrm{~m}+\mathrm{n}}$
$x=\frac{1(6)+3(2)}{1+3}=\frac{12}{4}=3$
So point is $(3,0)$
8. If a pair of linear equations is consistent, then the lines represented by them are
(A) parallel
(B) intersecting or coincident
(C) always coincident
(D) always intersecting

Sol. (B) Intersecting or Coincident
9. The total surface area of a frustum-shaped glass tumbler is $\left(r_{1}>r_{2}\right)$
(A) $\pi r_{1} l+\pi r_{2} l$
(B) $\pi l\left(r_{1}+r_{2}\right)+\pi r_{2}^{2}$
(C) $\frac{1}{3} \pi h\left(r_{1}^{2}+r_{2}^{2}+r_{1} r_{2}\right)$
(D) $\sqrt{h^{2}+\left(r_{1}-r_{2}\right)^{2}}$

Sol. (B) T.S.A. of Frustum $=\pi\left(r_{1}+r_{2}\right) \ell+\pi r_{2}{ }^{2}$

$$
=\pi \ell\left(r_{1}+r_{2}\right)+\pi r_{2}^{2}
$$

10. 120 can be expressed as a product of its prime factors as
(A) $5 \times 8 \times 3$
(B) $15 \times 2^{3}$
(C) $10 \times 2^{2} \times 3$
(D) $5 \times 2^{3} \times 3$

Sol. (D) $120=2^{3} \times 3^{1} \times 5^{1}$

## Fill in the blanks in question numbers 11 to 15.

11. Area of quadrilateral $A B C D=$ Area of $\triangle A B C+$ area of $\qquad$ -
Sol.


Area of quadrilateral
$A B C D=$ Area of $\triangle A B C+$ Area of $\triangle A C D$
12. If the radii of two spheres are in the ratio $2: 3$, then the ratio of their respective volumes is $\qquad$ -
Sol. Volume of sphere $=\frac{4}{3} \pi r^{3}$
So ratio of volumes $=\left(\frac{r_{1}}{r_{2}}\right)^{3}=\left(\frac{2}{3}\right)^{3}=8: 27$

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13. If 2 is a zero of the polynomial $a x^{2}-2 x$, then the value of ' $a$ ' is $\qquad$ .

Sol. If 2 is a zero of the Polynomial then its satisfy given Polynomial so

$$
\text { Put } P(2)=0
$$

$$
a(2)^{2}-2(2)=0
$$

$4 a-4=0$
$a=1$
14. A line intersecting a circle in two points is called a $\qquad$ .
Sol. Secant
15. All squares are $\qquad$ (congruent/similar)
Sol. Similar

## Answer the following question numbers 16 to 20 :

16. A dice is thrown once. If getting a six, is a success, then find the probability of a failure.

Sol. Total out comes $=1,2,3,4,5,6$
So probability of a failure $=\frac{5}{6}$
17. Find the value of $x$ so that $-6, x, 8$ are in A.P.

## OR

Find the $11^{\text {th }}$ term of the A.P. $-27,-22,-17,-12$,
Sol. $-6, x, 8$ are in A.P. So

$$
\begin{aligned}
& 2 x=-6+8 \\
& 2 x=2 \\
& x=1
\end{aligned}
$$

OR
$-27,-22,-17,-12 \ldots \ldots . . . . . . . . . . . . .(i n ~ A . P$.
$a=-27, d=-22+27=5$
So, $T_{n}=a+(n-1) d$
$\mathrm{T}_{11}=-27+(11-1) 5$
$\mathrm{T}_{11}=-27+50$
$\mathrm{T}_{11}=23$
$\mathrm{T}_{11}=23$
18. In Figure-2, the angle of elevation of the top of a tower $A C$ from a point $B$ on the ground is $60^{\circ}$. If the height of the tower is 20 m , find the distance of the point from the foot of the tower.


Figure-2

Sol.


In $\triangle A B C$
$\tan 60^{\circ}=\frac{A C}{A B}$
$\sqrt{3}=\frac{20}{\mathrm{AB}}$
$A B=\frac{20}{\sqrt{3}} \quad$ or $\quad \frac{20}{3} \sqrt{3} \approx 11.54$
19. Evaluate :
$\tan 40^{\circ} \times \tan 50^{\circ}$
OR
If $\cos \mathrm{A}=\sin 42^{\circ}$, then find the value of A .
Sol. $\quad \operatorname{Tan} 40^{\circ} \times \tan 50^{\circ}$
$\tan 40^{\circ} \times \tan \left(90^{\circ}-40^{\circ}\right)$
$\tan 40^{\circ} \times \cot 40^{\circ}$
$=1$
OR
$\cos A=\sin 42$
$\cos A=\sin (90-48)$
$\cos A=\cos 48$
on comparing
$\mathrm{A}=48^{\circ}$
20. Find the height of a cone of radius 5 cm and slant height 13 cm . .

Sol. $\quad r^{2}=h^{2}+r^{2}$
$13^{2}=h^{2}+5^{2}$
$h^{2}=144$
$\mathrm{h}=12 \mathrm{~cm}$

## SECTION B

## Question numbers 21 to 26 carry 2 marks each.

21. In Figure-3, $\triangle A B C$ and $\triangle X Y Z$ are shown. If $A B=3 \mathrm{~cm}, B C=6 \mathrm{~cm}, A C=2 \sqrt{3} \mathrm{~cm}, \angle A=80^{\circ}, \angle B=$ $60^{\circ}, X Y=4 \sqrt{3} \mathrm{~cm}, Y Z=12 \mathrm{~cm}$ and $X Z=6 \mathrm{~cm}$, then find the value of $\angle Y$.


## Figure-3

Sol. $\operatorname{In} \triangle A B C$ and $\triangle X Z Y$

$$
\begin{aligned}
& \frac{A B}{X Z}=\frac{3}{6}=\frac{1}{2} \\
& \frac{B C}{Y Z}=\frac{6}{12}=\frac{1}{2} \\
& \frac{A C}{X Z}=\frac{2 \sqrt{3}}{4 \sqrt{3}}=\frac{1}{2}
\end{aligned}
$$

By sss
$\Delta \mathrm{ABC} \sim \Delta X Z Y$
$\therefore \angle \mathrm{X}=\angle \mathrm{A}=80^{\circ}$
$\angle \mathrm{Z}=\angle \mathrm{B}=60^{\circ}$
By Angle sum property of $\Delta$
In $\triangle X Y Z$
$\angle \mathrm{X}+\angle \mathrm{Y}+\angle \mathrm{Z}=180^{\circ}$
$80^{\circ}+\angle Y+60^{\circ}=180^{\circ}$
$\angle \mathrm{Y}=180^{\circ}-140^{\circ}=40^{\circ}$
22. Find the mean for the following distribution :

| Classes : | $5-15$ | $15-25$ | $25-35$ | $35-45$ |
| :--- | :---: | :---: | :---: | :---: |
| Frequency : | 2 | 4 | 3 | 1 |

OR
The following distribution shows the transport expenditure of 100 employees :

| Expenditure <br> (in Rs.): | $200-400$ | $400-600$ | $600-800$ | $800-1000$ | $1000-1200$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Number of <br> employees : | 21 | 25 | 19 | 23 | 12 |

Find the mode of the distribution.

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## Sol.

| Classes | (f) <br> Frequency | $(x)$ <br> Class mark | x.f |
| :--- | :---: | :---: | :---: |
| $5-15$ | 2 | 10 | 20 |
| $15-25$ | 4 | 20 | 80 |
| $25-35$ | 3 | 30 | 90 |
| $35-45$ | 1 | 40 | 40 |
| $\sum \mathrm{f}=10$ |  |  |  |

$$
\overline{\mathrm{X}}=\frac{\sum \mathrm{fx}}{\sum \mathrm{f}}=\frac{230}{10}=23
$$

$\therefore \quad$ Mean is 23


Model Class in 400-600
$\therefore \quad \ell=400$
Class size $(\mathrm{g})=600-400=200$
$\mathrm{f}_{1}=25$
$\mathrm{f}_{0}=21$
$\mathrm{f}_{2}=19$
Mode $=\ell++\frac{f_{1}-f_{0}}{2 f_{1}-f_{0}-f_{2}} \times h$
$=400+\frac{25-21}{2(25)-21-19} \times 200$
$=400+\frac{4}{50-40} \times 200=400+\frac{4}{10} \times 200$
$=400+80$
$=480$
$\therefore$ Mode is 480
23. Solve for $x: 2 x^{2}+5 \sqrt{5} x-15=0$

Sol. $2 x^{2}+5 \sqrt{5} x-15=0$
$2 x^{2}+6 \sqrt{5} x-\sqrt{5} x-15=0$
$2 x[x+3 \sqrt{5}]-\sqrt{5}[x+3 \sqrt{5}]=0$
$(x+3 \sqrt{5})(2 x-\sqrt{5})=0$
So $x=-3 \sqrt{5}$ or $\frac{\sqrt{5}}{2}$

24．Check whether $6^{n}$ can end with the digit＇ 0 ＇（zero）for any natural number $n$ ．

## OR

Find the LCM of 150 and 200.
Sol．Any positive integer ending with the digit zero is divisible by 2 and 5 so its prime factorization must contain the prime 2 and 5 ．

$$
6^{n}=(2 \times 3)^{n}=2^{n} \times 3^{n}
$$

$\Rightarrow \quad$ The prime in the factorisation of $6^{n}$ is 2 and 3 ．
$\Rightarrow \quad 5$ does not occur in the prime factorisation of $6^{n}$ for any $n$ ．
$\Rightarrow \quad 6^{\mathrm{n}}$ does not end with the digit zero for any natural number n ．

## OR

$$
\begin{aligned}
& 150=2 \times 3 \times 5^{2} \\
& 200=2^{3} \times 5^{2} \\
& \text { LCM } \quad 2^{3} \times 3^{1} \times 5^{2} \\
& =600
\end{aligned}
$$

25．If $5 \tan \theta=4$ ，show that $\frac{5 \sin \theta-3 \cos \theta}{5 \sin \theta+3 \cos \theta}=\frac{1}{7}$ ．
Sol．L．H．S．$=\frac{5 \tan \theta-3}{5 \tan \theta+3}$
$\frac{5\left(\frac{4}{5}\right)-3}{5\left(\frac{4}{5}\right)+3}=\frac{1}{7}$
＝R．H．S．

26． 14 defective bulbs are accidentally mixed with 98 good ones．It is not possible to just look at the bulb and tell whether it is defective or not．One bulb is taken out at random from this lot．Determine the probability that the bulb taken out is a good one
Sol．Defective bulb $=14$
Good Bulb＝ 98
total Bulb $=14+98=112$
Probability of take out a good bulb $=\frac{\text { Noof goodbulb }}{\text { totalno．of bulb }}$
$=\frac{98}{112}=\frac{14}{16}=\frac{7}{8}$

## SECTION C

## Question numbers 27 to 34 carry 3 marks each．

27．Krishna has an apple orchard which has a $10 \mathrm{~m} \times 10 \mathrm{~m}$ sized kitchen 3 garden attached to it．She divides it into a $10 \times 10$ grid and puts soil and manure into it．She grows a lemon plant at A，a coriander plant at $B$ ，an onion plant at $C$ and a tomato plant at $D$ ．Her husband Ram praised her kitchen garden and points out that on joining $A, B, C$ and $D$ they may form a parallelogram．Look at the below figure carefully and answer the following questions ：

(i) Write the coordinates of the points $\mathrm{A}, \mathrm{B}, \mathrm{C}$ and D , using the $10 \times 10$ grid as coordinate axes.
(ii) Find whether $A B C D$ is a parallelogram or not.

Sol. (i) $A=(2,2)$

$$
\begin{aligned}
& \mathrm{B}=(5,4) \\
& \mathrm{C}=(7,7) \\
& \mathrm{D}=(4,5)
\end{aligned}
$$

(ii) Now $A B=\sqrt{(5-2)^{2}+(4-2)^{2}}=\sqrt{9+4}=\sqrt{13}$

$$
\begin{aligned}
& \mathrm{BC}=\sqrt{(7-5)^{2}+(7-4)^{2}}=\sqrt{4+9}=\sqrt{13} \\
& \mathrm{CD}=\sqrt{(4-7)^{2}+(5-7)^{2}}=\sqrt{9+4}=\sqrt{13} \\
& \mathrm{DA}=\sqrt{(2-4)^{2}+(2-5)^{2}}=\sqrt{4+9}=\sqrt{13} \\
& \because \quad \mathrm{AB}=\mathrm{BC}=\mathrm{CD}=\mathrm{DA}=\sqrt{13}
\end{aligned}
$$

So it is a rhombus.
All rhombus are parallelogram.
So it is also a parallelogram.
28. Prove that $\sqrt{3}$ is an irrational number.

Sol. Let $\sqrt{3}$ is a rational number
$\therefore \sqrt{3}=\frac{\mathrm{a}}{\mathrm{b}}$ [where $\mathrm{a} \& \mathrm{~b}$ are co-primes $\& \mathrm{~b} \neq 0$ ]
$\mathrm{a}^{2}=3 \mathrm{~b}^{2}$
$\Rightarrow 3$ divides $\mathrm{a}^{2}$
$\Rightarrow 3$ also divides a
$\Rightarrow \mathrm{a}=3 \mathrm{c}$
[Where c is any non-zero positive integer]
$\Rightarrow \mathrm{a}^{2}=9 \mathrm{c}^{2}$
From equation (i)
$3 b^{2}=9 c^{2}$
$\Rightarrow b^{2}=3 c^{2} \quad \Rightarrow \quad 3$ divides $b^{2}$
$\Rightarrow 3$ also divides b
So, 3 is a common factor of $a$ and $b$.
Our assumption is wrong, because $a$ and $b$ are not co-primes.
It means $\sqrt{3}$ is an irrational number.
29. Prove that : $\frac{\tan \theta}{1-\cot \theta}+\frac{\cot \theta}{1-\tan \theta}=1+\sec \theta \operatorname{cosec} \theta$.

Sol. $\frac{\tan \theta}{1-\cot \theta}+\frac{\cot \theta}{1-\tan \theta}$

$=\frac{\tan ^{2} \theta}{\tan \theta-1}+\frac{1}{\tan \theta(1-\tan \theta)}$
$=\frac{\tan ^{2} \theta}{\tan \theta-1}-\frac{1}{\tan \theta(\tan \theta-1)}$
$=\frac{\tan ^{3} \theta-1}{\tan \theta(\tan \theta-1)}$
$=\frac{(\tan \theta-1)\left(\tan ^{2} \theta+1+\tan \theta\right)}{\tan \theta(\tan \theta-1)}$
$=\frac{\left(\tan ^{2} \theta+1+\tan \theta\right)}{\tan \theta}$
$=\tan \theta+\cot \theta+1$
$=\frac{\sin \theta}{\cos \theta}+\frac{\cos \theta}{\sin \theta}+1$
$=\frac{\sin ^{2} \theta+\cos ^{2} \theta}{\sin \theta \cos \theta}+1$
$=\frac{1}{\sin \theta \cos \theta}+1$
$=\sec \theta \operatorname{cosec} \theta+1$.
30. Two concentric circles are of radii 5 cm and 3 cm . Find the length of chord of the larger circle with touches the smaller circle.
Sol.

$A C=\sqrt{5^{2}-3^{2}}=4$
$A B=4 \times 2=8 \mathrm{~cm}$.
31. The difference between two numbers is 26 and the larger number exceeds thrice of the smaller number by 4 . Find the numbers.
Solve for $x$ and $y$ :
$\frac{2}{x}+\frac{3}{y}$ and $\frac{5}{x}-\frac{4}{y}=-2$
Sol. Let numbers are $x \& y$, where $x>y$.
So According to question -
$x-y=26 \ldots \ldots$. (i)
and $\quad x-3 y=4$
Put value of $x$ from (i) to (ii)
$26+y-3 y=4$
$26-2 y=4$
$2 y=22$
$y=11$
and $x=26+11=37$
So numbers are 37 and 11
$\frac{2}{x}+\frac{3}{y}=13$
multiply the equation by 5
$\frac{10}{x}+\frac{15}{y}=65$
and $\frac{5}{x}-\frac{4}{y}=-2$
multiple the equation by 2
$\frac{10}{x}-\frac{8}{y}=-4$.
Subtract eq. (ii) from (i)
$\frac{15}{y}+\frac{8}{y}=65+4$
$\frac{23}{y}=69$
$\frac{1}{y}=3$
$y=\frac{1}{3}$
Put the value of $y$ is eq. (i)
$\frac{2}{x}+\frac{3}{1 / 3}=13$
$\frac{2}{x}+9=13$
$\frac{2}{x}=4$
$x=\frac{1}{2}$
So

$$
x=\frac{1}{2} \& y=\frac{1}{3}
$$

32. In Figure-4, $A B$ and $C D$ are two diameters of a circle (with centre $O$ ) perpendicular to each other and $O D$ is the diameter of the smaller circle. If $O A=7 \mathrm{~cm}$, then find the area of the shaded region.


Figure-4

## OR

In Figure $-5, \mathrm{ABCD}$ is a square with side 7 cm . A circle is drawn circumscribing the square. Find the area of the shaded region.


Figure-5

Sol.


Area of Shaded region $=($ Area of smaller circle $)+($ Area of segment AC and AD)
$=\left(\frac{22}{7} \times \frac{7}{2} \times \frac{7}{2}\right)+2\left[\frac{1}{4}\left(\frac{22}{7} \times 7 \times 7\right)-\left(\frac{1}{2} \times 7 \times 7\right)\right]$
$=\frac{77}{2}+2\left[\frac{77}{2}-\frac{49}{2}\right]$
$=\frac{77}{2}+28=\frac{133}{2}=66.5 \mathrm{~cm}^{2}$


Diameter of circle $=$ Diagonal of square
$\mathrm{d}=\sqrt{2} \times$ side
$\Rightarrow d=7 \sqrt{2} \mathrm{~cm}$
$\Rightarrow r=\frac{7}{\sqrt{2}} \mathbf{c m}$
area of shaded portion = area of circle - area of square
$\Rightarrow$ area of shaded portion $=\pi r^{2}-$ side $^{2}$
$\Rightarrow$ area of shaded portion $=\frac{22}{7} \times \frac{7}{\sqrt{2}} \times \frac{7}{\sqrt{2}}-7 \times 7=77-49$
$=28 \mathrm{~cm}^{2}$
33. Construct a triangle with its sides $4 \mathrm{~cm}, 5 \mathrm{~cm}$ and 6 cm . Then construct a triangle similar to it whose sides are $\frac{2}{3}$ of the corresponding sides of the first triangle.

OR
Draw a circle of radius 25 cm . Take a point $P$ at a distance of 8 cm from its centre. Construct a pair of tangents from the point P to the circle.
Sol.


Steps of Construction
(i) Draw a line segment $\mathrm{AB}=5 \mathrm{~cm}$.
(ii) With A as centre and radius $\mathrm{AC}=4 \mathrm{~cm}$, draw an arc.
(iii) With B as centre and $\mathrm{BC}=6 \mathrm{~cm}$, draw another arc, intersecting the arc draw in step (ii) at C .
(iv) Join $A C$ and $B C$ to obtain $\triangle A B C$.
(v) Below $A B$, make an acute angle $\angle B A X$.
(vi) Along $A X$, mark off three points (greater of 2 and 3 in $\frac{2}{3}$ ) $A_{1}, A_{2}, A_{3}$ such that $A A_{1}=A_{1} A_{2}=A_{2} A_{3}$.
(vii) Join $A_{3} B$.
(viii) Draw $A_{2} B^{\prime} \| A_{3} B$, meeting $A B$ at $B^{\prime}$.

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(ix) From $B^{\prime}$, draw $B^{\prime} C^{\prime} \| B C$, meeting $A C$ at $C^{\prime}$.
$A B^{\prime} C^{\prime}$ is the required triangle, each of the whose sides is two-third of the corresponding sides of $\triangle A B C$.


Steps of Construction
(i) Draw a circle of radius 2.5 cm . Let its centre be O .
(ii) Join $\mathrm{OP}=8 \mathrm{~cm}$ and bisect it. Let M be mid-point of OP .
(iii) Taking M as centre and MO as radius draw a circle to intersect C in two points, say A and B .
(iv) Join PA and PB. These are the required tangents from $P$ to $C(O, r)$.
34. If the sum of first 7 terms of an A.P. is 49 and that of 17 terms is 289 , then find the sum of first $n$ terms.

Sol. Given $\mathrm{S}_{7}=49$
and $\mathrm{S}_{17}=289$
Now $\mathrm{S}_{7}=\frac{7}{2}[2 \mathrm{a}+(7-1) \mathrm{d}]=49$
$2 a+6 d=14$
$a+3 d=7 \ldots$. (i)
and $\mathrm{S}_{17}=\frac{17}{2}[2 \mathrm{a}+(17-1) \mathrm{d}]=289$
$2 a+16 d=34$
$a+8 d=17 \ldots .$. (ii)
Subtract eq (i) from eq(ii)
$5 \mathrm{~d}=10$
$d=2$
Put the value of $d$ in equation (i)
$a+3(2)=7$
$\mathrm{a}=1$
So sum of first's ' $n$ ' terms $=\frac{n}{2}[2 a+(n-1) d]$
$=\frac{\mathrm{n}}{2}[2+(\mathrm{n}-1) 2]$
$=n(1+n-1)=n^{2}$

## SECTION D

## Question numbers 35 to 40 carry 4 marks each.

35. Two water taps together can fill a tank in $9 \frac{3}{8}$ hours. The tap of larger diameter takes 10 hours less than the smaller one to fill the tank separately. Find the time in which each tap can separately fill the tank.

OR
A rectangular park is to be designed whose breadth is 3 m less than its length. Its area is to be 4 square metres more than the area of a park that has already been made in the shape of an isosceles triangle with its base as the breadth of the rectangular park and of altitude 12 m . Find the length and breadth of the park.

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Sol. Let the time taken by the smaller pipe to fill the tank be $x \mathrm{hr}$.
Time taken by the larger pipe $=(x-10) \mathrm{hr}$.
Part of tank filled by smaller pipe in 1 hour $=\frac{1}{x}$
Part of tank filled by larger pipe in 1 hour $=\frac{1}{x-10}$
It is given that the tank can be filled in $9 \frac{3}{8}=\frac{75}{8}$ hours by both the pipes
together.
Therefore,
$\frac{1}{x}+\frac{1}{x-10}=\frac{8}{75}$
$\frac{x-10+x}{x(x-10)}=\frac{8}{75}$
$\Rightarrow \frac{2 x-10}{x(x-10)}=\frac{8}{75}$
$\Rightarrow 75(2 x-10)=8 x^{2}-80 x$
$\Rightarrow 150 x-750=8 x^{2}-80 x$
$\Rightarrow 8 x^{2}-230 x+750=0$
$\Rightarrow 8 x^{2}-200 x-30 x+750=0$
$\Rightarrow 8 x(x-25)-30(x-25)=0$
$\Rightarrow(x-25)(8 x-30)=0$
i.e., $x=25, \frac{30}{8}$

Time taken by the smaller pipe cannot be $\frac{30}{8}=3.75$ hours. As in this case, the time taken by the larger pipe will be negative, which is logically not possible.
so $x=25 \mathrm{hr}$.
$\& x-10=15 \mathrm{hr}$.

## OR

Let the length of rectangular park be x
Breath $=x-3$
$\therefore$ Base of isosceles $\Delta=\mathrm{x}-3$
Altitude = 12 m
Area of rectangular park $=x(x-3)$
Area of isosceles triangle $=\frac{1}{2} \times(x-3) 12$
ATP $\rightarrow$

$$
\begin{aligned}
& x(x-3)=\frac{1}{2}(x-3) \times 12+4 \\
& x^{2}-3 x=6 x-18+4 \\
& x^{2}-9 x+14=0 \\
& (x-7)(x-2)=0 \\
& x=7,2
\end{aligned}
$$

$X=7 \quad x=2$ (not possible)
$\therefore$ Length $=7 \mathrm{~m}$
Breadth $=7-3=4 \mathrm{~m}$
36. Find the curved surface area of frustum of a cone of height 12 cm and radii of circular ends are 9 cm and 4 cm .
Sol. $h=12 \mathrm{~cm}$
$r_{1}=9 \mathrm{~cm}$
$\mathrm{r}_{2}=4 \mathrm{~cm}$
So $\ell=\sqrt{h^{2}+\left(r_{1}-r_{2}\right)^{2}}=\sqrt{12^{2}+(9-4)^{2}} \ell=13$
Now C.S.A. of frustum $=\pi\left(r_{1}+r_{2}\right) \ell$
$=\frac{22}{7} \times(9+4) 13$
$=\frac{22 \times 13 \times 3}{7}=169 \pi \mathrm{~cm}^{2} \quad$ or $\quad 530.92 \mathrm{~cm}^{2}$
37. Draw a less than' ogive for the following frequency distribution:

| Classes: | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency: | 7 | 14 | 13 | 12 | 20 | 11 | 15 | 8 |

Sol.

| Observation | Cumulative Frequency |
| :---: | :---: |
| Less than 10 | 7 |
| Less than 20 | 21 |
| Less than 30 | 34 |
| Less than 40 | 46 |
| Less than 50 | 66 |
| Less than 60 | 77 |
| Less than 70 | 92 |
| Less than 80 | 100 |


38. If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, prove that the other two sides are divided in the same ratio.

OR
In Figure-6, in an equilateral triangle $A B C, A D \perp B C, B E \perp A C$ and $C F \perp A B$. Prove that $4\left(A D^{2}+B E^{2}+\right.$ $\left.C F^{2}\right)=9 A^{2}$


Figure-6
Sol. Given: A $\triangle A B C$ in which a line parallel to side $B C$ intersects other two sides $A B$ and $A C$ at $D$ and $E$ respectively.
To Prove : $\quad \frac{A D}{D B}=\frac{A E}{E C}$.


Construction : Join BE and CD and draw $\mathrm{DM} \perp \mathrm{AC}$ and $\mathrm{EN} \perp \mathrm{AB}$.
Proof : Area of $\triangle A D E=\frac{1}{2}$ (base $\times$ height) $=\frac{1}{2} A D \times E N$.
Area of $\triangle A D E$ is denoted as $\operatorname{ar}(A D E)$.
So, $\operatorname{ar}(\mathrm{ADE})=\frac{1}{2} \mathrm{AD} \times \mathrm{EN} \quad$ and $\quad \operatorname{ar}(\mathrm{BDE})=\frac{1}{2} \mathrm{DB} \times \mathrm{EN}$.
Therefore, $\frac{\operatorname{ar}(\mathrm{ADE})}{\operatorname{ar}(\mathrm{BDE})}=\frac{\frac{1}{2} \mathrm{AD} \times \mathrm{EN}}{\frac{1}{2} \mathrm{DB} \times \mathrm{EN}}=\frac{\mathrm{AD}}{\mathrm{DB}}$
Similarly, $\operatorname{ar}(A D E)=\frac{1}{2} A E \times D M$ and $\operatorname{ar}(D E C)=\frac{1}{2} E C \times D M$.
And $\frac{\operatorname{ar}(\mathrm{ADE})}{\operatorname{ar}(\mathrm{DEC})}=\frac{\frac{1}{2} \mathrm{AE} \times \mathrm{DM}}{\frac{1}{2} \mathrm{EC} \times \mathrm{DM}}=\frac{\mathrm{AE}}{\mathrm{EC}}$
(ii)

Note that $\triangle$ BDE and $\triangle$ DEC are on the same base DE and between the two parallel lines $B C$ and $D E$. So, $\operatorname{ar}(\mathrm{BDE})=\operatorname{ar}(\mathrm{DEC})$
Therefore, from (i), (ii) and (iii), we have :

$$
\frac{A D}{D B}=\frac{A E}{E C} \quad \text { Hence Proved. }
$$



In $\triangle A B D$
$A D^{2}=A B^{2}-B D^{2}$ $\qquad$ (1)
$B E^{2}=B C^{2}-C E^{2}$ $\qquad$
$\mathrm{CF}^{2}=A C^{2}-\mathrm{AF}^{2}$ $\qquad$
Adding eq. (1), (2) and (3)
$A D+B E+C F^{2}=A B^{2}-B D^{2}+B C^{2}-C E^{2}+A C^{2}-A F^{2}$

$$
=A B^{2}-\frac{A B^{2}}{4}+A B^{2}-\frac{A B^{2}}{4}+A B^{2}-\frac{A B^{2}}{4}
$$

$4\left(A D^{2}+B E^{2}+C F^{2}\right)=9 A B^{2}$
39. Find other zeroes of the polynomial
$p(x)=3 x^{4}-4 x^{3}-10 x^{2}+8 x+8$,
if two of its zeroes are $\sqrt{2}$ and $-\sqrt{2}$.

## OR

Divide the polynomial $g(x)=x^{3}-3 x^{2}+x+2$ by the polynomial $x^{2}-2 x+1$ and verify the division algorithm.

Sol. $\quad p(x)=3 x^{4}-4 x^{3}-10 x^{2}+8 x+8$
Two factors are $(x-\sqrt{2})(x+\sqrt{2})$

$$
\begin{aligned}
& =x^{2}-2 \\
& \begin{array}{c}
x^{2}-2 \sqrt{3 x^{4}-4 x^{3}-10 x^{2}+8 x+8}\left(3 x^{2}-4 x-4\right. \\
3 x^{4} \quad-6 x^{2}
\end{array} \\
& -4 x^{3}-4 x^{2}+8 x+8 \\
& \begin{array}{c}
-4 x^{3} \quad \pm 8 x \\
\hline-4 x^{2}+8 \\
-4 x^{2}+8 \\
0
\end{array}
\end{aligned}
$$

$\therefore$ other factor is $3 x^{2}-4 x-4$

$$
=(3 x+2)(x-2)
$$

So other two zeros are $\frac{-2}{3}, 2$

## OR

$$
\begin{gathered}
x^{2}-2 x+1 \begin{array}{l}
\begin{array}{l}
\frac{x^{3}-3 x^{2}+x+2}{x^{3}-2 x^{2}+x} \\
-+\quad- \\
-x^{2}+2
\end{array} \\
\frac{+-1}{-x^{2}+2 x-1}+\quad+\begin{array}{l}
-2 x+3
\end{array}
\end{array}
\end{gathered}
$$

So, quoticut $=x-1$ and remainder $=-2 x+3$
Justification :-

$$
\text { Dividenal }=x^{3}-3 x^{2}+x+2
$$

and $\Rightarrow$ divisor $\times$ quotient + remainder
$\Rightarrow\left(\mathrm{x}^{2}-2 \mathrm{x}+1\right)(\mathrm{x}-1)+(-2 \mathrm{x}+3)$
$\Rightarrow x^{3}-3 x^{2}+x+2=$ Divided
40. A TV tower stands vertically on the bank of a canal. From a point on the other bank directly opposite the tower, the angle of elevation of the top of the tower is $60^{\circ}$. From another point on the same bank, which is 20 m away from this point, on the line joining this point to the foot of the bower, the angle of elevation of the top of the tower is $30^{\circ}$. Find the width of the canal.

Sol.


Let $A B$ is TV tower and $B C$ is a canal

$$
\text { and } A B=x m \& B C=y m
$$

So in $\triangle A B C$
$\tan 60^{\circ}=\frac{x}{y}$
$\sqrt{3}=\frac{x}{y}$
$x=\sqrt{3} y$
Now in $\triangle A B D$
$\tan 30^{\circ}=\frac{x}{y+20}$
$\frac{1}{\sqrt{3}}=\frac{\sqrt{3} y}{y+20}[$ from eq.(i)]
$y+20=3 y$
$20=2 y$
$y=10 \mathrm{~m}$.

